

# Math for Operators

*If you can't do the numbers, you can't make the water (or clean the wastewater!)*

Version 1.0 & May 2019



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Acknowledgements:

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## Editor

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## Content & Goals:

- To enhance and reinforce the math skills for operators

# Outline:

## Workshop topics

**Math Basics**

**Aids to Navigation**

**Units of Measure**

**Algebra**

**Trigonometry**

**Conversion Factors**

**Practical Applications**

**Examples – *2<sup>nd</sup> hour***

**Problem Solving Practice – *3<sup>rd</sup> hour***

# Math Basics

***You can't run the place without it!***

# Math Basics - Real Basics

$$1 + 1 = 2$$

$$2 * 2 = 4$$

*The numbers by themselves are generally not useful until we attach units to them so we know what we are measuring*

We will assume you have basic math (arithmetic) skills; + - x & /

# Math Basics – Adding Units of Measure

1 foot + 1 inch  $\neq$  2

# Math Basics – When adding and subtracting must be the **SAME** units

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

~~$$1 \text{ foot} + (1 \text{ inch} * (12 \text{ inches/foot})) =$$~~

$$1 \text{ foot} + (1 \text{ inch} * (1 \text{ foot}/12 \text{ inches})) =$$

*Convert to a common unit of measure, in this case feet*

# Closer Look – Keeping track of UNITS

*For addition need common units*

$$1 \text{ foot} + 1 \text{ inch} * \frac{1 \text{ ft}}{12 \text{ inches}} = 1 \frac{1}{12} \text{ ft or } \frac{13}{12}$$

*Accurate but maybe not useful*



# Unit Basics – It makes a difference what you want to do

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

$$1 \text{ foot} + 1 \text{ inch} * (1 \text{ foot}/12 \text{ inches}) =$$

$$1 \text{ foot} + 1/12 \text{ foot} = 1 \frac{1}{12} \text{ feet}$$

$$1 \text{ foot} + .083 \text{ foot} = 1.083 \text{ feet}$$

*Useful for a surveyor or bulldozer  
operator, or for measuring liquid depth*

# Unit Basics 2

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

$$1 \text{ foot} * (12 \text{ inches/foot}) + 1 \text{ inch} =$$
$$12 \text{ inches} + 1 \text{ inch} = 13 \text{ inches}$$

*Useful for a plumber or  
carpenter*



*Our choice of units  
has a lot to do with  
who we are and  
what we need to do  
with the “answer”*

# Math Basics – Short Cuts

## Exponents

$$2 * 2 = 4$$

$$2^2 = 4$$

$$3^2 = 3 * 3 = 9$$

$$30^{1.85} = 540.35$$

Whole number exponents used in area and volume formulas

Fractional exponents used in friction formulas and other equations

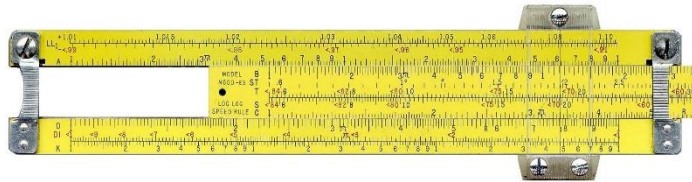
You can often do these by hand or in your head.

For this one you need your calculator, a computer, a slide rule, or log tables.

FOUR-PLACE COMMON LOGARITHMS

N	0				5				6				7				8				9				Proportional Parts								
	1	2	3	4	5	6	7	8	9	0	1	2	3	4	5	6	7	8	9	0	1	2	3	4	5	6	7	8	9	0	1	2	3
10	0000	0045	0086	0128	0170	0212	0255	0294	0334	0374	4	8	12	17	21	25	29	33	37	4	8	11	15	19	23	26	30	34					
11	0414	0455	0492	0531	0569	0607	0645	0682	0719	0755	9	0	4	8	11	14	17	21	24	28	3	7	10	14	17	21	24	28	31				
12	0792	0828	0864	0899	0934	0969	1004	1038	1072	1106	6	10	13	16	19	22	25	28	31	34	7	10	13	16	19	22	25	28	31	34			
13	1139	1173	1206	1239	1271	1303	1335	1367	1399	1430	1	4	7	10	13	16	19	22	25	28	3	6	9	12	15	18	21	24	27				
14	1461	1492	1523	1553	1584	1614	1644	1673	1703	1732	1	4	7	10	13	16	19	22	25	28	3	6	9	12	15	18	21	24	27				
15	1761	1790	1818	1847	1875	1903	1931	1959	1987	2014	5	6	8	11	14	17	20	22	25	28	3	5	8	11	14	17	20	22	25	28			
16	2041	2068	2095	2122	2148	2175	2201	2227	2253	2279	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
17	2304	2330	2355	2380	2405	2430	2455	2480	2504	2529	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
18	2553	2577	2601	2625	2648	2672	2695	2718	2742	2765	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
19	2788	2810	2831	2852	2878	2900	2923	2945	2967	2989	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
20	3010	3032	3054	3075	3096	3118	3139	3160	3181	3201	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
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22	3424	3444	3464	3483	3502	3522	3541	3560	3579	3598	2	4	6	8	10	12	14	16	18	20	2	4	6	8	10	12	14	16	18	20			
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27	4314	4330	4346	4362	4378	4393	4409	4425	4440	4456	2	3	5	7	9	10	11	13	14	15	2	3	5	7	9	10	11	13	14	15			
28	4472	4487	4502	4518	4533	4548	4564	4579	4594	4609	2	3	5	7	9	10	11	12	14	15	2	3	5	7	9	10	11	12	14	15			
29	4624	4639	4654	4669	4683	4698	4713	4728	4742	4757	1	3	4	6	7	9	10	12	13	14	1	3	4	6	7	9	10	12	13	14			
30	4771	4786	4800	4814	4829	4843	4857	4871	4886	4900	1	3	4	6	7	9	10	11	13	14	1	3	4	6	7	9	10	11	13	14			
31	4914	4928	4942	4955	4969	4983	4997	5011	5024	5038	1	3	4	6	7	8	10	11	12	13	1	3	4	6	7	8	10	11	12	13			
32	5051	5065	5079	5092	5105	5119	5132	5145	5159	5172	1	3	4	5	7	8	9	11	12	13	1	3	4	5	7	8	9	10	11	12			
33	5185	5198	5211	5224	5237	5250	5263	5276	5289	5302	1	3	4	5	6	8	9	10	12	13	1	3	4	5	6	8	9	10	11	12			
34	5315	5328	5340	5353	5366	5378	5391	5403	5416	5428	1	3	4	5	6	8	9	10	11	12	1	3	4	5	6	8	9	10	11	12			
35	5441	5453	5465	5478	5490	5502	5514	5527	5539	5551	1	2	4	5	6	7	9	10	11	12	1	2	4	5	6	7	9	10	11	12			
36	5563	5575	5587	5599	5611	5623	5635	5647	5658	5670	1	2	4	5	6	7	8	10	11	12	1	2	4	5	6	7	8	10	11	12			
37	5682	5694	5705	5717	5729	5740	5752	5763	5775	5786	1	2	3	5	6	7	8	9	10	11	1	2	3	5	6	7	8	9	10	11			
38	5798	5809	5821	5832	5843	5855	5866	5877	5888	5899	1	2	3	5	6	7	8	9	10	11	1	2	3	5	6	7	8	9	10	11			
39	5911	5922	5933	5944	5955	5966	5977	5988	5999	6010	1	2	3	4	5	7	8	9	10	11	1	2	3	4	5	7	8	9	10	11			
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47	6721	6730	6739	6749	6758	6767	6776	6785	6794	6803	1	2	3	4	5	6	7	8	9	10	1	2	3	4	5	6	7	8	9	10	11		
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49	6902	6911	6920	6929	6937	6946	6955	6964	6972	6981	1	2	3	4	5	6	7	8	9	10	1	2	3	4	5	6	7	8	9	10	11		
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52	7160	7168	7177	7185	7193	7202	7210	7218	7226	7235	1	2	3	4	5	6	7	8	9	10	1	2	3	4	5	6	7	8	9	10	11		
53	7243	7251	7259	7267	7275	7284	7292	7300	7308	7316	1	2	3	4	5	6	7	8	9	10	1	2	3	4	5	6	7	8	9	10	11		
54	7324	7332	7340	7348	7356	7364	7372	7380	7388	7396	1	2	3	4	5	6	7	8	9	10	1	2	3	4	5	6	7	8	9	10	11		
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Images from International Slide Rule Museum, coolstuff4891.blogspot.com+, & Abelard.com



# Math Basics – Short Cuts

Then how do the units follow?

$$2 * 2 = 2^2 = 4$$

$$\text{ft} * \text{ft} = \text{ft}^2$$

$$3^3 = 3 * 3 * 3 = 27$$

$$\text{ft} * \text{ft} * \text{ft} = \text{ft}^3$$

# Math Basics – 2 & 3 dimensions

$$2 * 2 = 4$$

$$2^2 = 4$$

$$\text{ft} * \text{ft} = \text{ft}^2$$

AREA



$$3^3 = 3 * 3 * 3 = 27$$

$$\text{ft} * \text{ft} * \text{ft} = \text{ft}^3$$

Volume



# Math Basics – Multiplication & Division

$$2 \text{ ft} * 2 \text{ ft} = 4 \text{ Square Feet (ft}^2\text{)}$$

$$\text{ft}^2 = \text{sq ft} = \text{sf}$$

*All abbreviations  
are used*

# Math Basics – Multiplication & Division

$$2 \text{ ft} * 2 \text{ inches} = 4 \text{ foot-inch}$$

Correct  
But not a useable term

# Math Basics – Multiplication & Division

$$2 \text{ acre} * 2 \text{ feet} = 4 \text{ acre-feet}$$

Very correct!  
Is a common term for lake  
volume

*Not all mixed  
units are  
wrong*

*(So how big is an acre you  
ask? 43,560 sf or a square  
208.71 feet on a side)*



# Math Basics – Multiplication & Division

## *Calculating areas*

$$= 2 \text{ ft} * 2 \text{ inches}$$

$$= 2 \text{ ft} * 2 \text{ inches} * (1 \text{ foot}/12 \text{ inches})$$

$$= 2 \text{ ft} * 2/12 \text{ ft}$$

$$= 4/12 \text{ ft}^2$$

$$= 0.33 \text{ ft}^2 \text{ (or } 1/3 \text{ ft}^2)$$

# Math Basics – Multiplication & Division

*But what if we want sq. in. instead of sq. ft.?*

$$= 2 \text{ ft} * 2 \text{ inches}$$

$$= (2 \text{ ft} * (12 \text{ inches}/1 \text{ foot})) * 2 \text{ inches}$$

$$= 24 \text{ inches} * 2 \text{ inches}$$

$$= 48 \text{ inches}^2$$

# Math Basics – Multiplication & Division

*Calculating flow rates*

$$= \frac{200 \text{ gallons}}{20 \text{ minutes}}$$

$$= 10 \text{ gallons per minute (gpm)}$$

*gpm is one of many  
terms of flow  
measurement*

# Aids to Navigation

*Resources that will come in handy*

# Aids to Navigation - Handout

## Formula/Conversion Table

Water Treatment, Distribution, & Water Laboratory Exams

$$\text{Alkalinity, mg/L as CaCO}_3 = \frac{(\text{Titrant Volume, mL})(\text{Acid Normality})}{\text{Sample Volume, mL}}$$

$$\text{Amps} = \frac{\text{Volts}}{\text{Ohms}}$$

$$\text{Area of Circle}^* = (0.785)(\text{Diameter}^2)$$

$$\text{Area of Circle} = (3.14)(\text{Radius}^2)$$

$$\text{Area of Cone (lateral area)} = (3.14)(\text{Radius})\sqrt{\text{Radius}^2 + \text{Height}^2}$$

$$\text{Area of Cone (total surface area)} = (3.14)(\text{Radius})(\text{Radius} + \sqrt{\text{Radius}^2 + \text{Height}^2})$$

$$\text{Area of Cylinder (total exterior surface area)} = [\text{End \#1 SA}] + [\text{End \#2 SA}] + [(3.14)(\text{Diameter})(\text{Height or Depth})]$$

*Where SA = surface area*

$$\text{Area of Rectangle}^* = (\text{Length})(\text{Width})$$

$$\text{Area of Right Triangle}^* = \frac{(\text{Base})(\text{Height})}{2}$$

$$\text{Average (arithmetic mean)} = \frac{\text{Sum of All Terms}}{\text{Number of Terms}}$$

$$\text{Average (geometric mean)} = [(X_1)(X_2)(X_3)(X_4)(X_n)]^{1/n} \quad \text{The } n^{\text{th}} \text{ root of the product of } n \text{ numbers}$$

$$\text{Blending} = (V_1)(C_1) + (V_2)(C_2) = (V_3)(C_3) \quad \text{Where } V = \text{volume or}$$

Graphics from ABC Professional Operators



## Formula/Conversion Table

Wastewater Treatment, Collection, Industrial Waste, & Wastewater Laboratory Exams



$$\text{Alkalinity, mg/L as CaCO}_3 = \frac{(\text{Titrant Volume, mL})(\text{Acid Normality})(50,000)}{\text{Sample Volume, mL}}$$

$$\text{Amps} = \frac{\text{Volts}}{\text{Ohms}}$$

$$\text{Area of Circle}^* = (0.785)(\text{Diameter}^2)$$

$$\text{Area of Circle} = (3.14)(\text{Radius}^2)$$

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$$\text{Biochemical Oxygen Demand (seeded), mg/L} = \frac{[(\text{Initial DO, mg/L}) - (\text{Final DO, mg/L}) - \text{Seed Correction Factor, mg/L}][300 \text{ mL}]}{\text{mL of Sample}}$$

$$\text{Biochemical Oxygen Demand (unseeded), mg/L} = \frac{[(\text{Initial DO, mg/L}) - (\text{Final DO, mg/L})][300 \text{ mL}]}{\text{mL of Sample}}$$

# Units of Measure

*Tracking what we count*

## Time for an Example



A 20 foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?

