

# *Joint Workshop*

## **Math for Operators - *Morning***

***A Necessary Skill for Water & Wastewater Operators***

## **Reading Process & Instrumentation**

***Diagrams - Afternoon***

***Following the lines of monitoring and control***



American Water Works Association  
**Pacific Northwest** Section



# ***Math for Operators:***

## **Content & Goals**

To review basic math skills and to practice those skills on practical problems

# Acknowledgements:

**Author**

**Doug Berschauer | Parametrix**

**Editor**

**Jeff Lundt | KCWTD**

**Today's Presenters:**

**Dave Price – Carollo**

**John Roth – Clark PUD**

**Jeff Lundt - KCWTD**

Content & Goals:

- To enhance and reinforce the math skills for operators

# Outline:

## Workshop topics

**Math Basics**

**Aids to Navigation**

**Units of Measure**

**Algebra**

**Trigonometry**

**Conversion Factors**

**Practical Applications**

**Examples – 2<sup>nd</sup> hour**

**Problem Solving Practice – 3<sup>rd</sup> hour**

# Safety

*The cornerstone of everything we do*

# Safety – Mission Critical

There are many hazards associated with water operations. Some examples include;

- Confined spaces
- Trenching & excavation
- Electrical
- Vehicles & equipment
- Chemicals
- Ergonomic

“If you’re not doing the job safely,  
you are not doing it right.”



*Photo from Tualatin Valley  
Water District*

# Protecting Yourself and Others

## Rules to live by:

1. **You** are responsible for your safety and the safety of others
2. Follow the rules
3. If you're not trained for it; Don't do it
4. Work smarter, not harder
5. Don't take short cuts
6. Practice good housekeeping
7. Be Prepared
8. Be a safety advocate



*Photo from Tualatin Valley  
Water District*

**“It’s better to take a minute to save your life than to lose your life in a minute.”**

# Personal Protection Equipment - PPE

Includes but is not limited to:

- Safety Glasses/Shield
- Hard Hat
- Hearing Protection
- Visible Safety Shirt/Jacket
- Protective Toe Footwear
- Gloves
- Gas Monitors
- Harness
- Radio/Flashlight
- *Mask*
- *Hand sanitizer*



*Graphic from Whitney  
Equipment Company, Inc.*



# 811 – Call Before You Dig – *it's the law*

## Utility Notification Center

- Each state operates its own 811 center
  - ID – 811 or 1-800-342-1585 (Boise) & 1-866-729-5140 (CdA)
  - OR – 811 or 1-800-332-2344
  - WA – 811 or 1-800-424-5555
  - Or on-line
- Open 24/7
- May be regional within a state
- 2 days advanced notice is required
- <https://youtu.be/ZH7cXJ2PpdY>



**Know what's below.  
Call before you dig.**

*Graphic from Tualatin Valley  
Water District*

# PNWS Training-in-a-Box (TIAB)

- Workshop curricula prepared by the Section's Training Coordination Committee to increase the quality and consistency of training in PNWS and to increase distribution of that training throughout the Section
- Current programs:
  - Pump Station O&M
  - Basic Waterworks
  - Emergency Preparedness
  - Water Storage Basics
  - Math for Operators / P&IDs
  - Groundwater Basics
- Upcoming programs:
  - Chemistry for Operators
  - Chemical Feed & Storage Systems



American Water Works Association

**Pacific Northwest** Section

Northwest Washington Subsection

# Questions, Comments and Suggestions?



American Water Works Association  
**Pacific Northwest** Section



*Prepared for the Pacific Northwest  
Section - AWWA*

# Math for Operators

*If you can't do the numbers, you can't make the water (or clean the wastewater!)*

Version 1.0 & May 2019



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Math Basics

***You can't run the place without it!***

# Math Basics - Real Basics

$$1 + 1 = 2$$

$$2 * 2 = 4$$

*The numbers by themselves are generally not useful until we attach units to them so we know what we are measuring*

We will assume you have basic math (arithmetic) skills; + - x & /

# Math Basics – Adding Units of Measure

1 foot + 1 inch  $\neq$  2

# Math Basics – When adding and subtracting must be the SAME units

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

~~$$1 \text{ foot} + (1 \text{ inch} * (12 \text{ inches/foot})) =$$~~

$$1 \text{ foot} + (1 \text{ inch} * (1 \text{ foot}/12 \text{ inches})) =$$

*Convert to a common unit of measure, in this case feet*



# Closer Look – Keeping track of UNITS

*For addition need common units*

$$1 \text{ foot} + 1 \text{ inch} * \frac{1 \text{ ft}}{12 \text{ inches}} = 1 \frac{1}{12} \text{ ft or } \frac{13}{12}$$

*Accurate but maybe not useful*

# Unit Basics – It makes a difference what you want to do

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

$$1 \text{ foot} + 1 \text{ inch} * (1 \text{ foot}/12 \text{ inches}) =$$

$$1 \text{ foot} + 1/12 \text{ foot} = 1 - 1/12 \text{ feet}$$

$$1 \text{ foot} + .083 \text{ foot} = 1.083 \text{ feet}$$

*Useful for a surveyor or bulldozer operator, or for measuring liquid depth*

# Unit Basics 2

$$1 \text{ foot} + 1 \text{ inch} \neq 2$$

$$1 \text{ foot} * (12 \text{ inches/foot}) + 1 \text{ inch} =$$
$$12 \text{ inches} + 1 \text{ inch} = 13 \text{ inches}$$

*Useful for a plumber or  
carpenter*



*Our choice of units has  
a lot to do with who  
we are and what we  
need to do with the  
“answer”*

# Math Basics – Short Cuts

## Exponents

Whole number exponents used area and volume formulas

$$2 * 2 = 4$$

$$2^2 = 4$$

You can often do these by hand or in your head.

Fractional exponents used in friction formulas and other equations

$$3^2 = 3 * 3 = 9$$

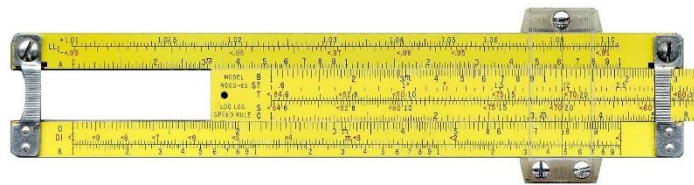
$$30^{1.85} = 540.35$$

For this one you need your calculator, a computer, a slide rule, or log tables.

FOUR-PLACE COMMON LOGARITHMS

N	0				5				6				7				8				9				Proportional Parts																																																																																																																																																																																																							
	1	2	3	4	5	6	7	8	9	0	1	2	3	4	5	6	7	8	9	0	1	2	3	4	5	6	7	8	9	0	1	2	3	4																																																																																																																																																																																														
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Images from International Slide Rule Museum, coolstuff4891.blogspot.com+, & Abelard.com



# Math Basics – Short Cuts

Then how do the units follow?

$$2 * 2 = 2^2 = 4$$

$$\text{ft} * \text{ft} = \text{ft}^2$$

$$3^3 = 3 * 3 * 3 = 27$$

$$\text{ft} * \text{ft} * \text{ft} = \text{ft}^3$$

# Math Basics – 2 & 3 dimensions

$$2 * 2 = 4$$

$$2^2 = 4$$

$$\text{ft} * \text{ft} = \text{ft}^2$$

AREA



$$3^3 = 3 * 3 * 3 = 27$$

$$\text{ft} * \text{ft} * \text{ft} = \text{ft}^3$$

Volume



# Math Basics – Multiplication & Division

$$2 \text{ ft} * 2 \text{ ft} = 4 \text{ Square Feet (ft}^2\text{)}$$

$$\text{ft}^2 = \text{sq ft} = \text{sf}$$

*All abbreviations  
are used*

# Math Basics – Multiplication & Division

2 ft \* 2 inches = 4 foot-inch

Correct  
But not a useable term



# Math Basics – Multiplication & Division

$$2 \text{ acre} * 2 \text{ feet} = 4 \text{ acre-feet}$$

Very correct!  
Is a common term for lake & large  
reservoir volume

*Not all mixed  
units are wrong*

*(So how big is an acre you ask?  
43,560 sf or a square 208.71  
feet on a side)*

# Math Basics – Multiplication & Division

## Calculating areas

*This is a conversion factor. It allows us to convert a measurement in one type of unit to another type of unit.*

$$= 2 \text{ ft} * 2 \text{ inches}$$

$$= 2 \text{ ft} * 2 \text{ inches} * (1 \text{ foot}/12 \text{ inches})$$

$$= 2 \text{ ft} * 2/12 \text{ ft}$$

$$= 4/12 \text{ ft}^2$$

$$= 0.33 \text{ ft}^2 \text{ (or } 1/3 \text{ ft}^2)$$

# Math Basics – Multiplication & Division

*But what if we want sq. in. instead of sq. ft.?*

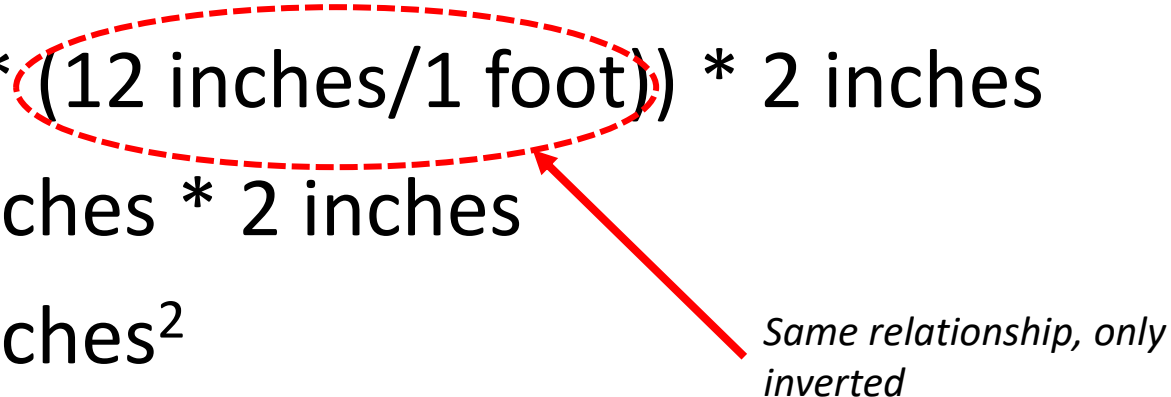
$$= 2 \text{ ft} * 2 \text{ inches}$$

$$= (2 \text{ ft} * (12 \text{ inches}/1 \text{ foot})) * 2 \text{ inches}$$

$$= 24 \text{ inches} * 2 \text{ inches}$$

$$= 48 \text{ inches}^2$$

*Same relationship, only inverted*



# Math Basics – Multiplication & Division

*Calculating flow rates*

$$= \frac{200 \text{ gallons}}{20 \text{ minutes}}$$

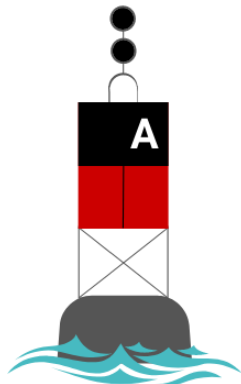
$$= 10 \text{ gallons per minute (gpm)}$$