# Time for an Example

A 20 foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?

$$\frac{10,000 \text{ gallons}^* \quad 1 \text{ hour}}{2 \text{ hours} \quad * \quad 60 \text{ minutes}}$$

*Change units from what you are given to what you need*



# Time for an Example

A 20 foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?

$$\frac{10,000 \text{ gallons} * \cancel{1 \text{ hour}}}{\cancel{2 \text{ hours}} * 60 \text{ minutes}} = 83.3 \text{ gpm}$$

*Average flow rate. Why is this likely not the continuous flow rate beginning to end?*

# Time for an Example

Same flow, different units

$$10,000 \text{ gallons} / 7.48 \text{ gallons} / \text{cu ft}$$

$$= 1,336.89 \text{ cu ft}$$

$$= \frac{1,336.89 \text{ ft}^3}{2 \text{ hrs} \times 60 \text{ min.} / \text{hr} \times 60 \text{ sec.} / \text{min.}}$$

$$= 0.186 \text{ cubic feet per second (cfs)}$$

*Volume per unit of time*

# Time for an Example

Could we go from gpm to cfs another way?

$$10,000 \text{ gallons} / 120 \text{ minutes} = 83.3 \text{ gpm}$$

*From the info we have this is the quickest way to get volume / unit time*

$$83.3 \text{ gpm} \times \text{conversion factor} \rightarrow ? \text{ cfs}$$

*Look in our aids and tables to find a conversion factor that fits*

$$83.3 \text{ gpm} \times 0.002228 \text{ cfs} / \text{gpm}$$

$$= 0.186 \text{ cubic feet per second (cfs)}$$

# Time for Another Example

Different starting information

$$= \frac{200 \text{ cu ft}}{20 \text{ seconds}}$$

$$= 10 \text{ cubic feet per second (cfs)}$$

*Volume per unit of time*

# Percentage, Fraction & Decimal



If the Mariners went 1 for 4 on recent road trip  
... demonstrate winning

As a fraction

As a decimal

As a percentage

# Percentage, Fraction & Decimal



If the Mariners went 1 for 4 on recent road trip  
... demonstrate winning

$$\frac{1}{4} \text{ Fraction}$$

0.25 Decimal

25% Percentage

# Algebra

*Just who is “X” and what do they want?*

# First We Need to Understand Math Order of Operations

- The order in which operations should be done is abbreviated as PEMDAS
  - Parentheses **()**
  - Exponents **^**
  - Multiplication & Division (from left to right) **\* /**
  - Addition & Subtraction (from left to right) **+ -**
  - **“Please Excuse My Dear Aunt Sally”**



# Algebra – Solving for X (and sometimes half of the rest of the alphabet)

*Addition*

$$X + 3 = 12$$

*Looking to isolate X on one side of the equation*

$$X + 3 - 3 = 12 - 3$$

$$X = 9$$

Subtract 3 from each side of the equal sign

# Algebra – Solving for X

*Subtraction*

$$X - 3 = 12$$

*Again we are looking to isolate X on one side of the equation*

$$X - 3 + 3 = 12 + 3$$

$$X = 15$$

Add 3 from each side of the equal sign

# Algebra – Solving for X

$$3 * X = 12$$

*Multiplication*

$$\frac{3 * X = 12}{3 \quad 3}$$

$$\frac{\cancel{3} * X = 12}{\cancel{3} \quad 3}$$

$$X = 4$$

Divide each side by 3

# Algebra – Solving for X

$$X / 3 = 12$$

*Division*

$$\frac{X * 3}{3} = 12 * 3$$

$$\frac{\cancel{X * 3}}{\cancel{3}} = 12 * 3$$

$$X = 36$$

Multiply each side by 3

# Algebra – Solving for X

$$36 / X = 12$$

$$\frac{36 * X}{X * 12} = \frac{12 * X}{12}$$

$$\frac{36 * \cancel{X}}{\cancel{X} * 12} = \frac{\cancel{12} * X}{\cancel{12}}$$

$$X = 3$$

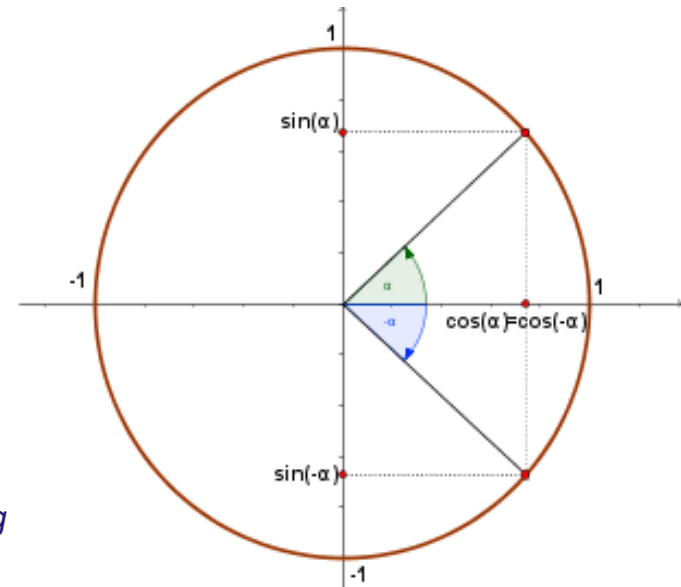
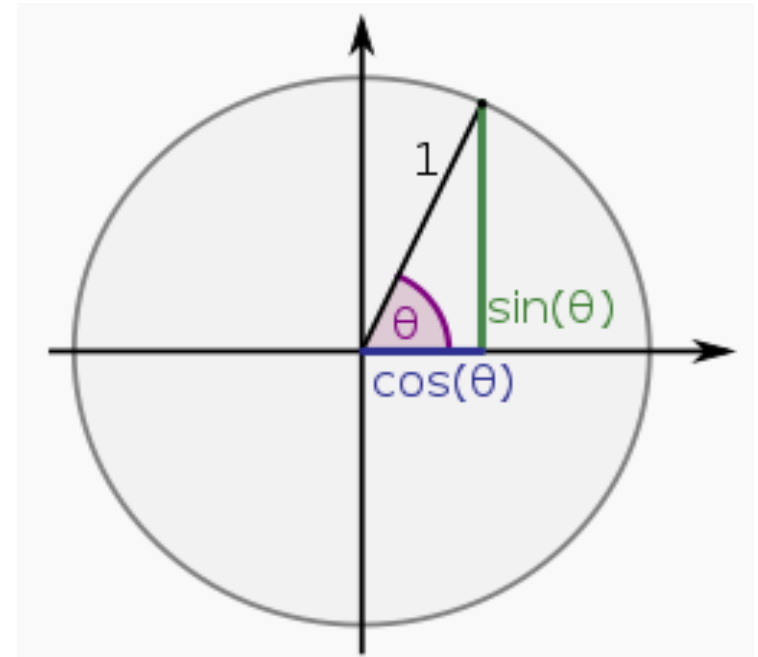
Multiply each side by X to bring X to the numerator and divide each side by 12 to isolate X on one side of the equation

# Trigonometry

*It's all about relationships!*

# Trigonometry

- From Greek trigonon "triangle" + metron "measure"
- New terms
  - Angle (theta,  $\theta$ )
  - Sine
  - Cosine
  - Tangent



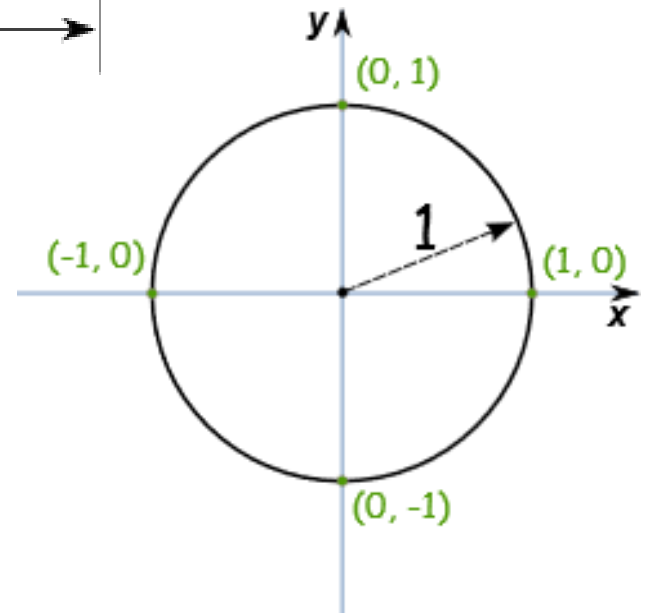
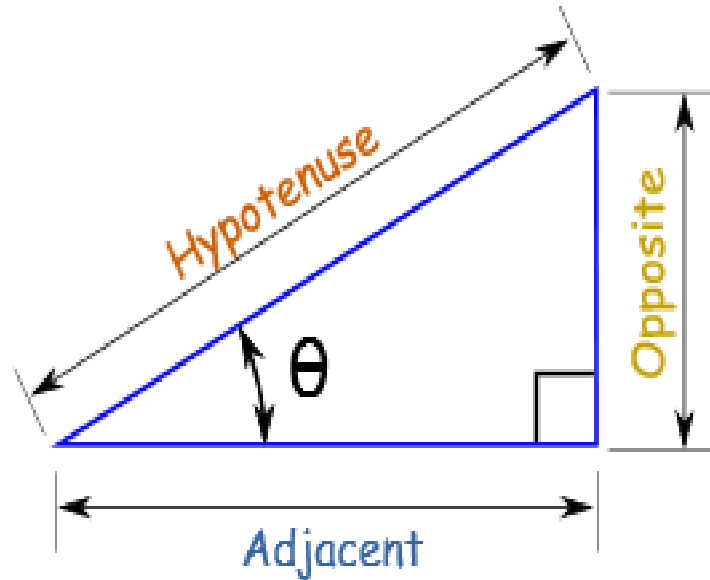
*Graphics from Wikipedia & MathPortal.org*

# How are They Defined?

$$\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}$$

$$\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}$$

$$\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$$



Angle	Degrees	Radians
⊥ Right Angle	90°	$\pi/2$
— Straight Angle	180°	$\pi$
○ Full Rotation	360°	$2\pi$

Graphics from Mathisfun.com



# Conversion Factors

***It's all about tracking units!***

# Conversion Factors are Your Friend!

*Most all of water and wastewater math is about converting from one set of units to another.*

# Conversion Factors are Your Friend!

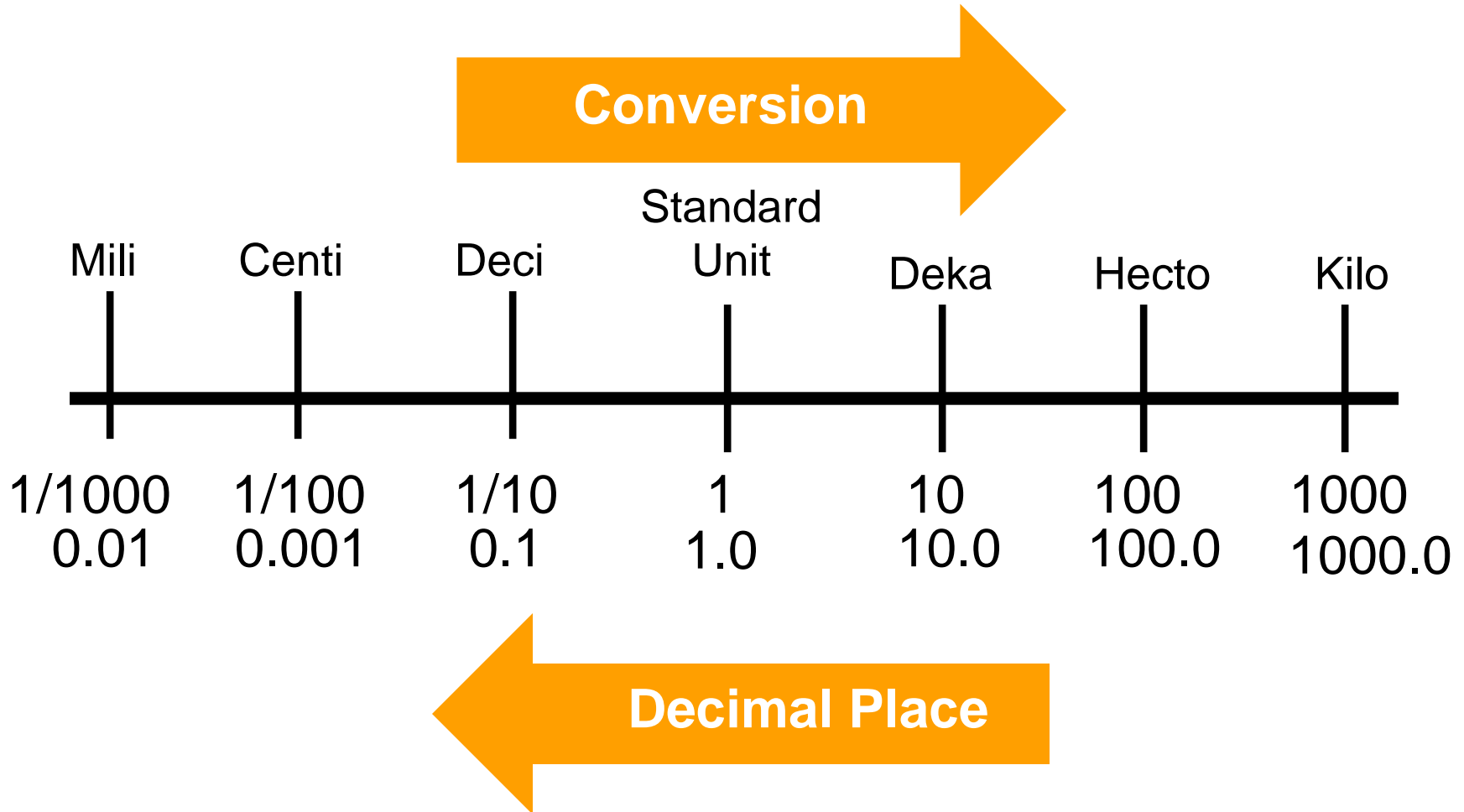
1 foot of water = 0.433 psi

1 cubic foot = 7.48 gallons

1 gallon water = 8.34 pounds

Memorize these (and other)  
conversion factors!

# Conversion Factors are Your Friends!



# Time Conversion Example



Determine how many seconds are in a day.

# Starting Point



1d

Start with 1 day and head towards seconds, one unit of measure at a time.

# One Step at a Time Days to Hours

1d

24 hr

d

24 hour per day

# One Step at a Time

~~1d~~

24 hr

~~d~~

Days cancel out



# One Step at a Time – Hours to Minutes

~~1d~~

24 hr

60 min

~~d~~

hr

60 minutes per hour

# One Step at a Time – Hours to Minutes

~~1d~~

~~24 hr~~

60 min

~~d~~

~~hr~~

Hours cancel

# One Step at a Time – Minutes to Seconds

~~1d~~

~~24 hr~~

60 min

60 sec

~~d~~

~~hr~~

min

60 Seconds per minute

# One Step at a Time

~~1d~~

~~24 hr~~

~~60 min~~

60 sec

~~d~~

~~hr~~

~~min~~

Minutes cancel

# Now do the Math

Multiply

$$24 \times 60 \times 60 =$$

86,400 seconds in 1 day

# Keeping Track of the Units

1 foot of water = 0.433 psi



What is the pressure of 3 feet of water?

# Keeping Track of the Units

1 foot of water = 0.433 psi

$$3 \text{ feet of water} * \frac{0.433 \text{ psi}}{1 \text{ foot of water}}$$

# Keeping Track of the Units

1 foot of water = 0.433 psi

$$\frac{3 \text{ feet of water} * 0.433 \text{ psi}}{1 \text{ foot of water}}$$

$$= 1.3 \text{ psi}$$



# Keeping Track of Units

1 foot of water = 0.433 psi



If the pressure is 3 psi what is that in feet of water?

# Keeping Track of Units

1 foot of water = 0.433 psi

$$\frac{3 \cancel{\text{psi}} * 1 \text{ foot of water}}{0.433 \cancel{\text{psi}}}$$

= 6.9 feet of water

# Keeping Track of Units

1 cubic foot = 7.48 gallons

 How many cubic feet in 100 gallons?

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ gallons} * \frac{1 \text{ cubic foot}}{7.48 \text{ gallons}}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \cancel{\text{gallons}} * \frac{1 \text{ cubic foot}}{7.48 \cancel{\text{gallons}}}$$

$$= 13.4 \text{ cubic feet (ft}^3\text{)}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons



How many gallons in 100 cubic feet?

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ ~~cubic feet~~} * \frac{7.48 \text{ gallons}}{1 \text{ ~~cubic foot~~}}$$

=748 gallons



# Keeping Track of Units

1 gallon water = 8.34 pounds



How many gallons in 100 pounds of water?

# Keeping Track of Units

1 gallon water = 8.34 pounds

100 pounds \*  $\frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$

# Keeping Track of Units

1 gallon water = 8.34 pounds

$$100 \cancel{\text{ pounds}} * \frac{1 \text{ gallon water}}{8.34 \cancel{\text{ pounds}}}$$

= 12 gallons

# Keeping Track of Units

1 gallon water = 8.34 pounds



How many pounds in 100 gallons of water?

# Keeping Track of Units

1 gallon water = 8.34 pounds

100 gallons \*  $\frac{8.34 \text{ pounds}}{1 \text{ gallon water}}$

# Keeping Track of Units

1 gallon water = 8.34 pounds

$$100 \cancel{\text{ gallons}} * \frac{8.34 \text{ pounds}}{1 \cancel{\text{ gallon water}}}$$

= 834 pounds

# Examples

***Let's try out the process***

# Problem

How many gallons in a ton of water?





# Problem – Changing Units

How many gallons in a ton of water?

1 gallon water = 8.34 pounds

1 ton = 2000 pounds

# Problem

How many gallons in a ton of water?

$$1 \text{ ton} * \frac{2000 \text{ pounds}}{1 \text{ ton}} * \frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$$

# Problem

How many gallons in a ton of water?

$$1 \cancel{\text{ton}}^* \times \frac{2000 \text{ pounds}}{1 \cancel{\text{ton}}} \times \frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$$

# Problem

How many gallons in a ton of water?

$$\cancel{1 \text{ ton}}^* \times \frac{\cancel{2000 \text{ pounds}}}{\cancel{1 \text{ ton}}} * \frac{1 \text{ gallon water}}{\cancel{8.34 \text{ pounds}}}$$

$$= 239.8 \text{ gallons}$$

# Problem

How many cubic feet in a ton of water?



# Problem

How many cubic feet in a ton of water?

$$1 \text{ ton} * \frac{2000 \text{ pounds}}{1 \text{ ton}} * \frac{1 \text{ gallon water}}{8.34 \text{ pounds}} * \frac{1 \text{ cubic foot}}{7.48 \text{ gallons}}$$

# Problem

How many cubic feet in a ton of water?

$$\cancel{1 \text{ ton}} * \frac{2000 \cancel{\text{ pounds}}}{\cancel{1 \text{ ton}}} * \frac{1 \cancel{\text{ gallon water}}}{8.34 \cancel{\text{ pounds}}} * \frac{1 \text{ cubic foot}}{7.48 \cancel{\text{ gallons}}}$$

$$= 32.1 \text{ cubic feet}$$

# Problem – Short cut if you know the conversion factor

How many cubic feet in a ton of water?

$$1 \cancel{\text{ ton}} * \frac{2000 \cancel{\text{ pounds}}}{1 \cancel{\text{ ton}}} * \left( \frac{1 \text{ cubic foot}}{62.4 \cancel{\text{ pounds}}} \right)$$

$$= 32.1 \text{ cubic feet}$$



# Significant Figures & Rounding

Significant figures –

How many # after the decimal point?

Usually one significant figure after the decimal point is sufficient or 3 numbers

So instead of 11.99034325234

It would be 12.0

11.09 would be 11.1

11.04 would be 11.0

# Practical Applications

*How do we use this ability?*

# Distance, Area and Volumes

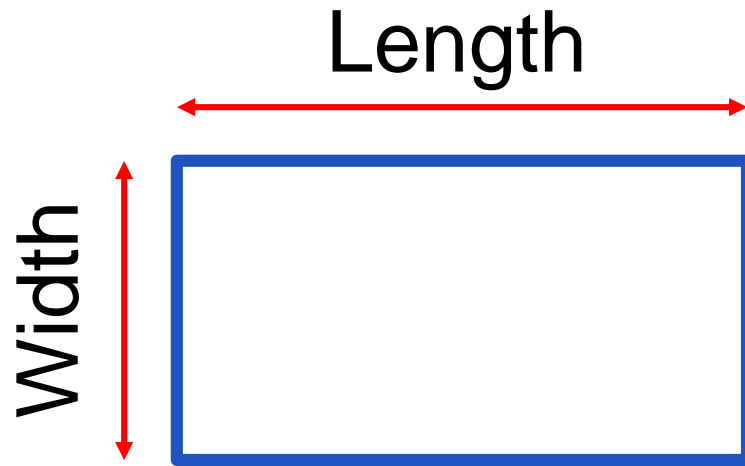
Distance is one dimension (i.e. ft, meters)

Areas are two dimensions (i.e.  $\text{ft}^2$ , SY, acres )

Volumes are three dimensions (i.e.  $\text{ft}^3$ , CM)

Other Volumes: Gallons, Liters, acre-ft

# Area – Squares / Rectangles

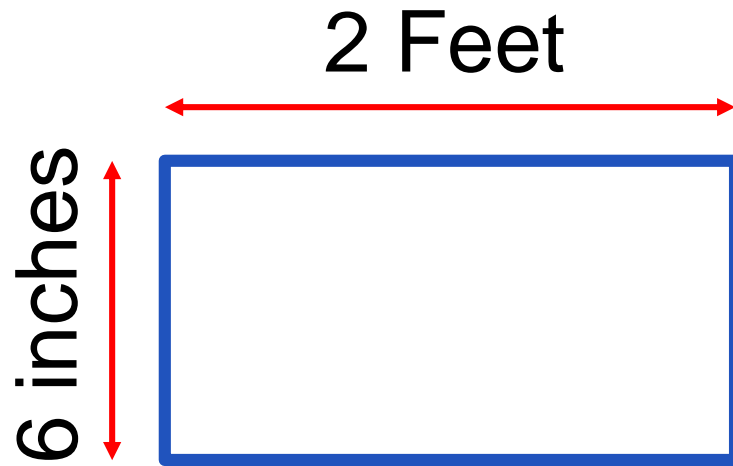


$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = \text{dimension}^1 * \text{dimension}^1$$

*Note 1 – Dimensions need to be the same units of measure*

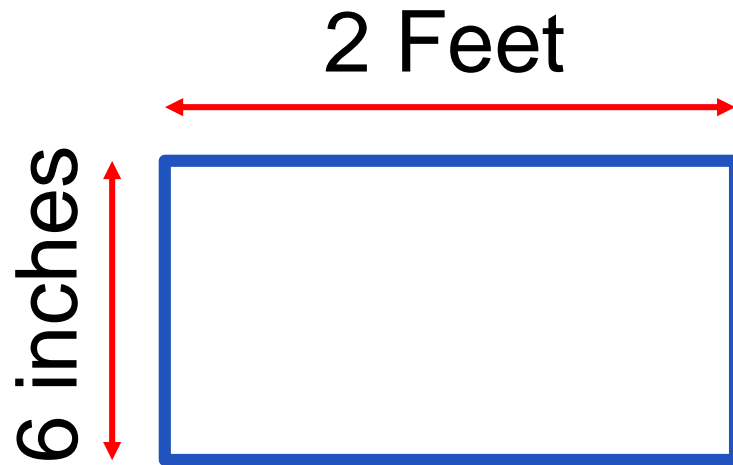
# Area



What is the area?

$$\text{Area} = \text{length} * \text{width}$$
$$\text{Area} = \text{dimension} * \text{dimension}$$

# Area



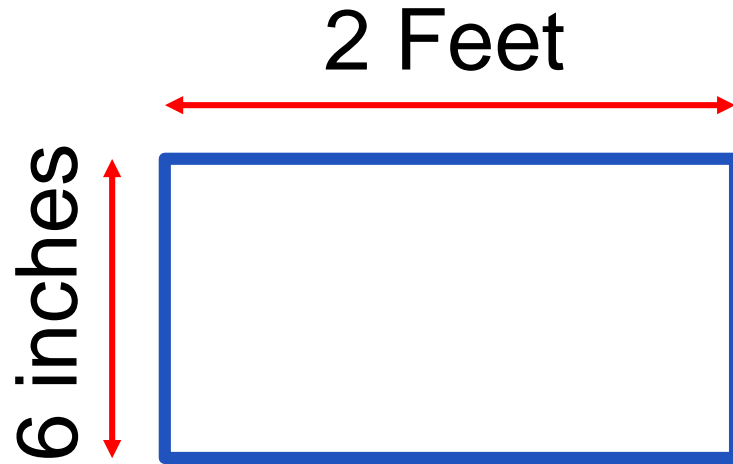
What is the area?

*First get all the dimensions in the same units*

$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = 2 \text{ feet} * \frac{6 \text{ inches} * 1 \text{ foot}}{12 \text{ inches}}$$

# Area



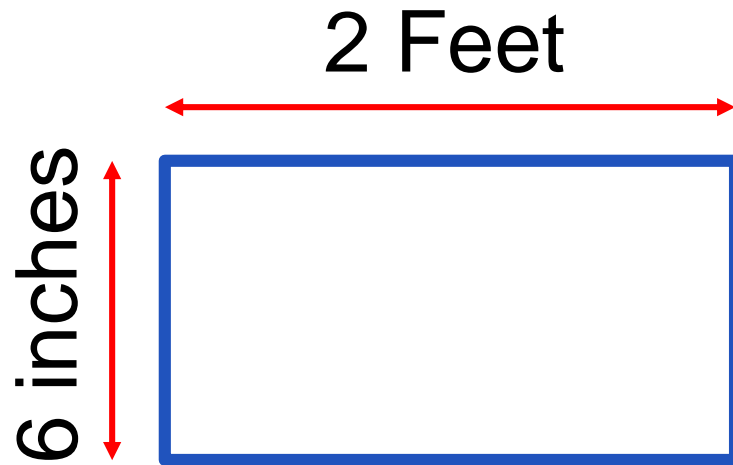
What is the area?

$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = 2 \text{ feet} * \frac{\cancel{6 \text{ inches}} * 1 \text{ foot}}{\cancel{12 \text{ inches}}}$$

$$\text{Area} = 1 \text{ sq ft}$$

# Area



What is the area?

*What if we need the area in square inches?*

$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = 2 \text{ feet} * \frac{12 \text{ inches}}{1 \text{ foot}} * 6 \text{ inches}$$

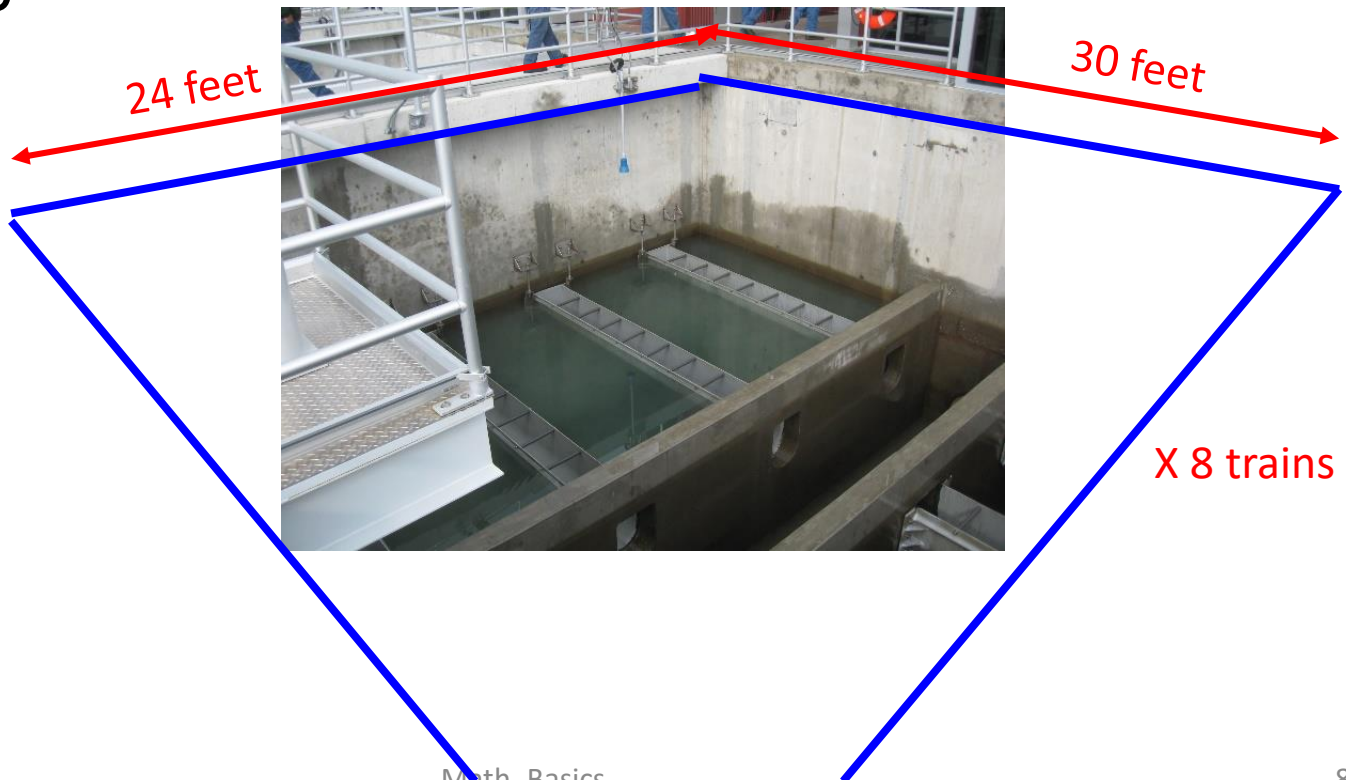
$$\text{Area} = 144 \text{ sq in}$$



# Practical Application



You are going to cover your sand filters and the sales rep wants to know the area so he can get you a price. There are 8 trains, each 24 feet wide. The trains are 30 feet long.