*gpm is one of many terms  
of flow measurement*

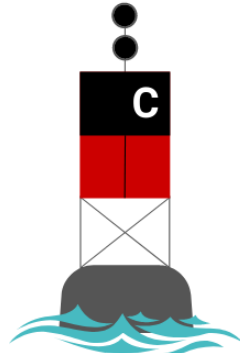
# Aids to Navigation

*Resources that will come in handy*

BR "A"  
Fl (2) 5s



LIGHTED



UNLIGHTED

BR "C"



# Aids to Navigation - Handout

## Formula/Conversion Table

Water Treatment, Distribution, & Water Laboratory Exams

$$\text{Alkalinity, mg/L as CaCO}_3 = \frac{(\text{Titrant Volume, mL})(\text{Acid Normality})}{\text{Sample Volume, mL}}$$

$$\text{Amps} = \frac{\text{Volts}}{\text{Ohms}}$$

$$\text{Area of Circle}^* = (0.785)(\text{Diameter}^2)$$

$$\text{Area of Circle} = (3.14)(\text{Radius}^2)$$

$$\text{Area of Cone (lateral area)} = (3.14)(\text{Radius})\sqrt{\text{Radius}^2 + \text{Height}^2}$$

$$\text{Area of Cone (total surface area)} = (3.14)(\text{Radius})(\text{Radius} + \sqrt{\text{Radius}^2 + \text{Height}^2})$$

$$\text{Area of Cylinder (total exterior surface area)} = [\text{End \#1 SA}] + [\text{End \#2 SA}] + [(3.14)(\text{Diameter})(\text{Height or Depth})]$$

*Where SA = surface area*

$$\text{Area of Rectangle}^* = (\text{Length})(\text{Width})$$

$$\text{Area of Right Triangle}^* = \frac{(\text{Base})(\text{Height})}{2}$$

$$\text{Average (arithmetic mean)} = \frac{\text{Sum of All Terms}}{\text{Number of Terms}}$$

$$\text{Average (geometric mean)} = [(X_1)(X_2)(X_3)(X_4)(X_n)]^{1/n} \quad \text{The } n^{\text{th}} \text{ root of the product of } n \text{ numbers}$$

$$\text{Blending} = (V_1)(C_1) + (V_2)(C_2) = (V_3)(C_3) \quad \text{Where } V = \text{volume or}$$

Graphics from ABC Professional Operators



## Formula/Conversion Table

Wastewater Treatment, Collection, Industrial Waste, & Wastewater Laboratory Exams



$$\text{Alkalinity, mg/L as CaCO}_3 = \frac{(\text{Titrant Volume, mL})(\text{Acid Normality})(50,000)}{\text{Sample Volume, mL}}$$

$$\text{Amps} = \frac{\text{Volts}}{\text{Ohms}}$$

$$\text{Area of Circle}^* = (0.785)(\text{Diameter}^2)$$

$$\text{Area of Circle} = (3.14)(\text{Radius}^2)$$

$$\text{Area of Cone (lateral area)} = (3.14)(\text{Radius})\sqrt{\text{Radius}^2 + \text{Height}^2}$$

$$\text{Area of Cone (total surface area)} = (3.14)(\text{Radius})(\text{Radius} + \sqrt{\text{Radius}^2 + \text{Height}^2})$$

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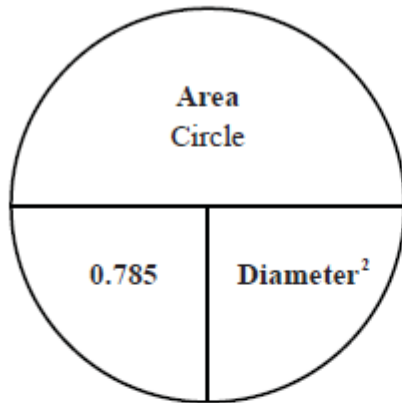
$$\text{Average (geometric mean)} = [(X_1)(X_2)(X_3)(X_4)(X_n)]^{1/n} \quad \text{The } n^{\text{th}} \text{ root of the product of } n \text{ numbers}$$

$$\text{Biochemical Oxygen Demand (seeded), mg/L} = \frac{[(\text{Initial DO, mg/L}) - (\text{Final DO, mg/L}) - \text{Seed Correction Factor, mg/L}][300 \text{ mL}]}{\text{mL of Sample}}$$

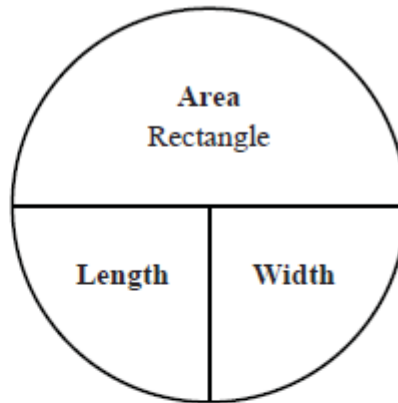
$$\text{Biochemical Oxygen Demand (unseeded), mg/L} = \frac{[(\text{Initial DO, mg/L}) - (\text{Final DO, mg/L})][300 \text{ mL}]}{\text{mL of Sample}}$$

# Aids to Navigation – Handout2

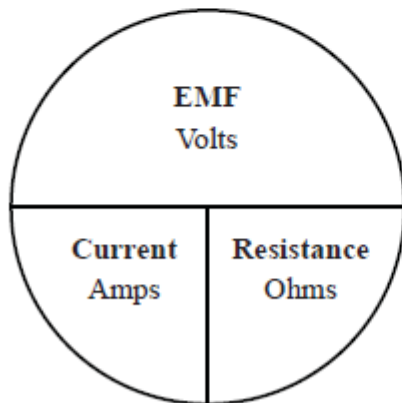
Area of Circle



Area of Rectangle

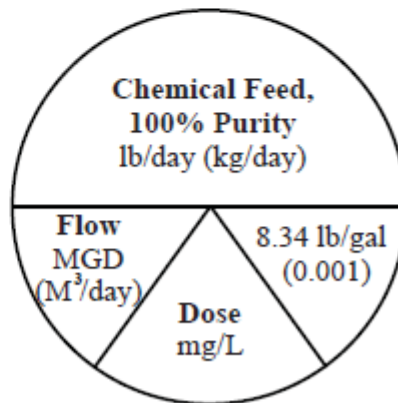


Electromotive Force (EMF), Volts



Force, lb (Newtons)

Feed Rate, lb/day (kg/day)



Loading Rate, lb/day (kg/day)

## Abbreviations

C	.....	Celsius
cfs	.....	cubic feet per second
cm	.....	centimeters
DO	.....	dissolved oxygen
EMF	.....	electromotive force
F	.....	Fahrenheit
ft	.....	feet
ft lb	.....	foot-pound
g	.....	grams
gal	.....	US gallons
gfd	.....	US gallons flux per day
gpcd	.....	US gallons per capita per day
gpd	.....	US gallons per day
gpg	.....	grains per US gallon
gpm	.....	US gallons per minute
hp	.....	horsepower
hr	.....	hours
in	.....	inches
kg	.....	kilograms
km	.....	kilometers
kPa	.....	kilopascals
kW	.....	kilowatts
kWh	.....	kilowatt-hours
L	.....	liters
lb	.....	pounds
Lpcd	.....	liters per capita per day
Lpd	.....	liters per day

## Conversion Factors

1 acre	.....	= 43,560 ft <sup>2</sup>
	.....	= 4,046.9 m <sup>2</sup>
1 acre foot of water	.....	= 326,000 gal
1 cubic foot of water	.....	= 7.48 gal
	.....	= 62.4 lb
1 cubic foot per second	.....	= 0.646 MGD
	.....	= 448.8 gpm
1 cubic meter of water	.....	= 1,000 kg
	.....	= 1,000 L
	.....	= 264 gal
1 foot	.....	= 0.305 m
1 foot of water	.....	= 0.433 psi
1 gallon (US)	.....	= 3.785 L
	.....	= 8.34 lb of water

Graphics from ABC Professional Operators

# Units of Measure

*Tracking what we count*



# Time for an Example



A 20-foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?



*Graphics from Pioneer  
Water Storage Tank*

## Time for an Example

A 20-foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?

$$\frac{10,000 \text{ gallons} * 1 \text{ hour}}{2 \text{ hours} * 60 \text{ minutes}}$$

*Change units  
from what you  
are given to  
what you need*

## Time for an Example

A 20-foot diameter tank, with 10,000 gallons of water (4.25 feet water depth) is drained in 2 hours using a pump. What is average flow rate in gpm?

$$\frac{10,000 \text{ gallons} * \cancel{1 \text{ hour}}}{\cancel{2 \text{ hours}} * 60 \text{ minutes}} = 83.3 \text{ gpm}$$

*Average flow rate. Why is this likely not the continuous flow rate beginning to end?*

# Time for an Example

Same flow, different units

$$10,000 \text{ gallons} / 7.48 \text{ gallons} / \text{cu ft}$$

$$= 1,336.89 \text{ cu ft}$$

$$= \frac{1,336.89 \text{ ft}^3}{\cancel{2 \text{ hrs} \times 60 \text{ min.} / \text{hr}} \times 60 \text{ sec.} / \cancel{\text{min.}}}$$

$$= 0.186 \text{ cubic feet per second (cfs)}$$

*Volume per unit of time*

# Time for an Example

Could we go from gpm to cfs another way?

$$10,000 \text{ gallons} / 120 \text{ minutes} = 83.3 \text{ gpm}$$

*From the info we have this is the quickest way to get volume / unit time*

$$83.3 \text{ gpm} \times \text{conversion factor} \rightarrow ? \text{ cfs}$$

*Look in our aids and tables to find a conversion factor that fits*

$$83.3 \text{ gpm} \times 0.002228 \text{ cfs} / \text{gpm}$$

$$= 0.186 \text{ cubic feet per second (cfs)}$$

# Time for Another Example

Different starting information

$$= \frac{200 \text{ cu ft}}{20 \text{ seconds}}$$

$$= 10 \text{ cubic feet per second (cfs)}$$

*Volume per unit of time*

# Percentage, Fraction & Decimal



If the Mariners went 1 for 4 on recent road trip ...  
demonstrate winning

As a fraction

As a decimal

As a percentage

# Percentage, Fraction & Decimal



If the Mariners went 1 for 4 on recent road trip ...  
demonstrate winning

$$\frac{1}{4} \text{ Fraction}$$

0.25 Decimal

25% Percentage



# Algebra

*Just who is “X” and what do they want?*

# First We Need to Understand Math Order of Operations

- The order in which operations should be done is abbreviated as PEMDAS
  - **P**arentheses **()**
  - **E**xponents **^**
  - **M**ultiplication & **D**ivision (from left to right) **\*** **/**
  - **A**ddition & **S**ubtraction (from left to right) **+** **-**
    - **“Please Excuse My Dear Aunt Sally”**
  - $Q = \frac{(w_1 + w_2)}{2} * d * C / n * R^{2/3} * S^{1/2}$   
(Manning's Equation for a trapezoidal channel)