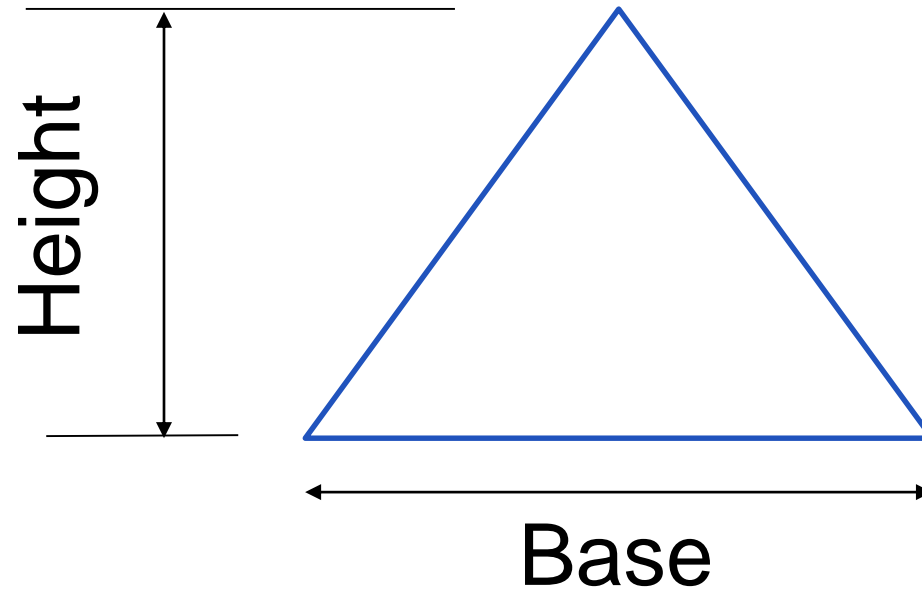
# Practical Application - Area

You are going to cover your sand filters and the sales rep wants to know the area so he can get you a price. There are eight trains, each 24 feet wide. The trains are 30 feet long.

$$\text{Area} = 8 \text{ basins} * 24 \text{ ft} * 30 \text{ ft}$$

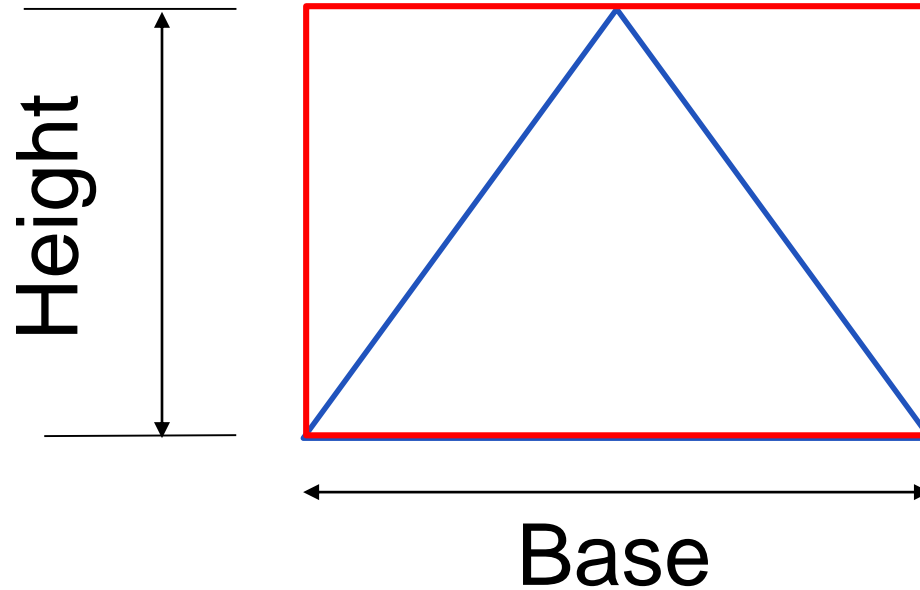
$$\text{Area} = \mathbf{5,760 \text{ sq ft}}$$

# Area - Triangles



$$\text{Area} = (1/2) * \text{base} * \text{height}$$

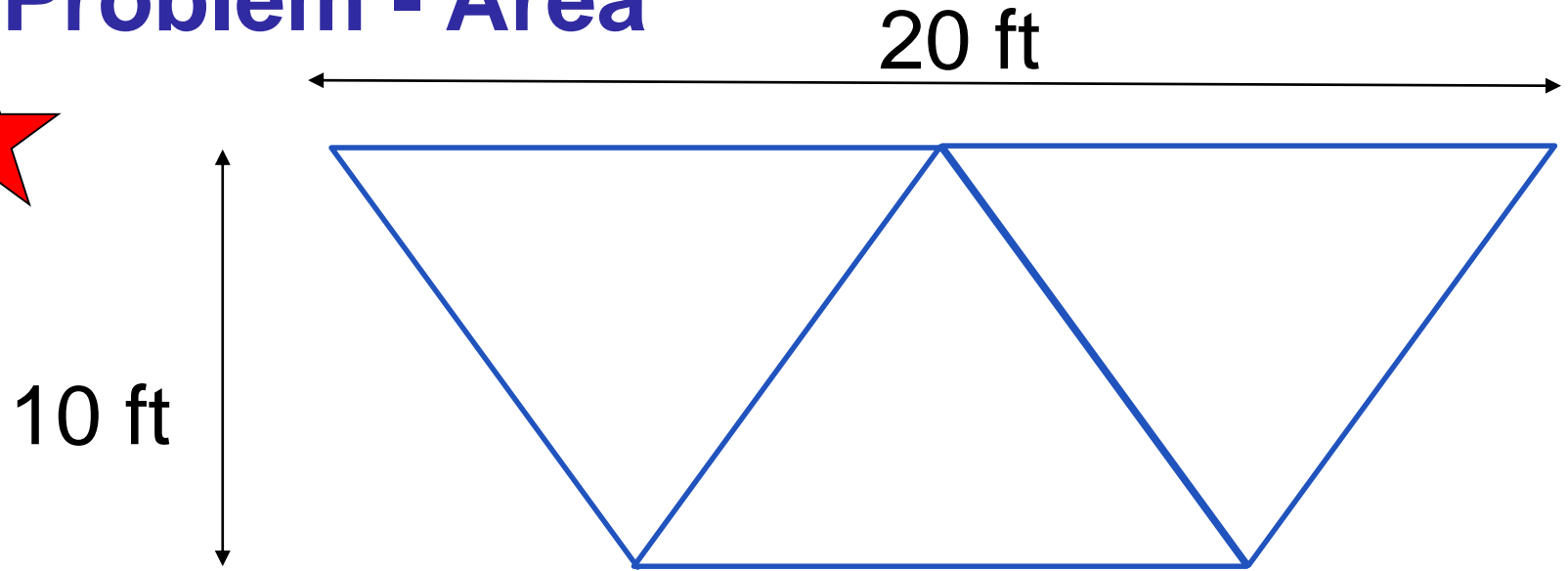
# Area



$$\text{Area} = (1/2) * \text{base} * \text{height}$$

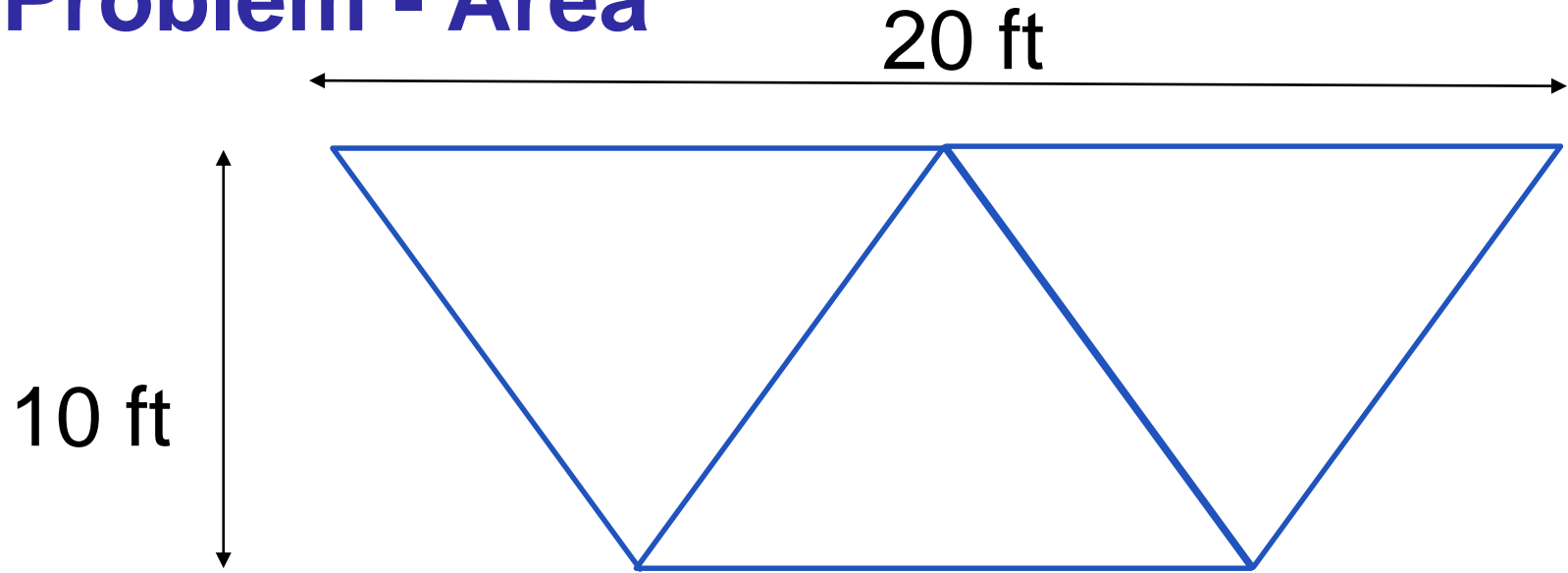
Triangle is  $\frac{1}{2}$  of rectangle!

# Problem - Area



You are covering a truss with a banner for City Celebration. They want to cover the truss. How big?

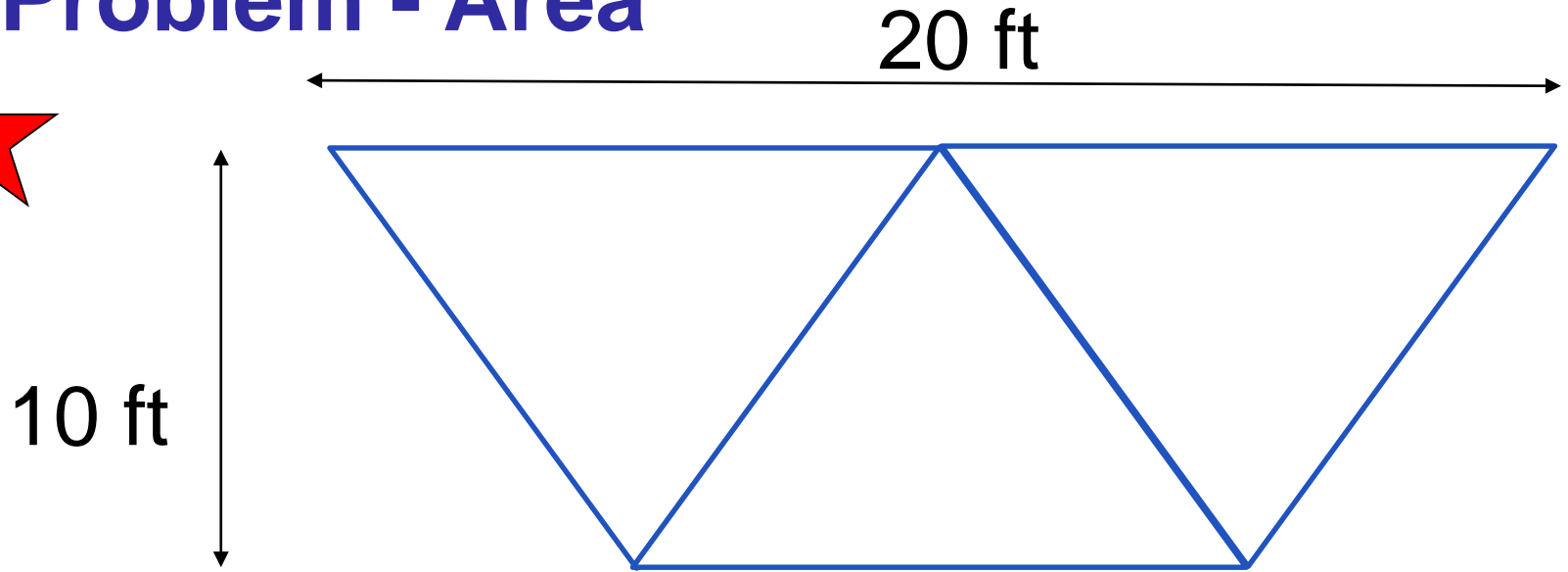
# Problem - Area



You are covering a truss with a banner for City Celebration. They want to cover the truss. How big will the banner be?

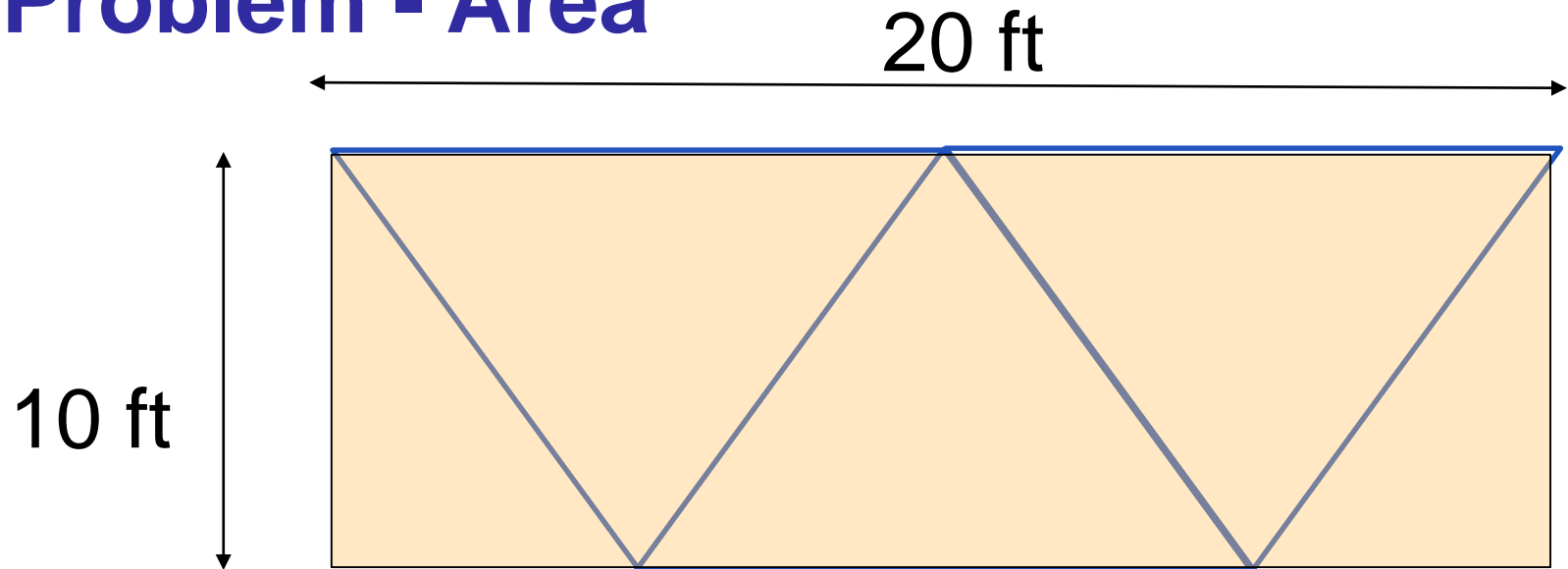
$$\begin{aligned} \text{Area} &= 3 \text{ triangles} \\ &= 3 * \frac{1}{2} * 10 \text{ ft} * 10 \text{ ft} \\ &= 150 \text{ sq ft} \end{aligned}$$

# Problem - Area



Opps! Change of plan, the City Manager now wants a rectangular banner – how big will it be?