# Algebra – Solving for X (and sometimes half of the rest of the alphabet)

*Addition*

$$X + 3 = 12$$

*Looking to isolate X on one side of the equation*

$$X + 3 - 3 = 12 - 3$$

$$X = 9$$

Subtract 3 from each side of the equal sign

# Algebra – Solving for X

*Subtraction*

$$X - 3 = 12$$

$$X - 3 + 3 = 12 + 3$$

$$X = 15$$

*Again we are looking to isolate X on one side of the equation*

Add 3 from each side of the equal sign

# Algebra – Solving for X

$$3 * X = 12$$

*Multiplication*

$$\frac{3 * X = 12}{3 \quad 3}$$

$$\frac{\cancel{3} * X = 12}{\cancel{3} \quad 3}$$

$$X = 4$$

Divide each side by 3

# Algebra – Solving for X

$$X / 3 = 12$$

*Division*

$$\frac{X * 3}{3} = 12 * 3$$

$$\frac{\cancel{X * 3}}{\cancel{3}} = 12 * 3$$

$$X = 36$$

Multiply each side by 3

# Algebra – Solving for X

$$36 / X = 12$$

$$\frac{36 * X}{X * 12} = \frac{12 * X}{12}$$

$$\frac{36 * \cancel{X}}{\cancel{X} * 12} = \frac{\cancel{12} * X}{\cancel{12}}$$

$$X = 3$$

Multiply each side by X to bring X to the numerator and divide each side by 12 to isolate X on one side of the equation

# Trigonometry

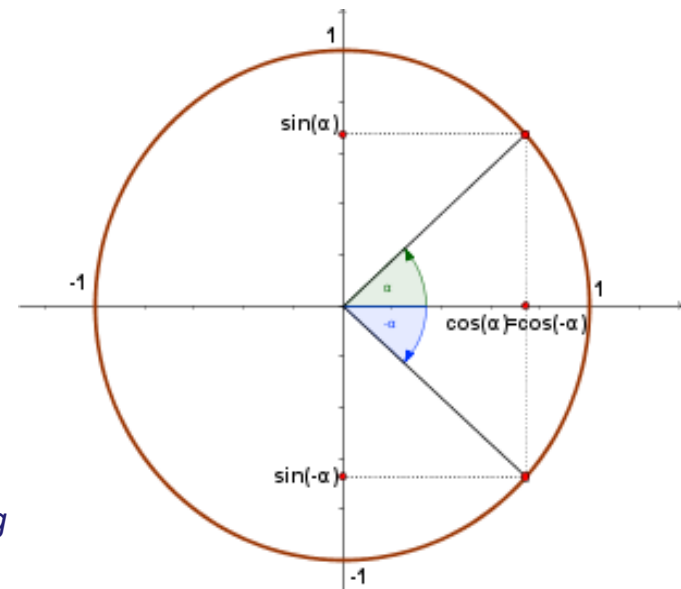
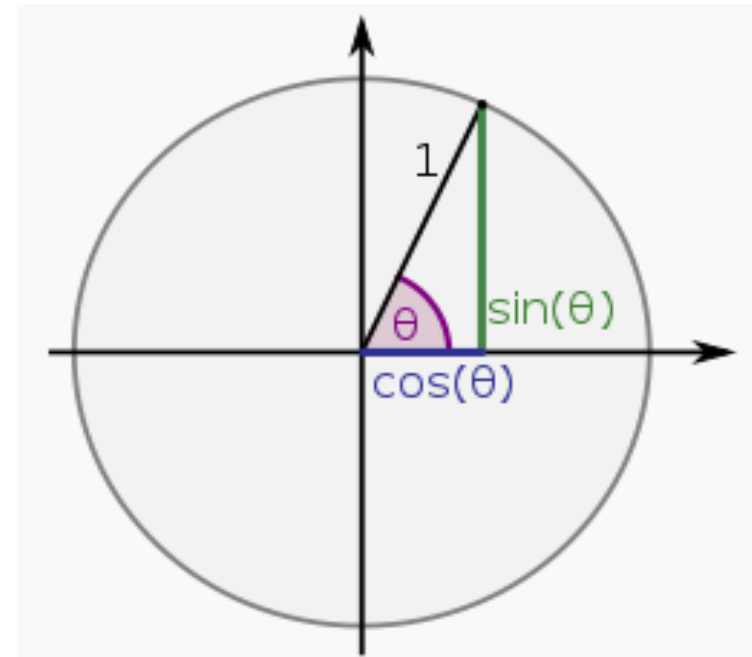
*It's all about relationships!*



# Trigonometry

- From Greek trigonon "triangle" + metron "measure"
- New terms
  - Angle (theta,  $\theta$ )
  - Sine
  - Cosine
  - Tangent

*Graphics from Wikipedia & MathPortal.org*

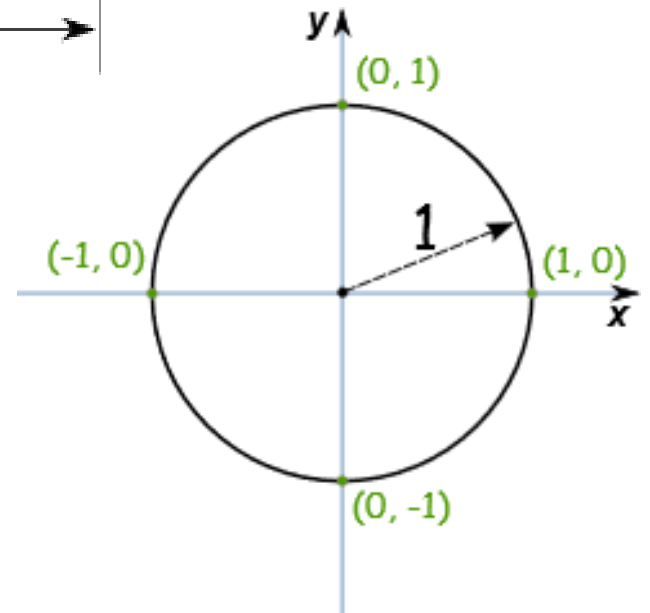
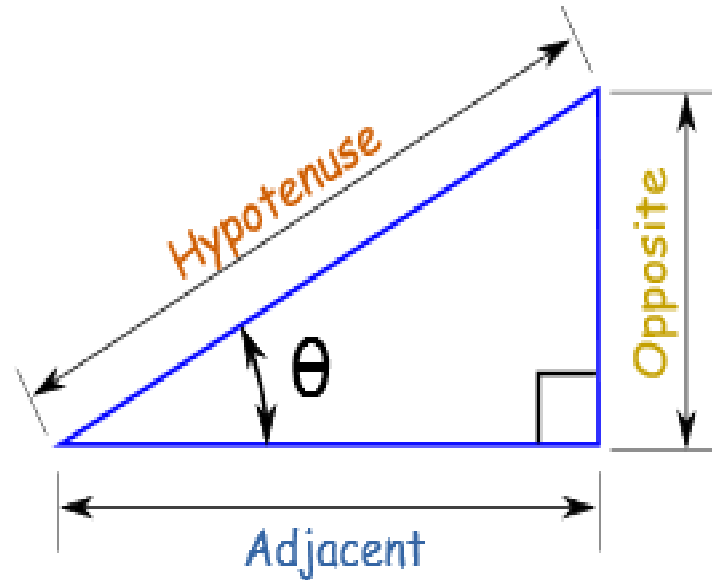


# How are They Defined?

$$\sin \theta = \frac{\text{Opposite}}{\text{Hypotenuse}}$$

$$\cos \theta = \frac{\text{Adjacent}}{\text{Hypotenuse}}$$

$$\tan \theta = \frac{\text{Opposite}}{\text{Adjacent}}$$



Angle	Degrees	Radians
⊥ Right Angle	90°	$\pi/2$
— Straight Angle	180°	$\pi$
○ Full Rotation	360°	$2\pi$

Graphics from [Mathisfun.com](http://Mathisfun.com)

# Conversion Factors

*It's all about tracking units!*

# Conversion Factors are Your Friend!

*Most all of water and wastewater math is about converting from one set of units to another.*

# Conversion Factors are Your Friend!

1 foot of water = 0.433 psi

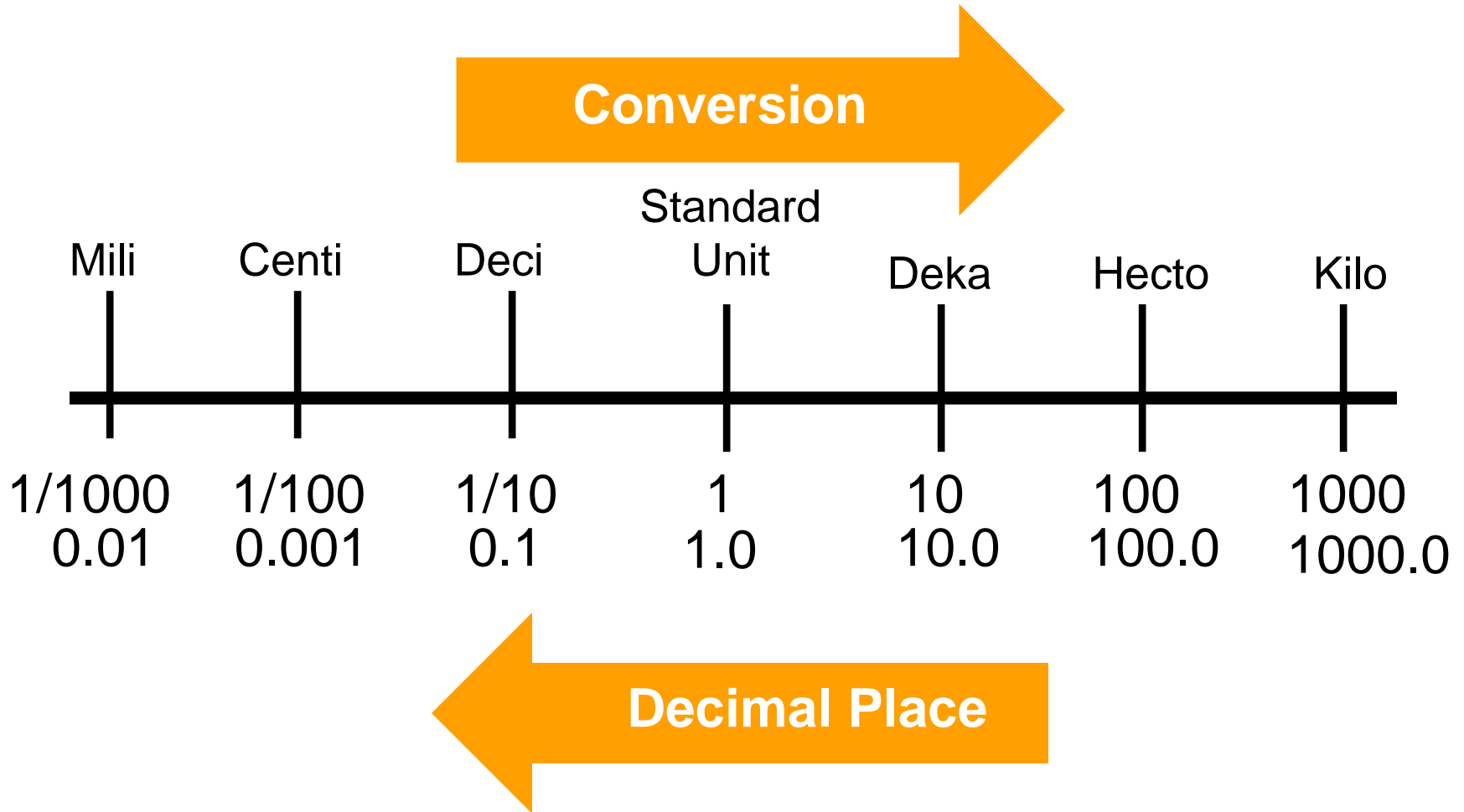
1 psi = 2.31 feet of water (head)

1 cubic foot = 7.48 gallons

1 gallon water = 8.34 pounds

Memorize these (and other)  
conversion factors!

# Conversion Factors are Your Friends!



# Time Conversion Example



Determine how many seconds are in a day.

# Starting Point



1d

sec.

Start with 1 day and head towards seconds, one unit of measure at a time.



# One Step at a Time Days to Hours

1d

24 hr

sec.

d

24 hour per day

# One Step at a Time

~~1d~~

24 hr

sec.

~~d~~

Days cancel out

# One Step at a Time – Hours to Minutes

~~1d~~

24 hr

60 min

~~d~~

hr

60 minutes per hour

# One Step at a Time – Hours to Minutes

~~1d~~

~~24 hr~~

60 min

sec.

~~d~~

~~hr~~

Hours cancel

# One Step at a Time – Minutes to Seconds

~~1d~~

~~24 hr~~

60 min

60 sec

~~d~~

~~hr~~

min

60 Seconds per minute

# One Step at a Time

~~1d~~

~~24 hr~~

~~60 min~~

60 sec

~~d~~

~~hr~~

~~min~~

Minutes cancel

## Now do the Math

Multiply

$$1 \times 24 \times 60 \times 60 =$$

86,400 seconds in 1 day

# Keeping Track of the Units

1 foot of water = 0.433 psi



What is the pressure of 3 feet of water?



# Keeping Track of the Units

$$1 \text{ foot of water} = 0.433 \text{ psi}$$

$$3 \text{ feet of water} * \frac{0.433 \text{ psi}}{1 \text{ foot of water}}$$

# Keeping Track of the Units

1 foot of water = 0.433 psi

$$\frac{3 \text{ feet of water} * 0.433 \text{ psi}}{1 \text{ foot of water}}$$

$$= 1.3 \text{ psi}$$

# Keeping Track of Units

1 foot of water = 0.433 psi



If the pressure is 3 psi what is that in feet of water?

# Keeping Track of Units

1 foot of water = 0.433 psi

$$\frac{3 \cancel{\text{psi}} * 1 \text{ foot of water}}{0.433 \cancel{\text{psi}}}$$

= 6.9 feet of water

# Keeping Track of Units

1 cubic foot = 7.48 gallons

 How many cubic feet in 100 gallons?

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ gallons} * \frac{1 \text{ cubic foot}}{7.48 \text{ gallons}}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \cancel{\text{ gallons}} * \frac{1 \text{ cubic foot}}{7.48 \cancel{\text{ gallons}}}$$

$$= 13.4 \text{ cubic feet (ft}^3\text{)}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons



How many gallons in 100 cubic feet?



# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Keeping Track of Units

1 cubic foot = 7.48 gallons

$$100 \text{ ~~cubic feet~~} * \frac{7.48 \text{ gallons}}{1 \text{ ~~cubic foot~~}}$$

=748 gallons

# Keeping Track of Units

1 gallon water = 8.34 pounds

 How many gallons in 100 pounds of water?

# Keeping Track of Units

1 gallon water = 8.34 pounds

100 pounds \*  $\frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$

# Keeping Track of Units

1 gallon water = 8.34 pounds

$$100 \cancel{\text{ pounds}} * \frac{1 \text{ gallon water}}{8.34 \cancel{\text{ pounds}}}$$

= 12 gallons

# Keeping Track of Units

1 gallon water = 8.34 pounds



How many pounds in 100 gallons of water?

# Keeping Track of Units

1 gallon water = 8.34 pounds

$$100 \text{ gallons} * \frac{8.34 \text{ pounds}}{1 \text{ gallon water}}$$

# Keeping Track of Units

1 gallon water = 8.34 pounds

$$100 \cancel{\text{ gallons}} * \frac{8.34 \text{ pounds}}{1 \cancel{\text{ gallon water}}}$$

= 834 pounds



# Examples

*Let's try out the process*

# Problem

How many gallons in a ton of water?



# Problem – Changing Units

How many gallons in a ton of water?

1 gallon water = 8.34 pounds

1 ton = 2000 pounds

# Problem

How many gallons in a ton of water?

$$1 \text{ ton} * \frac{2000 \text{ pounds}}{1 \text{ ton}} * \frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$$

# Problem

How many gallons in a ton of water?

$$1 \cancel{\text{ton}}^* \times \frac{2000 \text{ pounds}}{1 \cancel{\text{ton}}} \times \frac{1 \text{ gallon water}}{8.34 \text{ pounds}}$$

# Problem

How many gallons in a ton of water?

$$\cancel{1 \text{ ton}}^* \times \frac{\cancel{2000 \text{ pounds}}}{\cancel{1 \text{ ton}}} * \frac{1 \text{ gallon water}}{\cancel{8.34 \text{ pounds}}}$$

$$= 239.8 \text{ gallons}$$

# Problem

How many cubic feet in a ton of water?



# Problem

How many cubic feet in a ton of water?

$$1 \text{ ton} * \frac{2000 \text{ pounds}}{1 \text{ ton}} * \frac{1 \text{ gallon water}}{8.34 \text{ pounds}} * \frac{1 \text{ cubic foot}}{7.48 \text{ gallons}}$$



# Problem

How many cubic feet in a ton of water?

$$\cancel{1 \text{ ton}} * \frac{2000 \cancel{\text{ pounds}}}{\cancel{1 \text{ ton}}} * \frac{1 \cancel{\text{ gallon water}}}{8.34 \cancel{\text{ pounds}}} * \frac{1 \text{ cubic foot}}{7.48 \cancel{\text{ gallons}}}$$

$$= 32.1 \text{ cubic feet}$$

# Problem – Short cut if you know the conversion factor

How many cubic feet in a ton of water?

$$1 \cancel{\text{ ton}} * \frac{2000 \cancel{\text{ pounds}}}{1 \cancel{\text{ ton}}} * \left( \frac{1 \text{ cubic foot}}{62.4 \cancel{\text{ pounds}}} \right)$$

$$= 32.1 \text{ cubic feet}$$

# Significant Figures & Rounding – The Result

Significant figures –

How many # after the decimal point?

Usually one significant figure after the decimal point is sufficient or 3 numbers

So instead of 11.99034325234

It would be 12.0

11.09 would be 11.1

11.04 would be 11.0

# Significant Figures & Rounding – The Calculation

Generally, let the calculator or computer carry whatever they have. If you have to write down a number as part of an interim step,  
Use the roundoff rules

# Practical Applications

*How do we use this ability?*

# Distance, Area and Volumes

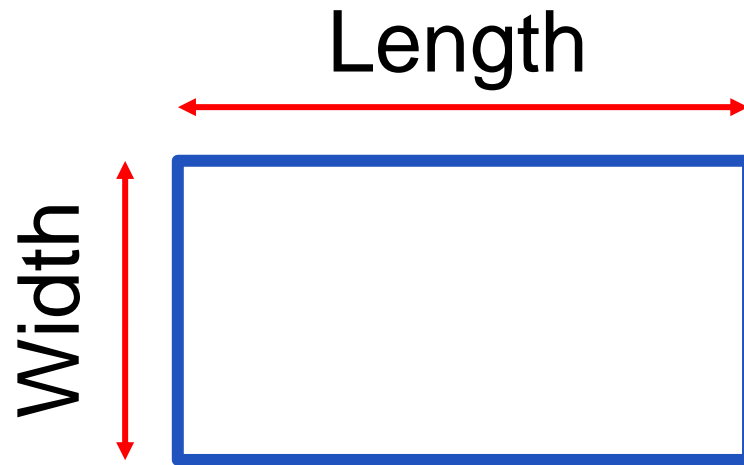
Distance is one dimension (i.e. ft, meters)

Areas are two dimensions (i.e.  $\text{ft}^2$ , SY, acres )

Volumes are three dimensions (i.e.  $\text{ft}^3$ , CM)

Other Volumes: Gallons, Liters, acre-ft

# Area – Squares / Rectangles

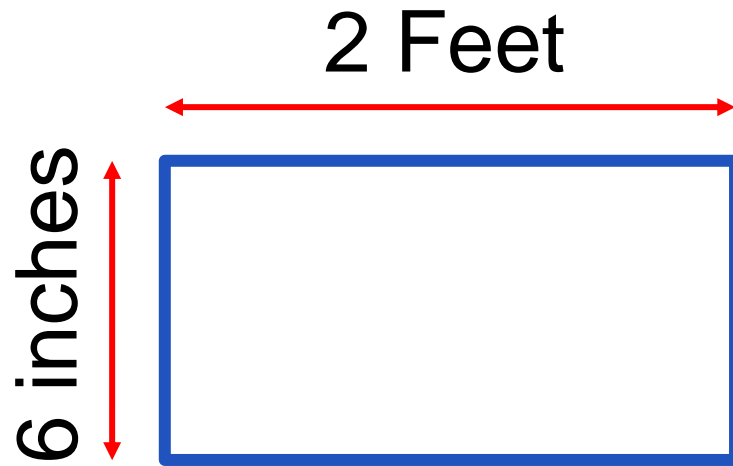


$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = \text{dimension}^1 * \text{dimension}^1$$

*Note 1 – Dimensions need to be the same units of measure*

# Area

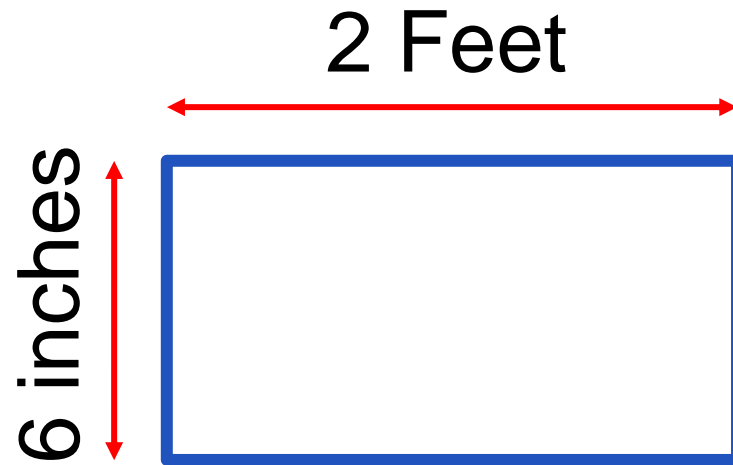


What is the  
area?

$$\text{Area} = \text{length} * \text{width}$$
$$\text{Area} = \text{dimension} * \text{dimension}$$



# Area



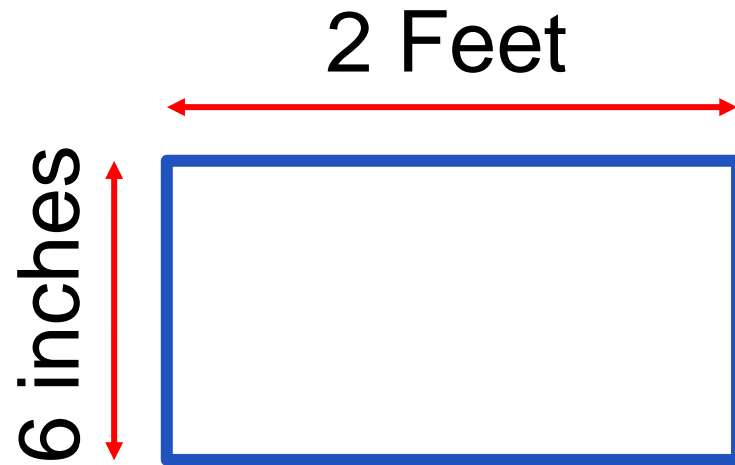
What is the area?