## Problem - Area



The City Manager wants  
rectangular banner – how big?

$$\text{Area} = 20 \text{ ft} * 10 \text{ ft} = 200 \text{ sq ft}$$



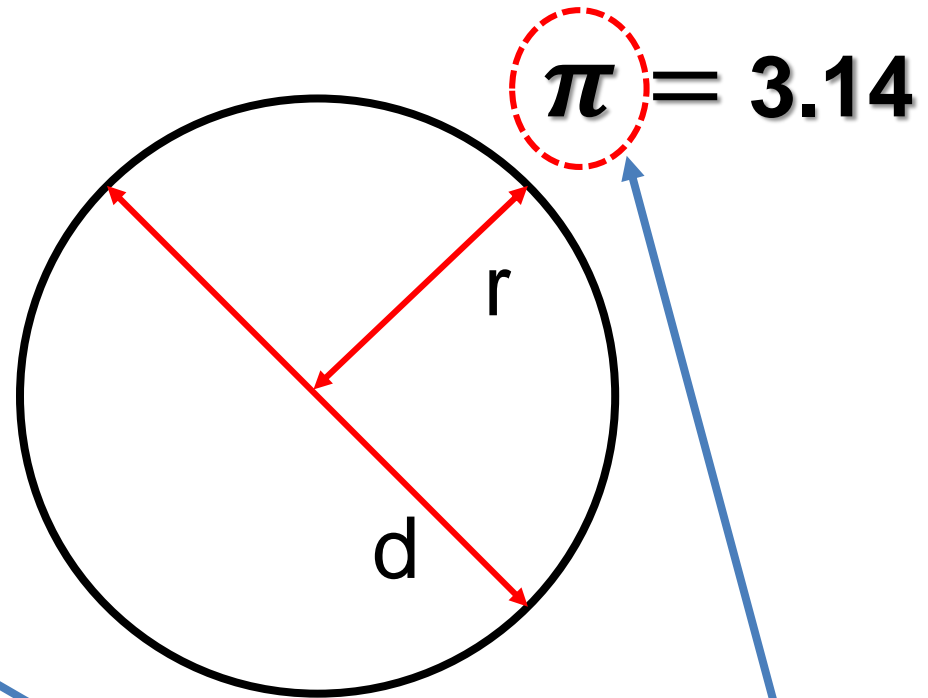
# Area - Circles

Area of a circle

$$A = \pi r^2$$

$$A = \pi (d^2 / 4)$$

$$A = 0.785 * d^2$$

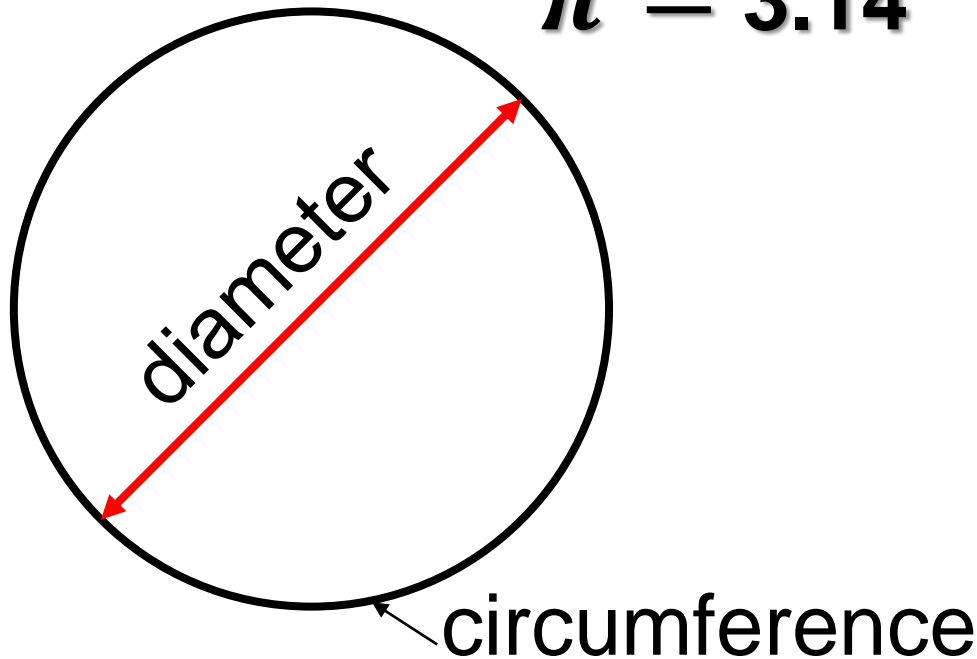


What is this symbol? It's all Greek to me!

# The Magical World of Pi

Pi is a name given to the ratio of the circumference of a circle to the diameter.

$$\pi = 3.14$$



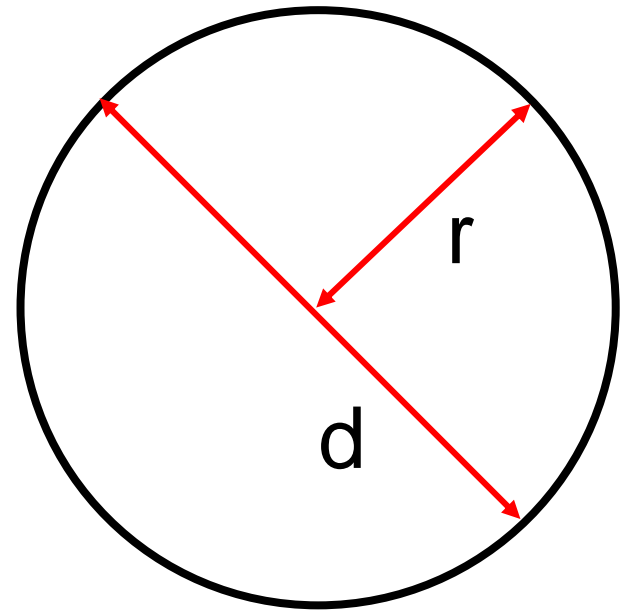
$\pi$   
3.14159  
265358979323  
84626433832795  
02884197169399375  
1058209749445923078  
164062862089986280  
3482534211706798214808  
651328230664709384460955058223  
17253594081284811174502841027019385211055  
59644622948954930381964428810975665933446128475648233786  
7831652712019091456485669234603486104543266482133936072602491412737245  
8700660631558817488152092096282925409171536436789259036001133053054882046652138414695194  
1511609433057270365759591953092186117381932611793105118548074462379962749567351885752748912279381  
8301194912983367336244065664308602139494639522473719070217986094370277053921717629317675238467481846766  
94051320005681271452635608277857713427577896091736371787214684409012249534301465495853710507922796892589235420  
199561121290219608640344181598136297747130996051870721134999998372978049951059731732816096318595024459455469083026  
425223082534468503526193118817101000313783875286587533208381420617177669147303598253490428755468731159562863882357875937519  
578185778053217122680661300192787661119500921642019893809525272010654858632788659361533818279682303019520353018529689957762259941389124  
9721752834791315155748572426413069595829531168617278558807309838175463746493919255064009277016711390984882401283856160365707660114710181942955596198046  
76737349442557971728477040735464208666825969491293136770289152104752162059690240780815019351253324003558746327496473209141892728042092276827347801800934

# The Magical World of Pi

$$\text{Circumference} = 2 * \pi * r$$

$$\text{Diameter} = 2 * r$$

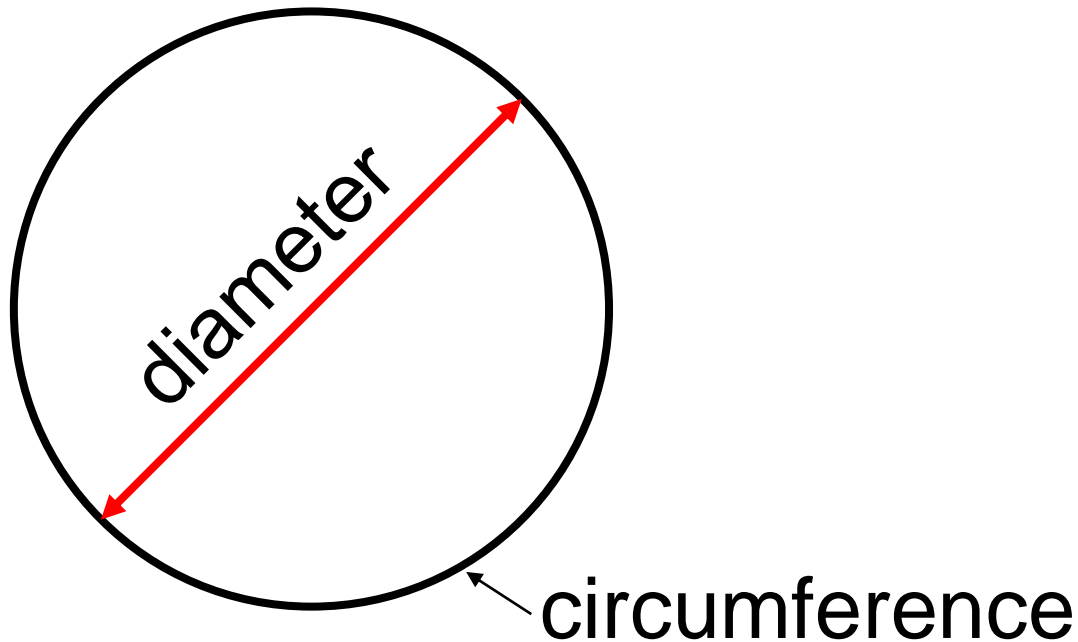
$$\frac{2 * \pi * r}{2 * r} = \pi$$



# Practical Use of Pi ( $\pi$ )

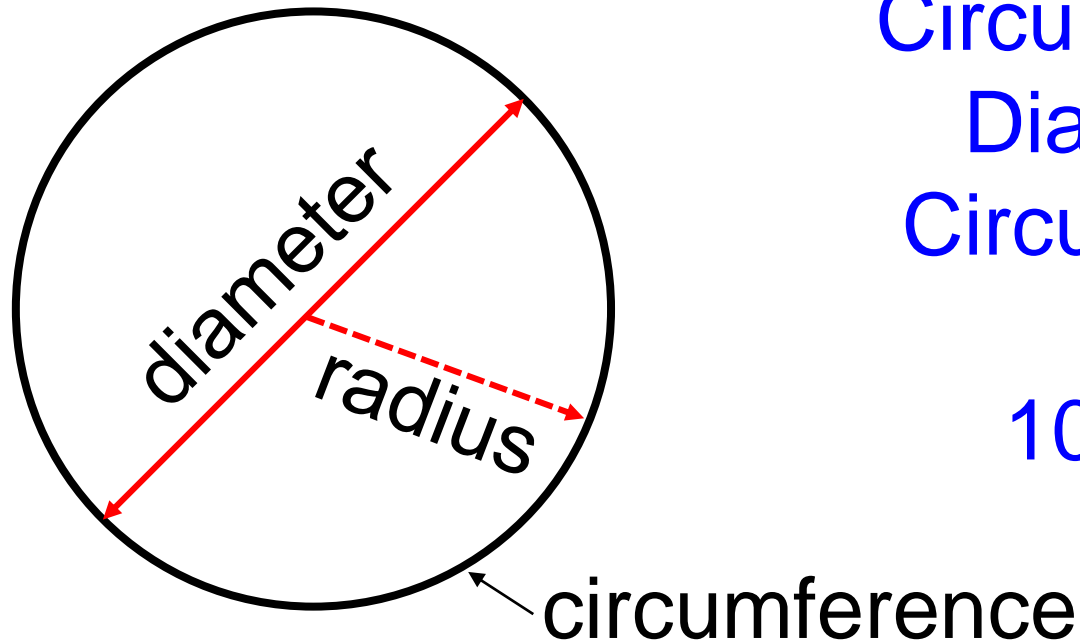


The diameter of the circular clarifier is 100 feet.  
What is the weir length (the circumference)?