*First get all the dimensions in the same units*

$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = 2 \text{ feet} * \frac{6 \text{ inches} * 1 \text{ foot}}{12 \text{ inches}}$$

# Area



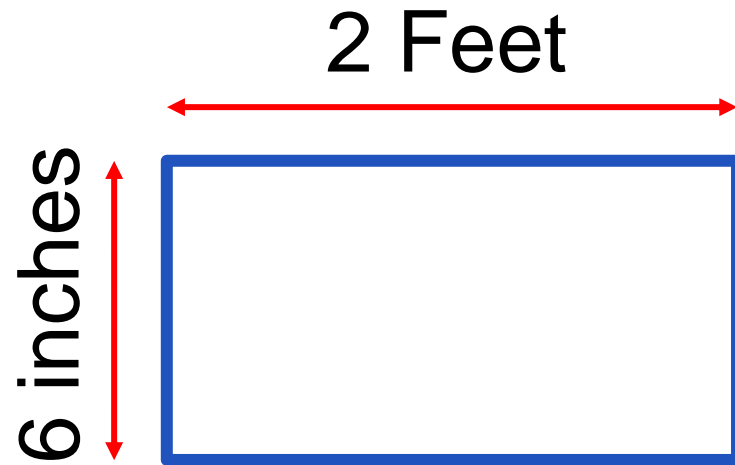
What is the area?

$$\text{Area} = \text{length} * \text{width}$$

$$\text{Area} = 2 \text{ feet} * \frac{\cancel{6 \text{ inches}} * 1 \text{ foot}}{\cancel{12 \text{ inches}}}$$

$$\text{Area} = 1 \text{ sq ft}$$

# Area



What is the area?

*What if we need the area in square inches?*

$$\text{Area} = \text{length} * \text{width}$$

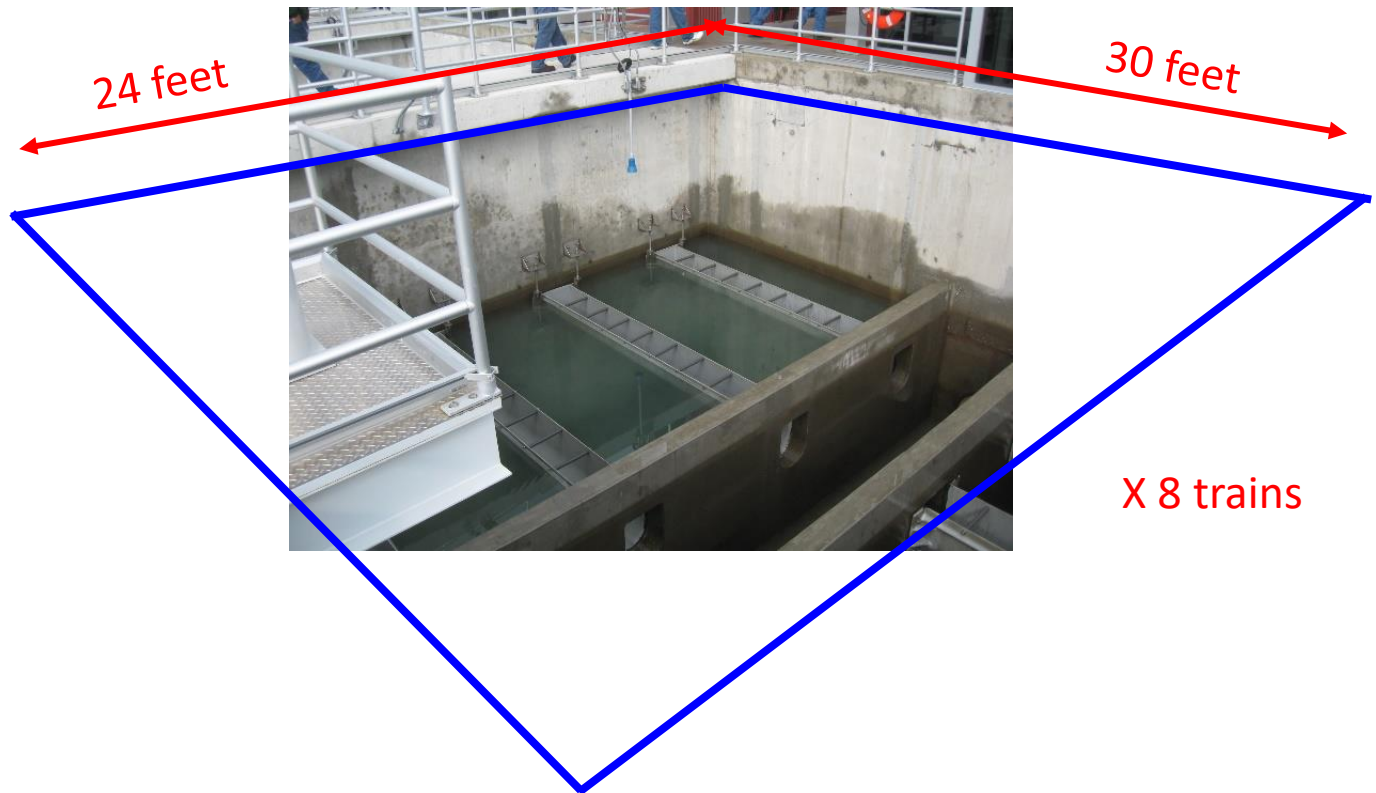
$$\text{Area} = 2 \text{ feet} * \frac{12 \text{ inches}}{1 \text{ foot}} * 6 \text{ inches}$$

$$\text{Area} = 144 \text{ sq in}$$

# Practical Application



You are going to cover your sand filters and the sales rep wants to know the area so he can get you a price. There are 8 trains, each 24 feet wide by 30 feet long.



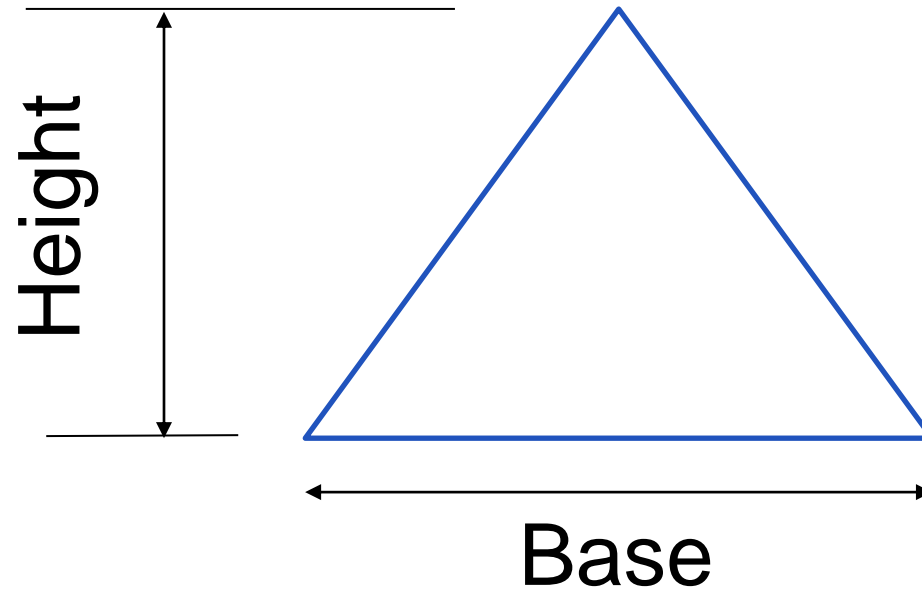
## Practical Application - Area

You are going to cover your sand filters and the sales rep wants to know the area so he can get you a price. There are eight trains, each 24 feet wide by 30 feet long.

$$\text{Area} = 8 \text{ basins} * 24 \text{ ft} * 30 \text{ ft}$$

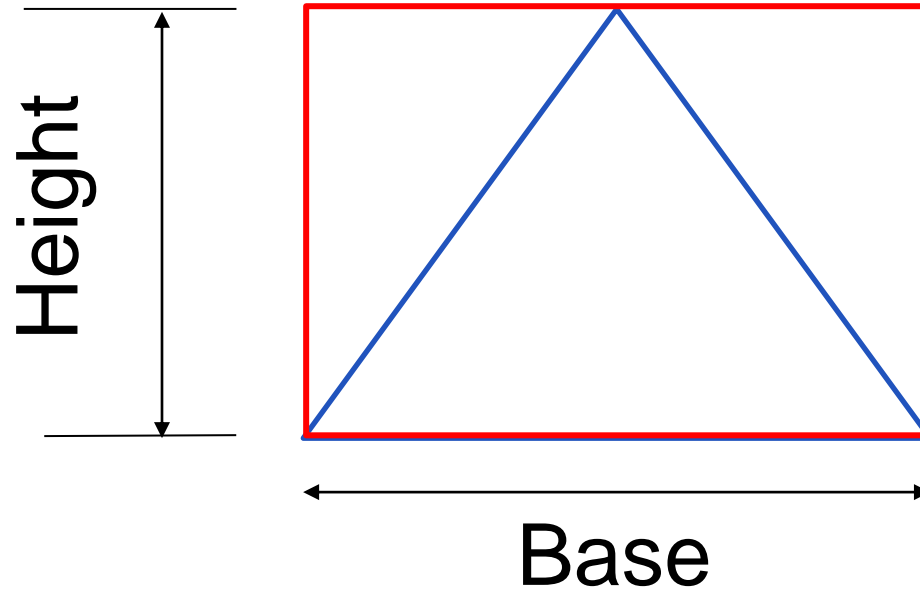
$$\text{Area} = \mathbf{5,760 \text{ sq ft}}$$

# Area - Triangles



$$\text{Area} = (1/2) * \text{base} * \text{height}$$

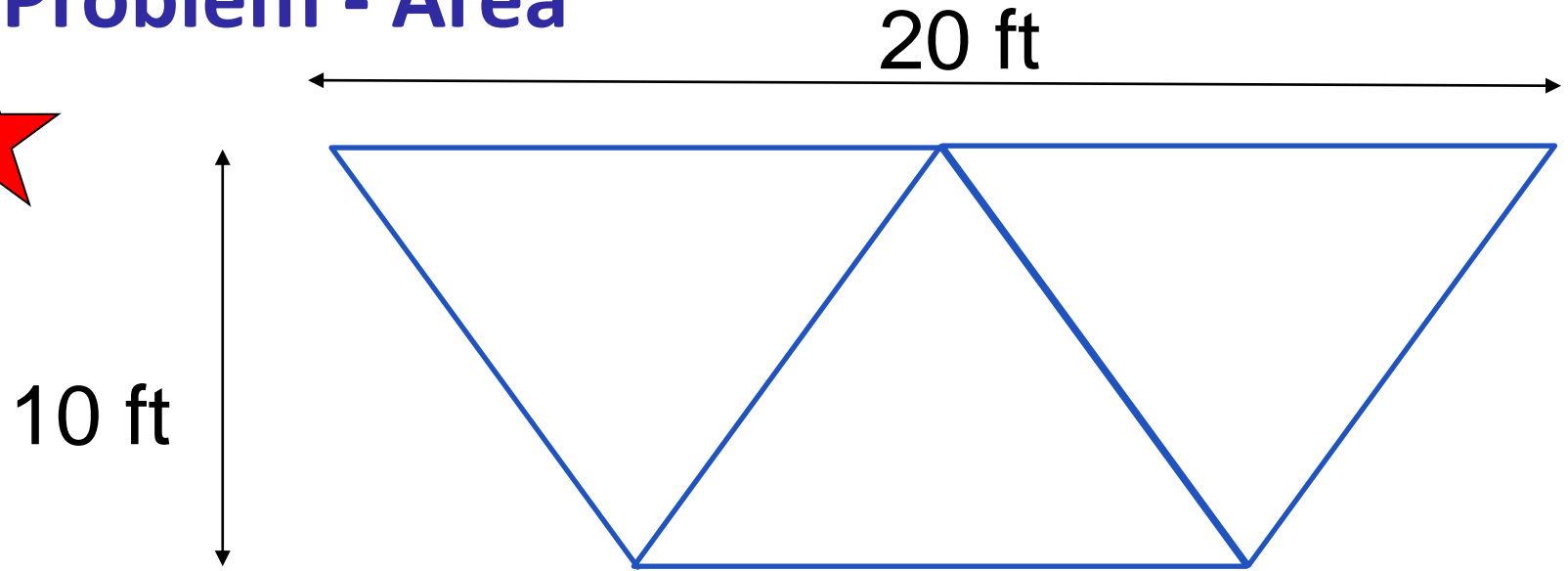
# Area



$$\text{Area} = (1/2) * \text{base} * \text{height}$$

Triangle is  $\frac{1}{2}$  of rectangle!

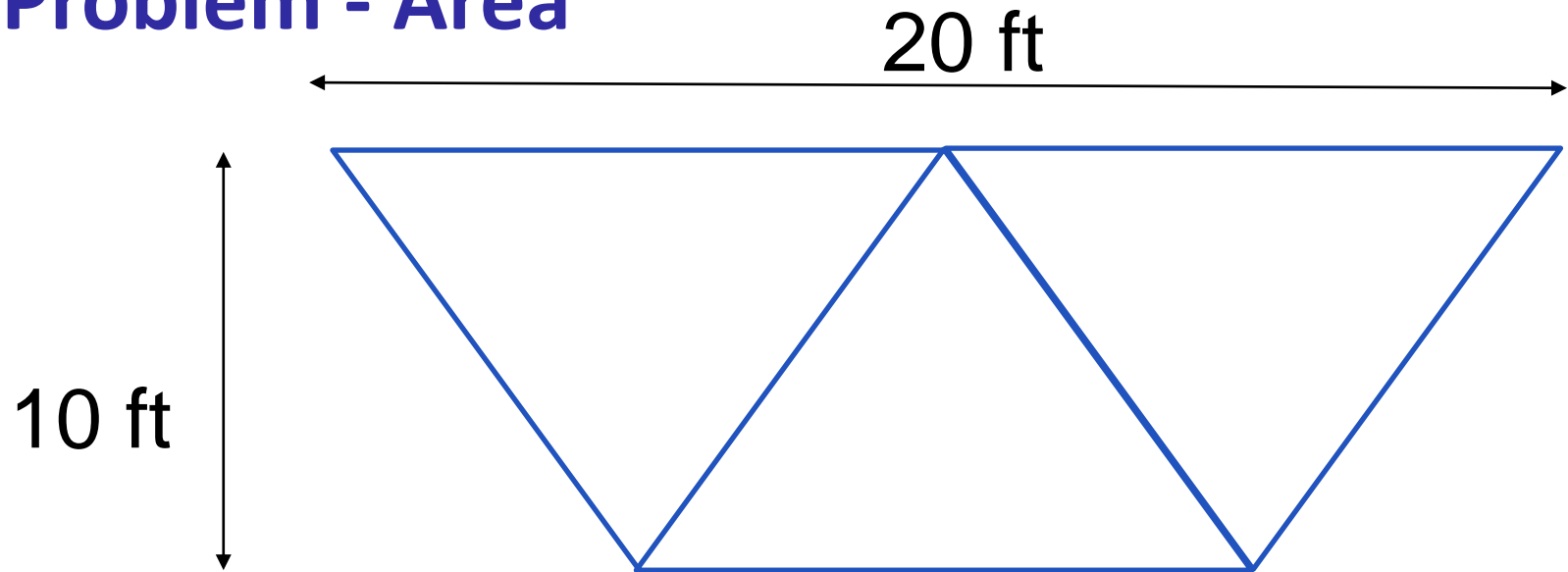
## Problem - Area



You are covering a truss with a banner for City Celebration. They want to cover the truss. How big?



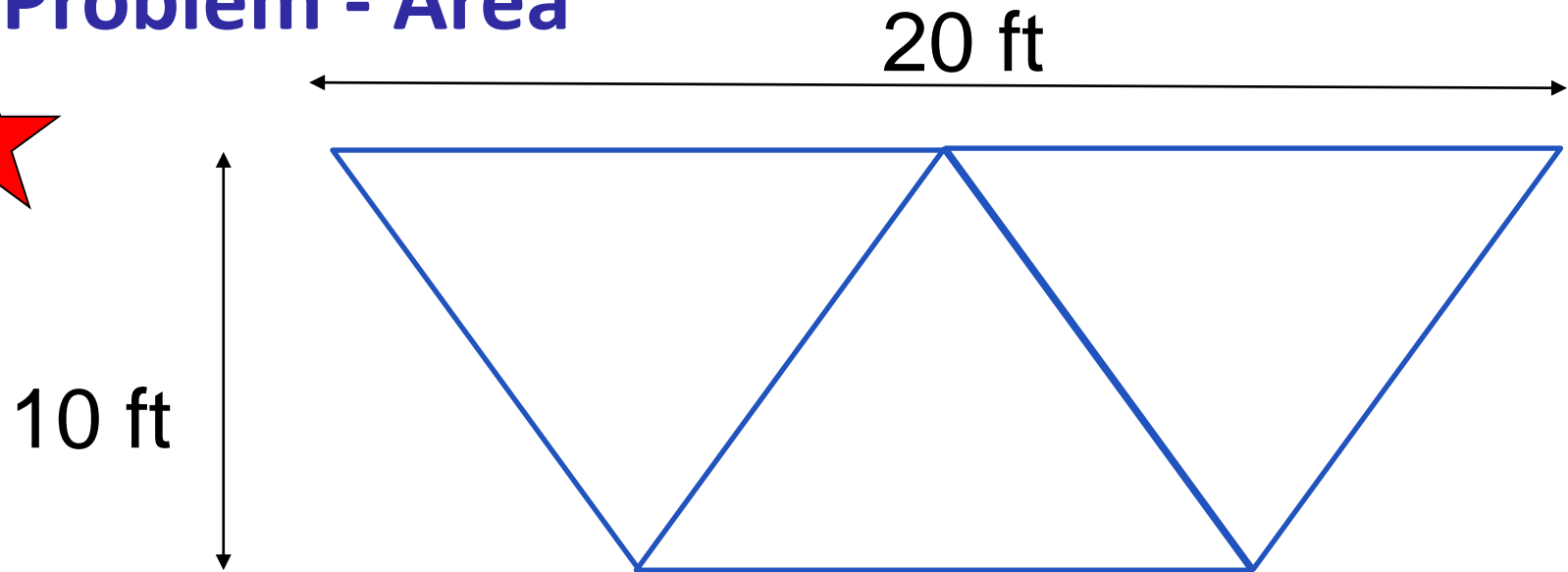
## Problem - Area



You are covering a truss with a banner for City Celebration. They want to cover the truss. How big will the banner be?

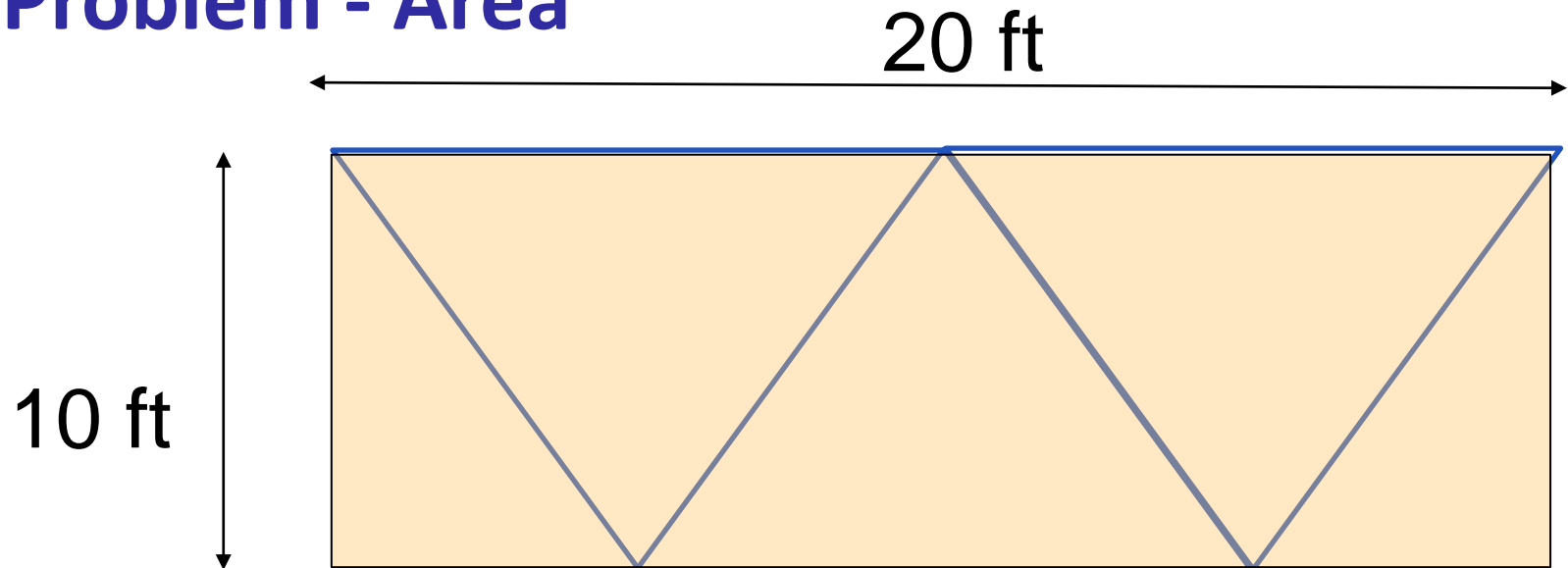
$$\begin{aligned}\text{Area} &= 3 \text{ triangles} \\ &= 3 * \frac{1}{2} * 10 \text{ ft} * 10 \text{ ft} \\ &= 150 \text{ sq ft}\end{aligned}$$

## Problem - Area



Opps! Change of plan, the City Manager now wants a rectangular banner – how big will it be?