# Practical Use of Pi ( $\pi$ )

The diameter of the circular clarifier is 100 feet.  
What is the weir length?



$$\text{Circumference} = 2 \pi r$$

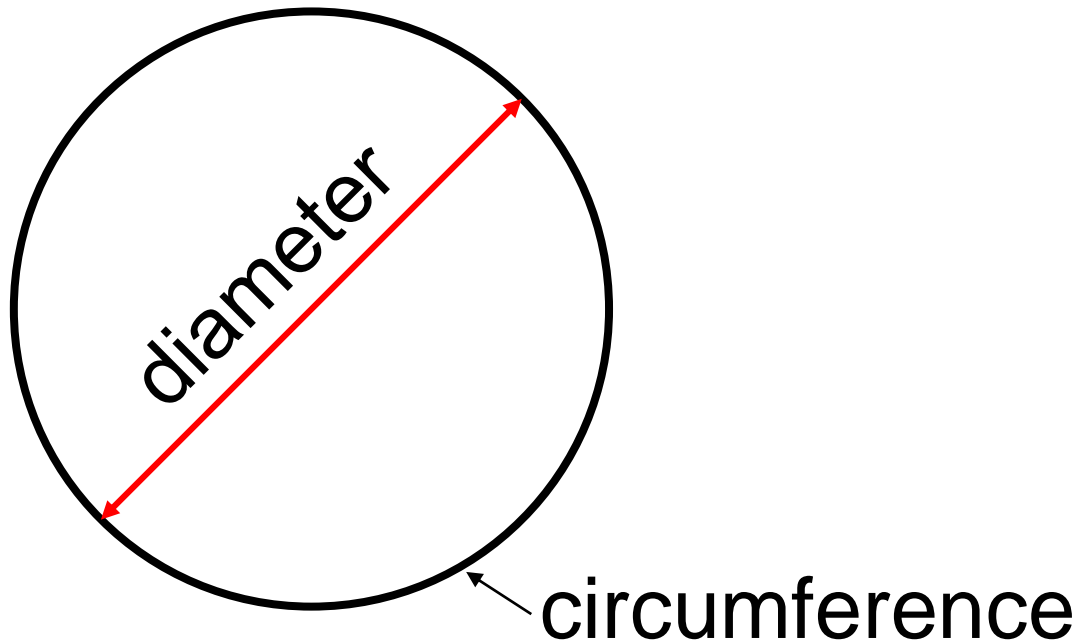
$$\text{Diameter (d)} = 2 r$$

$$\text{Circumference} = \pi d$$

$$100 \text{ feet} * \pi = \\ = 314 \text{ feet}$$

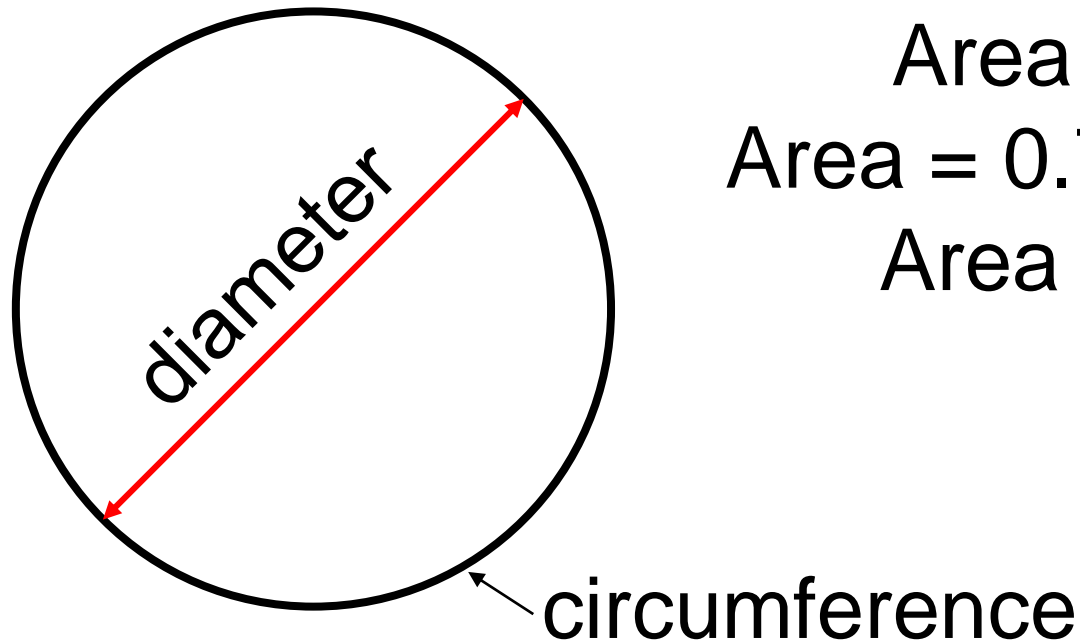
# Practical Use of Pi ( $\pi$ ) – Back to Area

The diameter of the circular clarifier is 100 feet.  
What is the surface area?



# Practical Use of Pi ( $\pi$ )

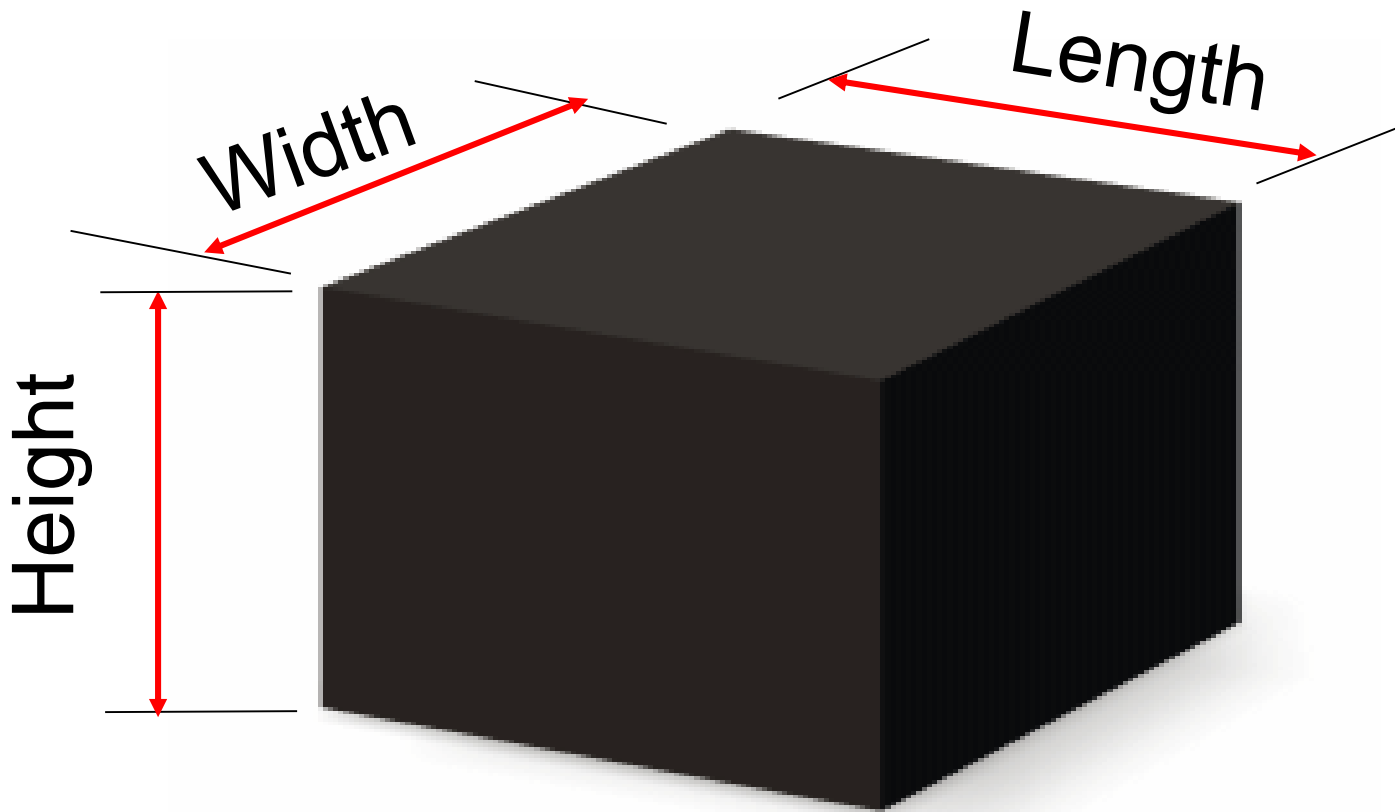
The diameter of the circular clarifier is 100 feet.  
What is the surface area?



$$\begin{aligned} \text{Area} &= 0.785 * d^2 \\ \text{Area} &= 0.785 * (100 \text{ feet})^2 \\ \text{Area} &= 7,850 \text{ sq ft} \end{aligned}$$

# Volume

$$\text{Volume} = \text{length} * \text{width} * \text{height}$$





# Volumes – Practical Question

What is the volume of water in a the basin with following characteristics? Answer in gallons.

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 3 feet

Desired answer needs to be gallons (volume). Basin dimensions are in feet (length)

**Depth of water = 20 feet – 3 feet**

Volume = length \* width \* depth

Volume = 200 ft \* 50 ft \* 17 feet

Volume = 170,000 cu ft

# Volumes – Practical Question

What is the volume of water in a the basin with following characteristics? Answer in gallons.

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 3 feet

**Change cubic feet to gallons – keep the units straight!**

$$\text{Volume} = \frac{170,000 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$

# Volumes – Practical Question

What is the volume of water in a the basin with following characteristics? Answer in gallons.

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 3 feet

**Change cubic feet to gallons – keep the units straight!**

$$\text{Volume} = \frac{170,000 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$

$$\text{Volume} = 1,271,600 \text{ gallons or } 1.27 \times 10^6$$

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet } - 1 \text{ meter }$$

Mixed units! Get all dimensions  
in one measurement unit

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - \underset{\text{Change meters to feet}}{1 \text{ meter}} * \frac{3.28 \text{ feet}}{1 \text{ meter}}$$

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - \frac{1 \text{ meter} * 3.28 \text{ feet}}{1 \text{ meter}}$$

## Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - 3.28 \text{ feet}$$

$$= 16.72 \text{ feet}$$

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

With all measurements in feet, now calculate the volume in cubic feet

$$\begin{aligned}\text{Vol} &= 50 \text{ ft} * 200 \text{ ft} * 16.72 \text{ ft} \\ &= 167,200 \text{ ft}^3\end{aligned}$$



# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

Now change cubic feet to gallons

$$\text{Vol} = 167,200 \text{ ft}^3$$

$$167,200 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

Now change gallons  
to million gallons

Vol = 1,250,656 gallons

$$\text{Vol} = \frac{1,250,656 \text{ gallons} * 1 \text{ MG}}{1,000,000 \text{ gal}}$$

# Volumes – Practical Question

What is the volume of the water in the basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

Vol = 1,250,656 gallons      Round off the answer

$$\text{Vol} = \frac{1,250,656 \text{ gallons}}{1,000,000 \text{ gallons}} * 1 \text{ MG} = \underline{\underline{1.25 \text{ MG}}}$$

# Volume –Tank Example (Cylinder)

Volume = Area x Height

$$\pi = \text{pi} = 3.14$$

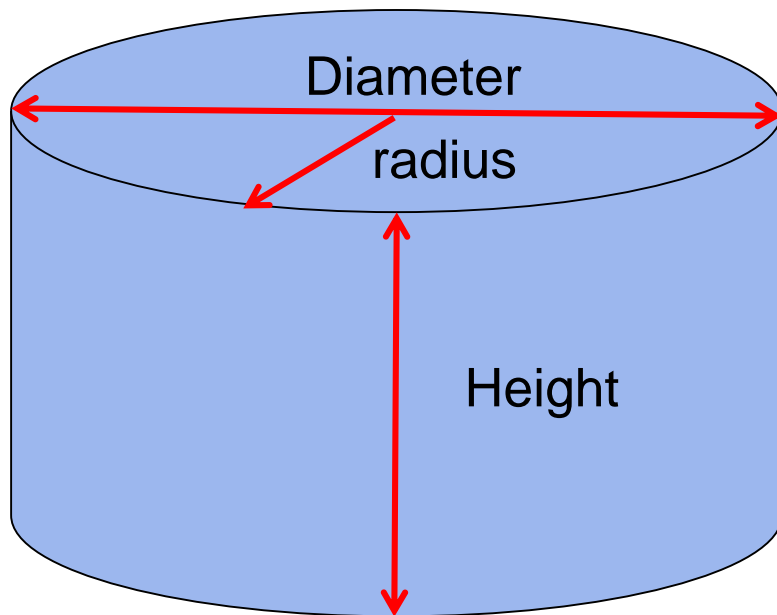
r = radius

D = Dia. = Diameter

$$2 * r = \text{Dia.}$$

$$\begin{aligned} \text{Vol} &= 3.14 * r^2 * \text{height} \\ &= .785 * d^2 * \text{height} \end{aligned}$$

Tank



# Volume –Tank Example



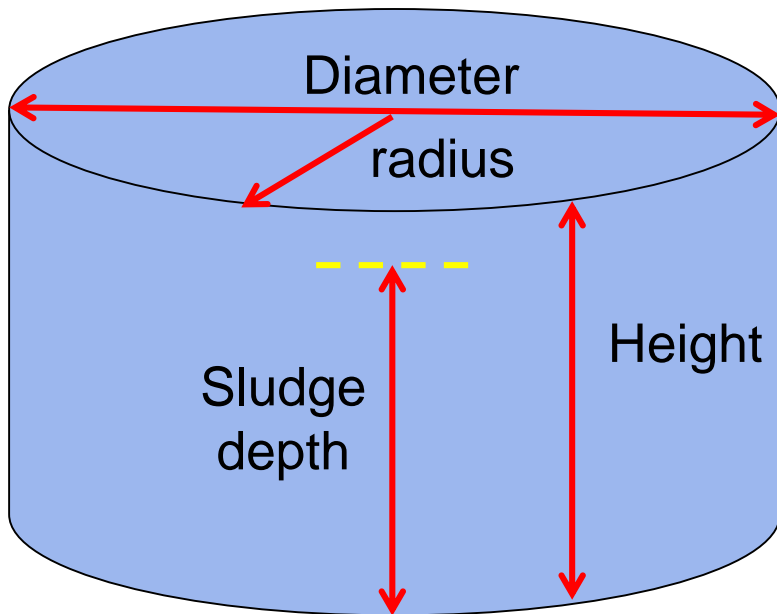
What is volume of sludge holding tank in gallons?

Diameter = 100 feet

Height = 24 feet

Sludge depth = 20 feet

Tank



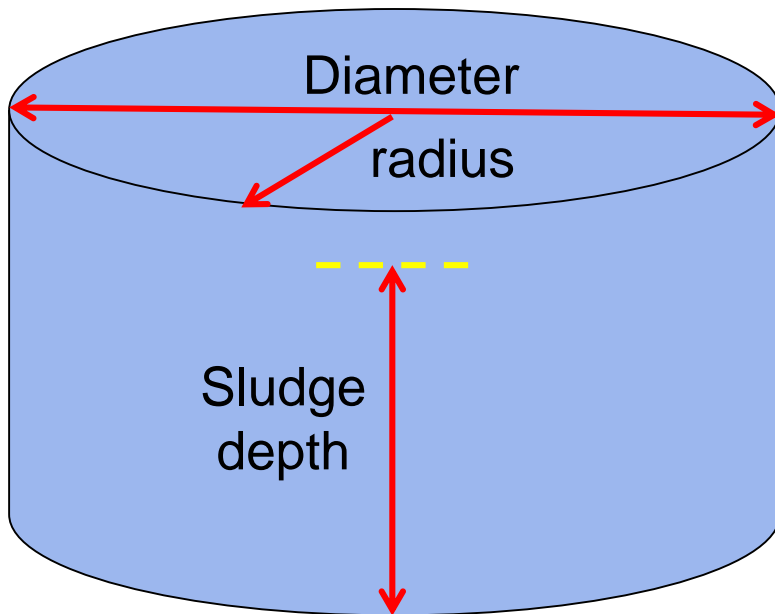
# Volume –Tank Example

What is volume of sludge holding tank in gallons?