## Problem - Area



The City Manager wants  
rectangular banner – how big?

$$\text{Area} = 20 \text{ ft} * 10 \text{ ft} = 200 \text{ sq ft}$$

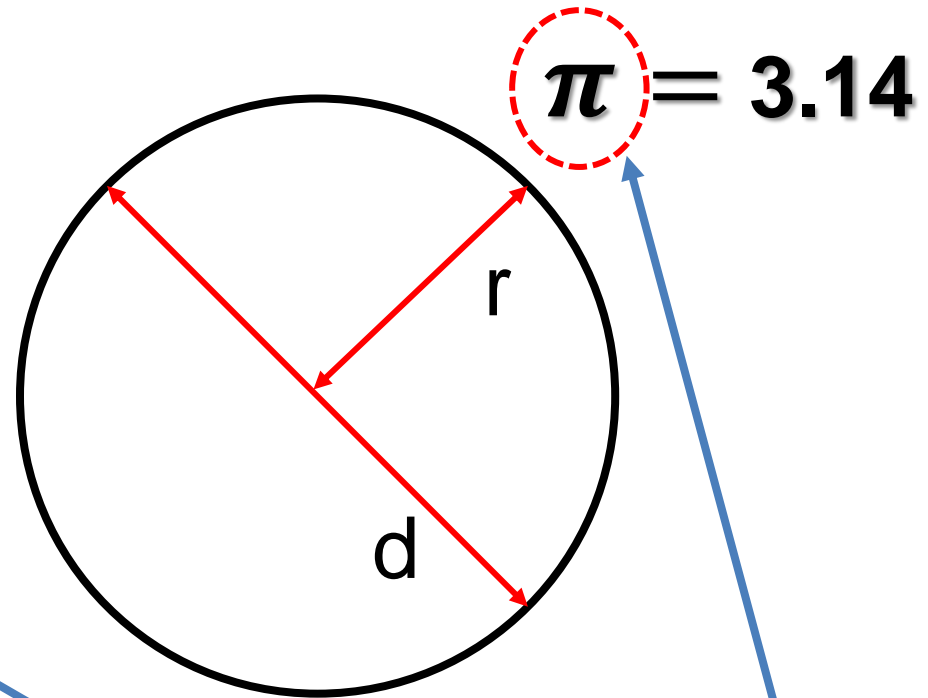
# Area - Circles

Area of a circle

$$A = \pi r^2$$

$$A = \pi (d^2 / 4)$$

$$A = 0.785 * d^2$$



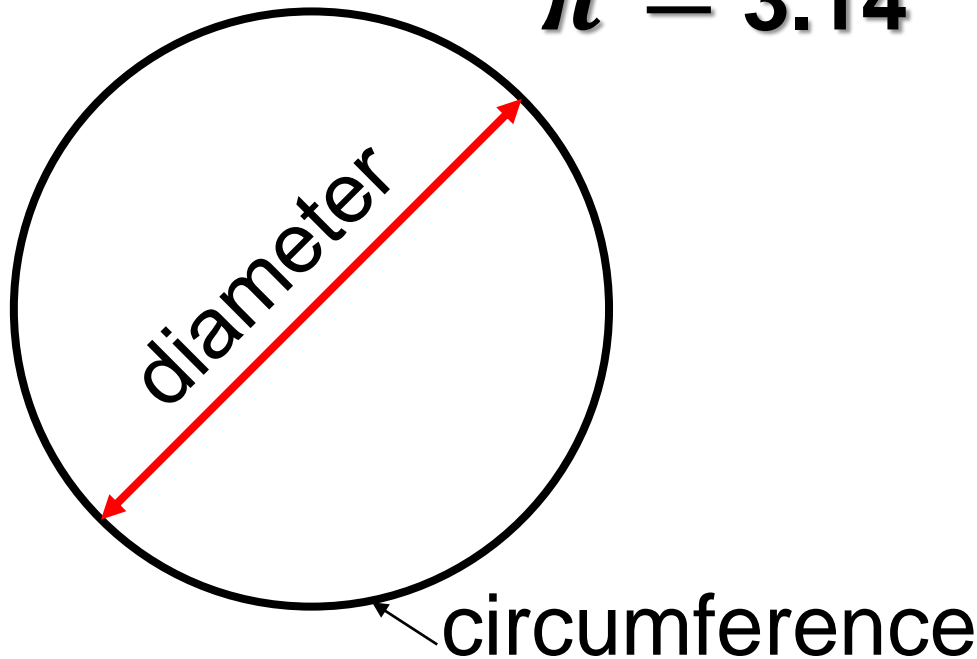
What is this symbol? It's all Greek to me!

Or use a constant

# The Magical World of Pi

Pi is a name given to the ratio of the circumference of a circle to the diameter.

$$\pi = 3.14$$



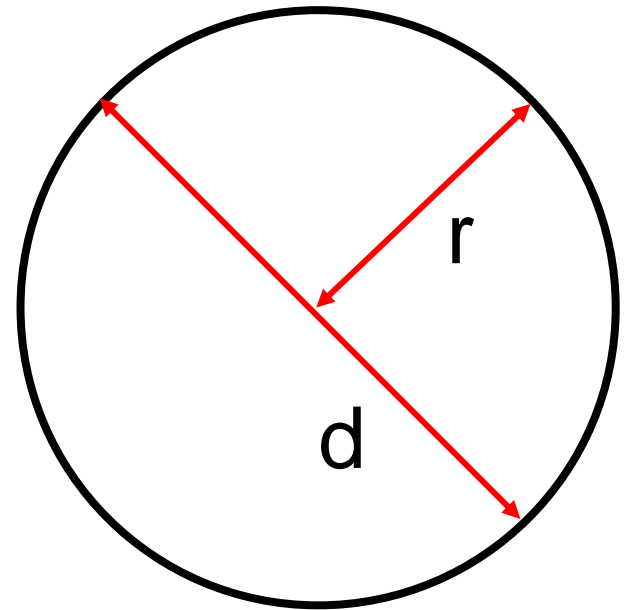
$\pi$   
3.14159  
265358979323  
84626433832795  
02884197169399375  
1058209749445923078  
164062862089986280  
3482534211706798214808  
651328230664709384460955058223  
17253594081284811174502841027019385211055  
59644622948954930381964428810975665933446128475648233786  
7831652712019091456485669234603486104543266482133936072602491412737245  
8700660631558817488152092096282925409171536436789259036001133053054882046652138414695194  
1511609433057270365759591953092186117381932611793105118548074462379962749567351885752748912279381  
8301194912983367336244065664308602139494639522473719070217986094370277053921717629317675238467481846766  
94051320005681271452635608277857713427577896091736371787214684409012249534301465495853710507922796892589235420  
199561121290219608640344181598136297747130996051870721134999998372978049951059731732816096318595024459455469083026  
425223082534468503526193118817101000313783875286587533208381420617177669147303598253490428755468731159562863882357875937519  
578185778053217122680661300192787661119500921642019893809525272010654858632788659361533818279682303019520353018529689957762259941389124  
97217528347913151557485724264130695958295311686172785588075098381754637464939319255064009277016711390984882401283856160356370766011471018194295559619846  
7673744444255797172847740475346420866682596949129313677028915210475216295960240780815019351123332000355874632749647320914912752402392768237840808934