Diameter = 100 feet

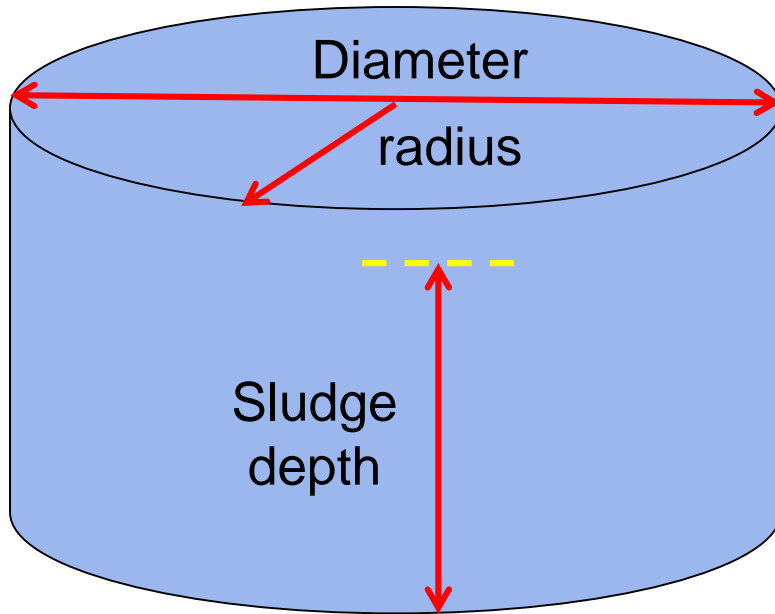
Height = 100 feet

Tank



$$\begin{aligned} \text{Vol} &= 0.785 * d^2 * \text{height} \\ &= 0.785 * (100 \text{ ft})^2 * 20 \text{ ft} \\ &= 157,000 \text{ ft}^3 \end{aligned}$$

# Volume –Tank Example



What is volume of sludge holding tank in gallons?

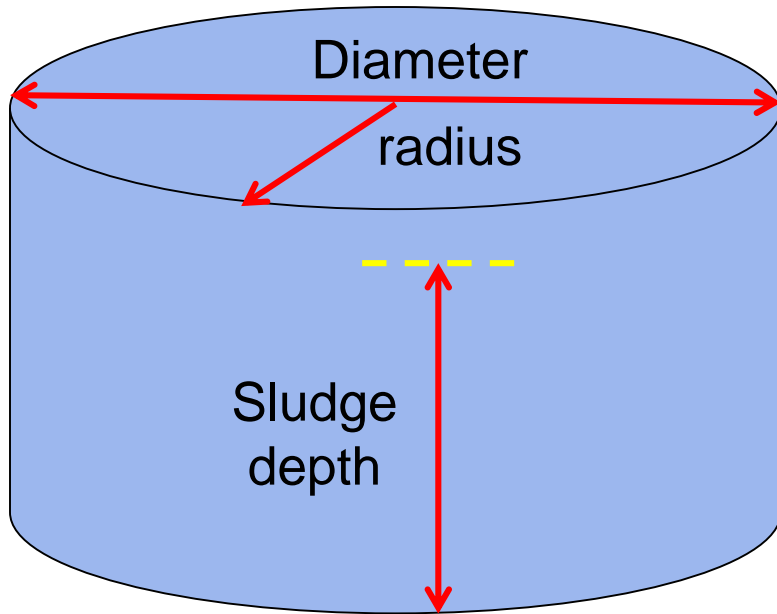
Diameter = 100 ft

Sludge depth = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3$$

$$157,000 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Volume –Tank Example



What is volume of sludge holding tank in gallons?

Diameter = 100 ft

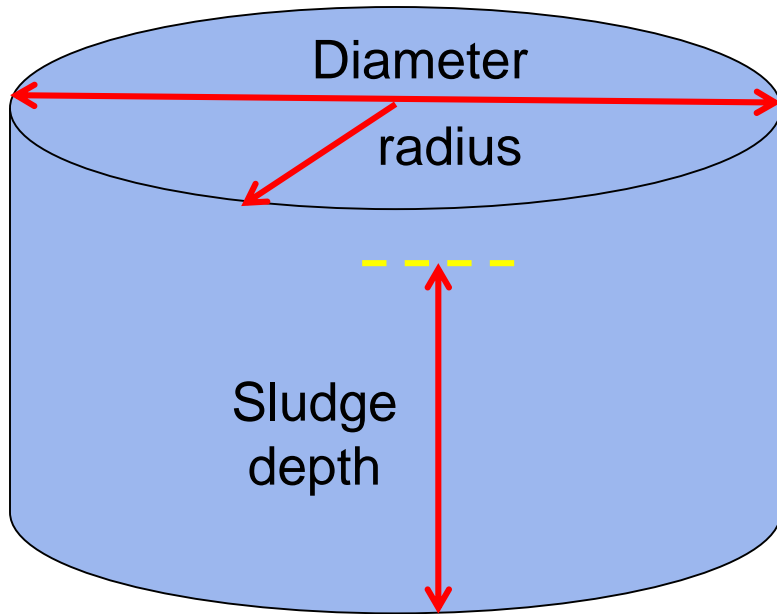
Sludge depth = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3$$

$$157,000 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$



# Volume –Tank Example



What is volume of sludge holding tank in gallons?

Diameter = 100 ft

Height = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3 * 7.48$$

1,174,360 gallons

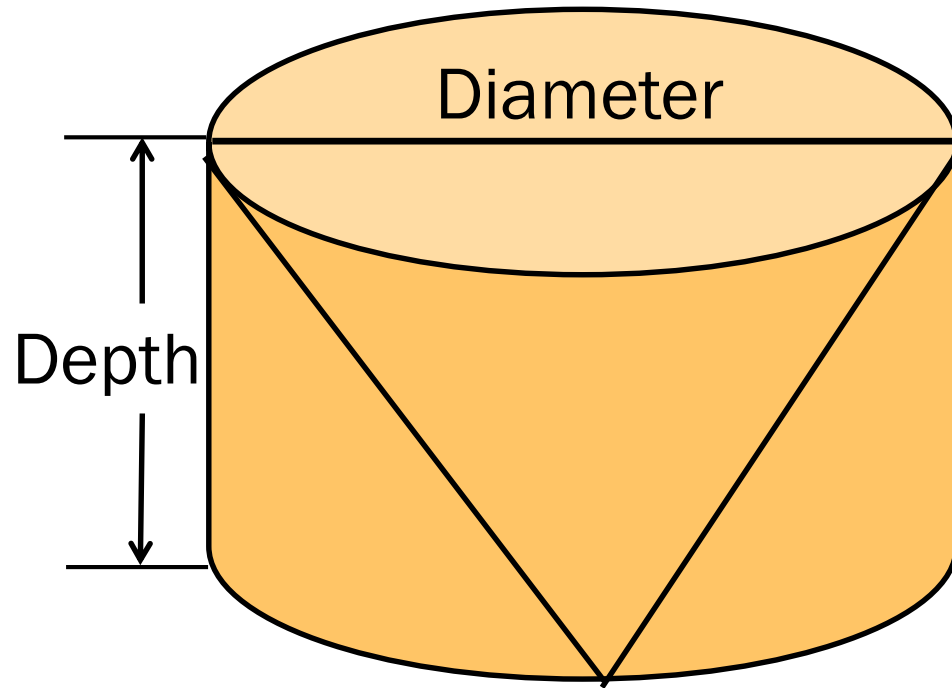
*or*

1.17 MG

Divide by 1,000,000  
and round off

# Volume of a Cone

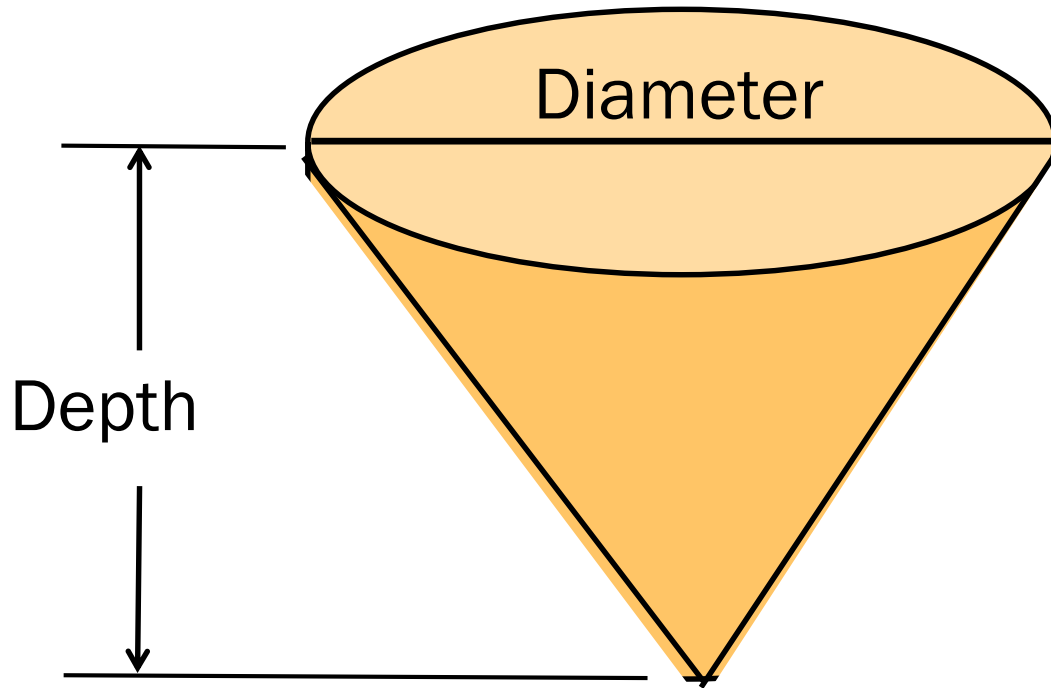
$\frac{1}{3}$  the volume of a cylinder.



# Practical Application



What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?



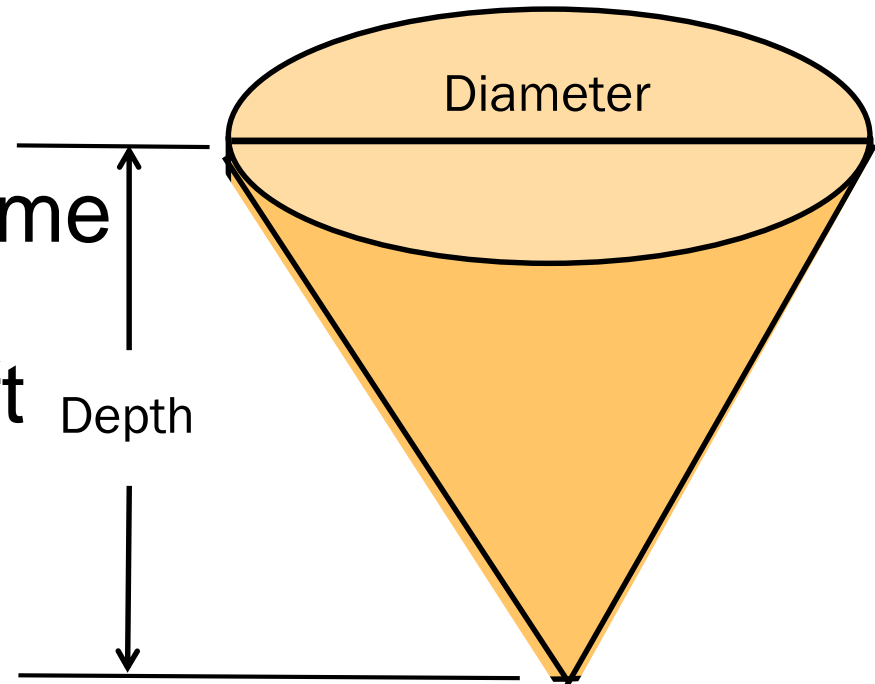
# Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder =  $0.785 * (5\text{ft})^2 * 10\text{ft}$

Cylinder = 196 cu ft



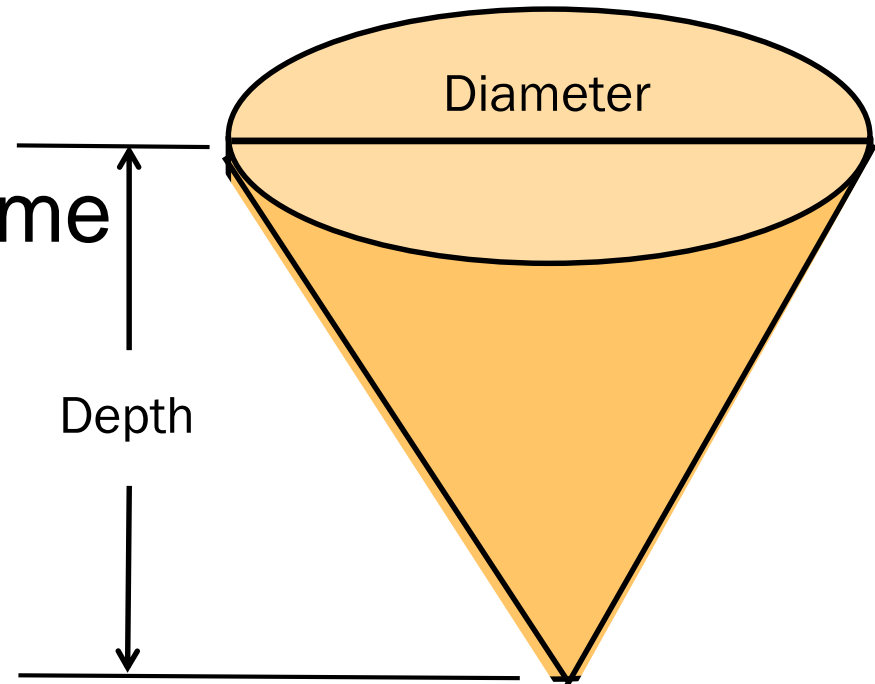
# Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder = 196 cu ft

$$\frac{196 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$



# Practical Application

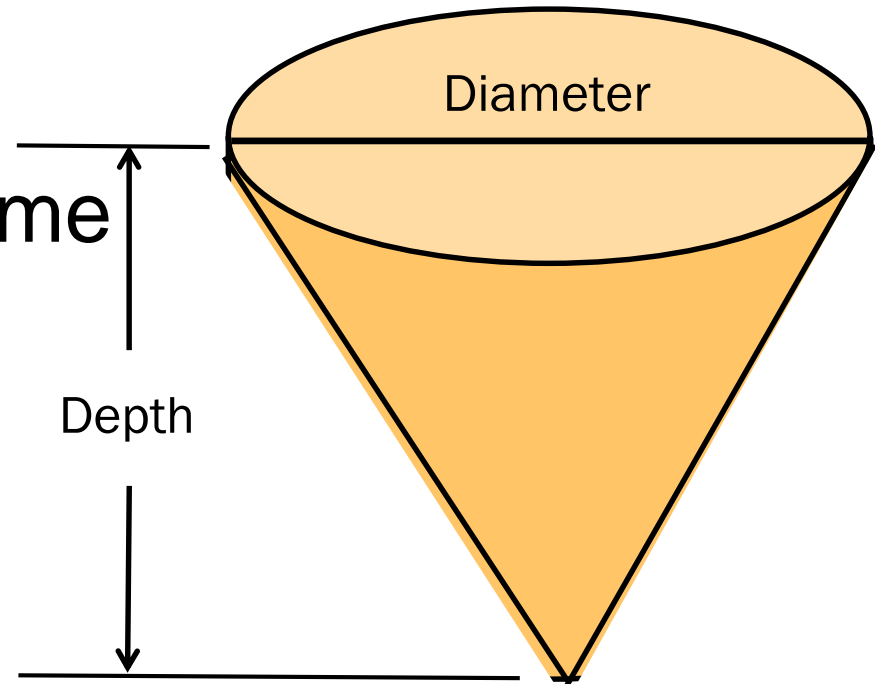
What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

Cone =  $\frac{1}{3}$  \* Cylinder Volume

Tank = 196 cu ft

$$\frac{196 \cancel{\text{ cu ft}} * 7.48 \text{ gallons}}{1 \cancel{\text{ cu ft}}}$$

Cylinder = 1,466 gallons



# Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

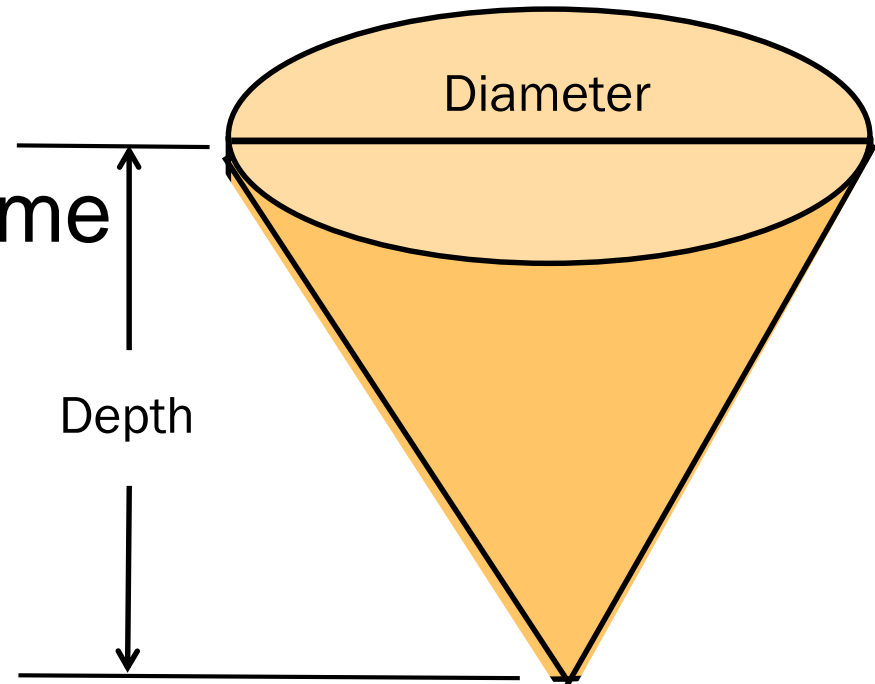
Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder = 196 cu ft

Cylinder = 1466 gallons

Cone =  $\frac{1}{3}$  \* 1466 gal

Cone = 489 gal



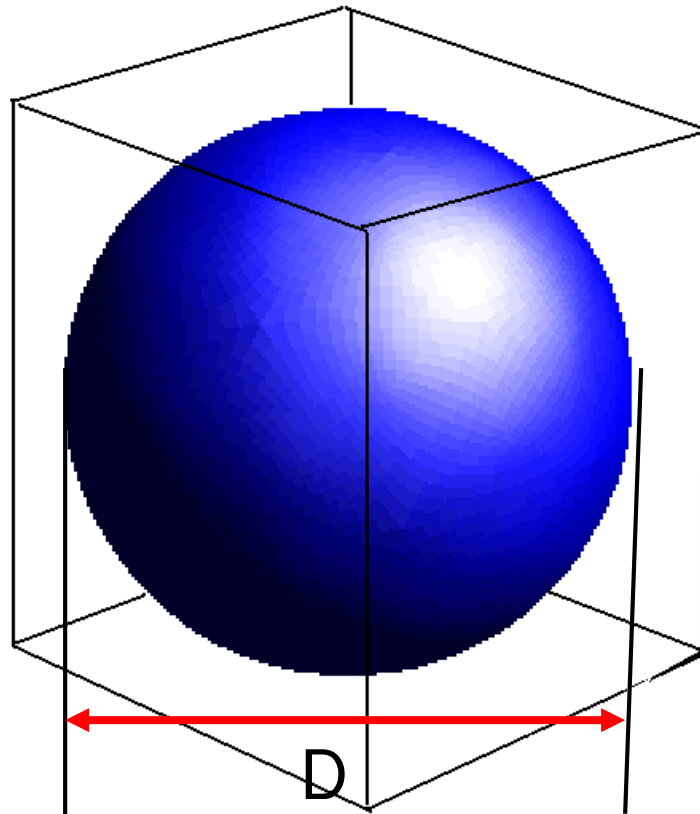
# Practical Application – What About Rounding?

- Tank 1,174,360 gallons or 1.17 MG
  - 1.2 MG “nominal”
- Cone 489 gallons
  - 500 “nominal” gallons
- It all depends on the use



# Volume of a Sphere

3/4 the volume of a cube with the same dimensions



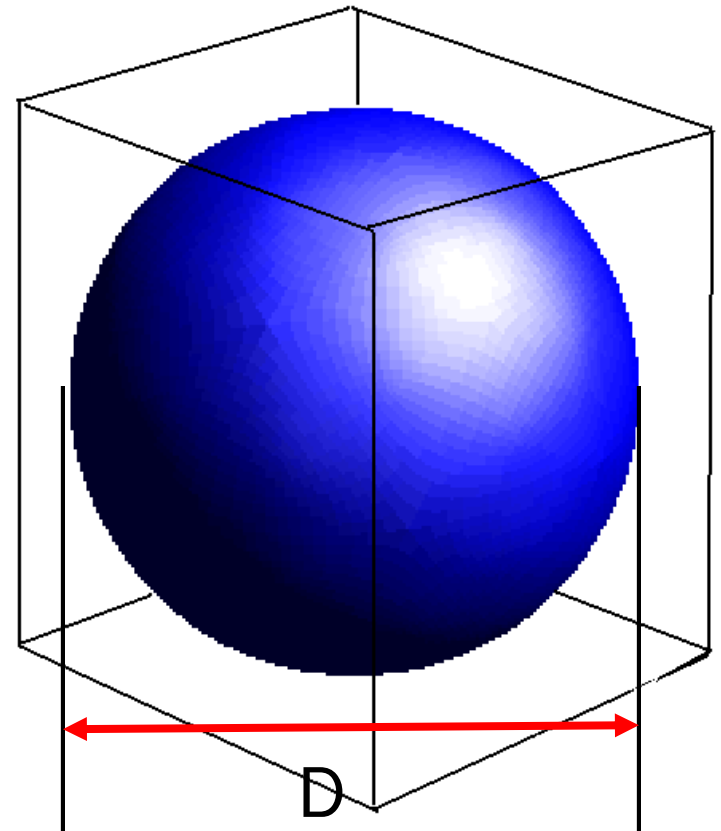
# Practical Application – Sphere Volume

What is the volume of the gas holding sphere if the diameter is 50 feet?

Sphere volume =  
 $\frac{3}{4}$  \* cube volume

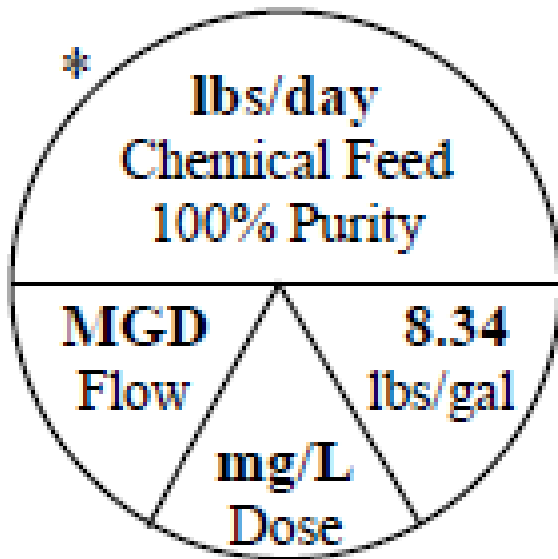
$$\begin{aligned}\text{Volume} &= \\ \frac{3}{4} * 50 \text{ ft} * 50 \text{ ft} * 50 \text{ ft} \\ &= 0.75 * 50^3 \text{ ft}\end{aligned}$$

Volume = 93,750 cubic feet



# Calculation Wheels – Refer to ABC Handout

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



*Can also be used without rate or flow*  
Feed in pounds, Volume in MG

# Time Out - Percentages

If something is 56%, what is the mathematical (decimal) way to show that number?

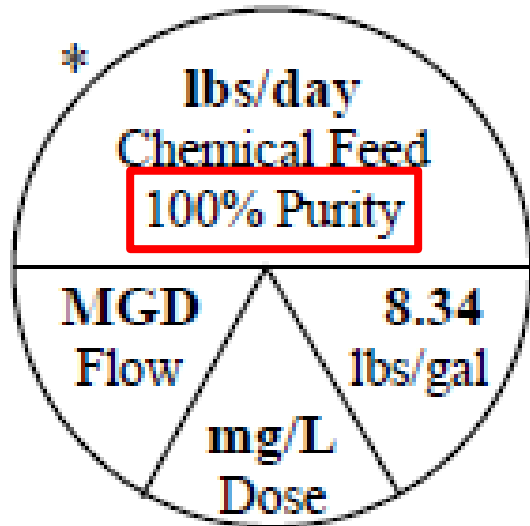
$$56\% = ?$$

# Time Out - Percentages

If something is 56%, what is mathematical (decimal) way to show number?

$$56\% = \frac{56}{100} = 0.56$$

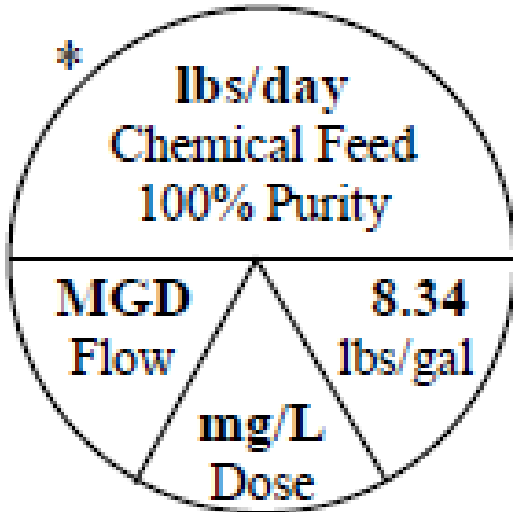
# Back to the Calculation Wheels



$$\text{Feed lbs/day} = \frac{\text{Flow MGD} * \text{Dose mg/l} * 8.34 \text{ lbs/gal}}{\text{Purity decimal percentage}}$$

*This is where that algebra stuff comes into play*

# Back to the Calculation Wheels



What if you know feed, but not flow?

Feed lbs/day

Flow MGD \* Dose mg/l \* 8.34 lbs/gal

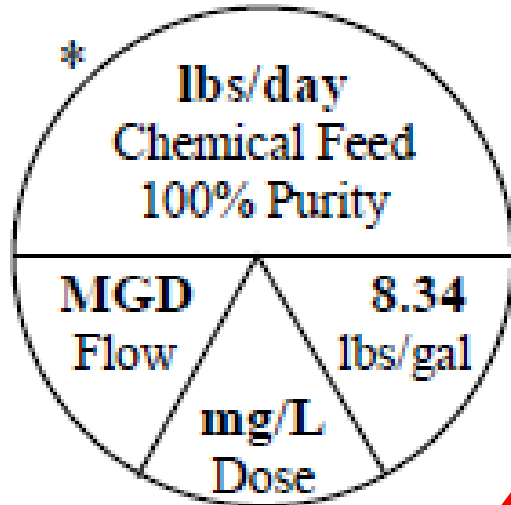
=

Dose mg/l \* 8.34 lbs/gal

Dose mg/l \* 8.34 lbs/gal

Rearrange the equation to isolate flow on one side

# Back to the Calculation Wheels



Division Line

Feed lbs/day

Flow MGD \* ~~Dose mg/l~~ \* ~~8.34 lbs/gal~~

Dose mg/l \* 8.34 lbs/gal

~~Dose mg/l~~ \* ~~8.34 lbs/gal~~

Make sure the units are correct



# Questions, Comments and Suggestions?



American Water Works Association  
**Pacific Northwest** Section

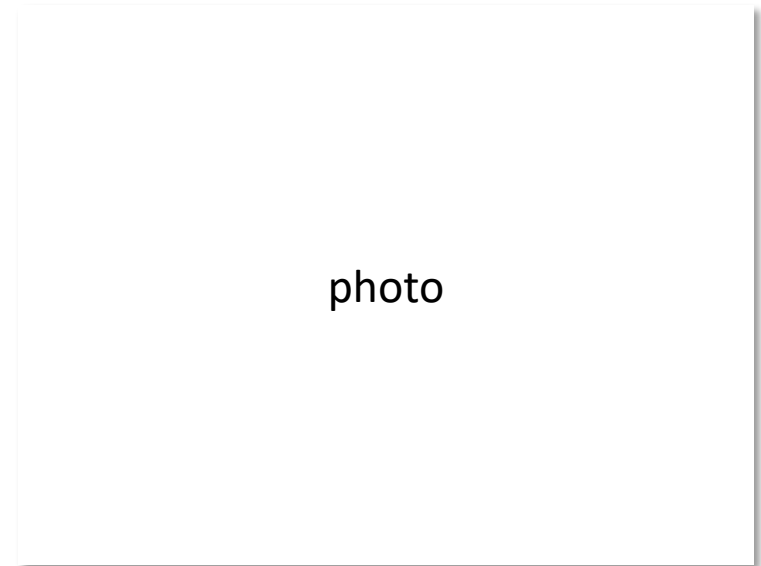
*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Section title

*subtitle*

# Header

- Tier 1 info
  - Tier 2 info
    - Tier 3 info



*Photo caption*

*Optional text here*

# Header

- Tier 1 info
  - Tier 2 info
    - Tier 3 info

*Photo caption*

# Header

## Case A

- info

## Case B

- info

# Header

	Col 1	Col 2	Col 3	Col 4
This	X	X	X	X
That	X	X	X	X
The	X	X	X	X
Other	X	X	X	X
Thing	X	X	X	X