# The Magical World of Pi

$$\text{Circumference} = 2 * \pi * r$$

$$\text{Diameter} = 2 * r$$

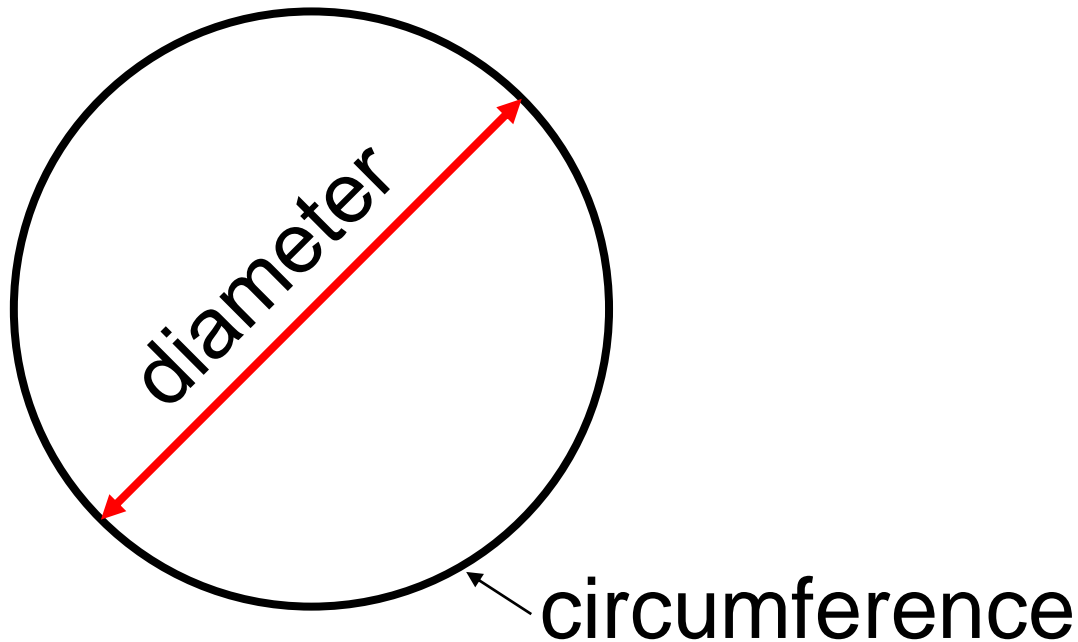
$$\frac{2 * \pi * r}{2 * r} = \pi$$



# Practical Use of Pi ( $\pi$ )

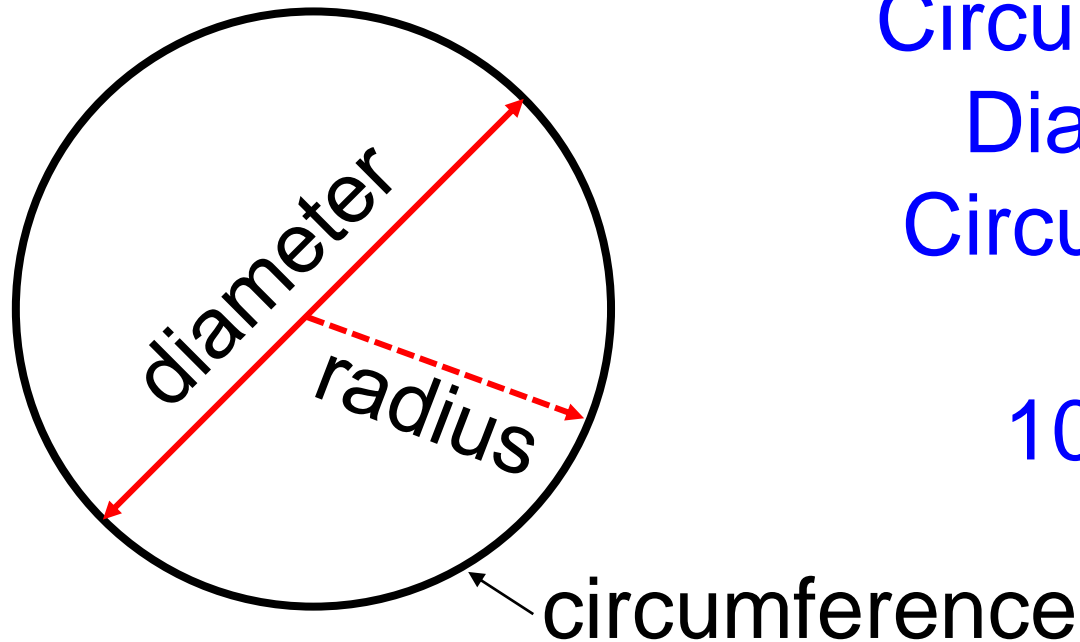


The diameter of the circular clarifier is 100 feet.  
What is the weir length (the circumference)?



## Practical Use of Pi ( $\pi$ )

The diameter of the circular clarifier is 100 feet.  
What is the weir length?



$$\text{Circumference} = 2 \pi r$$

$$\text{Diameter (d)} = 2 r$$

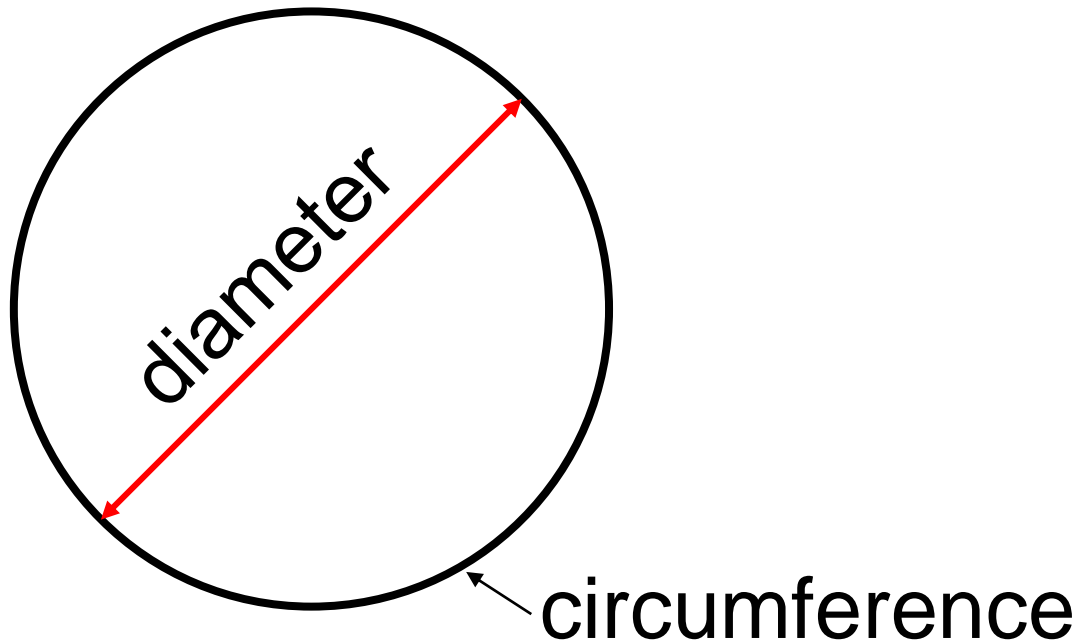
$$\text{Circumference} = \pi d$$

$$100 \text{ feet} * \pi = \\ = 314 \text{ feet}$$



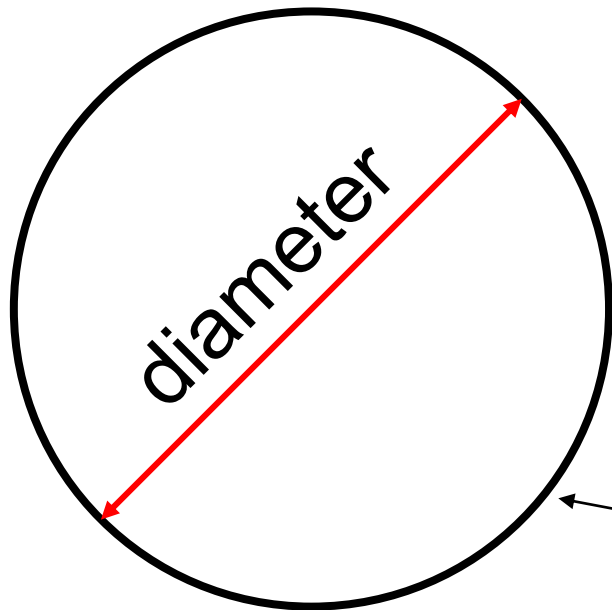
## Practical Use of Pi ( $\pi$ ) – Back to Area

The diameter of the circular clarifier is 100 feet.  
What is the surface area?



## Practical Use of Pi ( $\pi$ )

The diameter of the circular clarifier is 100 feet.  
What is the surface area?



$$\text{Area} = 0.785 * d^2$$

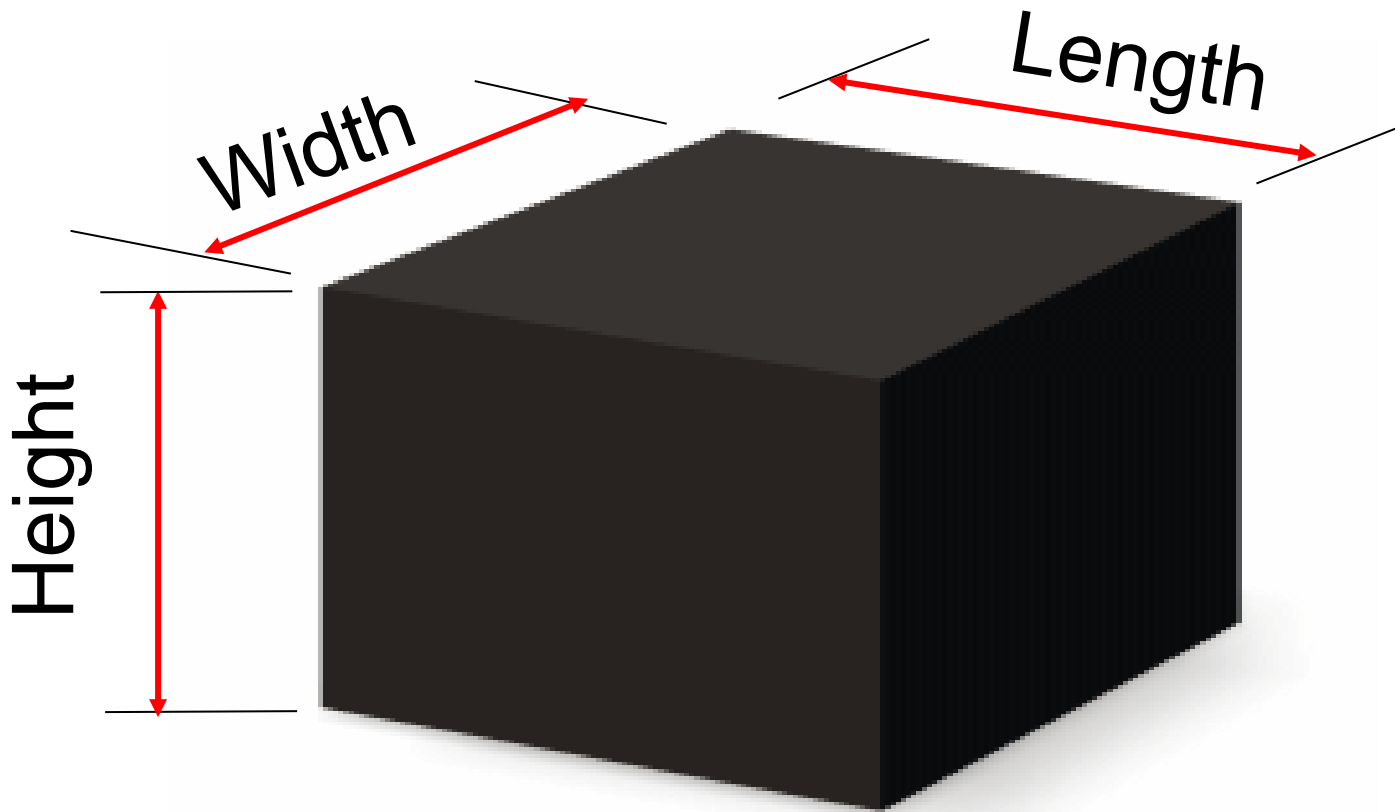
$$\text{Area} = 0.785 * (100 \text{ feet})^2$$

$$\text{Area} = 7,850 \text{ sq ft}$$

circumference

# Volume

$$\text{Volume} = \text{length} * \text{width} * \text{height}$$



## Volumes – Practical Question

★ What is the volume of water in a rectangular basin with following characteristics? Answer in **gallons**.

- Length 200 **feet**
- Width 50 **feet**
- Total Depth 20 **feet**
- Freeboard is 3 **feet**

Desired answer needs to be gallons (volume). Basin dimensions are in feet (length)

**Depth of water = 20 feet – 3 feet**

Volume = length \* width \* depth

Volume = 200 ft \* 50 ft \* 17 feet

Volume = 170,000 **cu ft**

## Volumes – Practical Question

What is the volume of water in a rectangular basin with following characteristics? Answer in gallons.

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 3 feet

**Change cubic feet to gallons – keep the units straight!**

$$\text{Volume} = \frac{170,000 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$

## Volumes – Practical Question

What is the volume of water in a rectangular basin with following characteristics? Answer in gallons.

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 3 feet

**Change cubic feet to gallons – keep the units straight!**

$$\text{Volume} = \frac{170,000 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$

$$\text{Volume} = 1,271,600 \text{ gallons or } 1.27 \times 10^6$$

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics?

Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet } - 1 \text{ meter }$$

*Mixed units! Get all dimensions in one measurement unit*

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - 1 \text{ meter} \times \frac{3.28 \text{ feet}}{1 \text{ meter}}$$

*Change meters to feet*



## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - \frac{1 \text{ meter} * 3.28 \text{ feet}}{1 \text{ meter}}$$

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

What is the water depth (height)?

$$= 20 \text{ feet} - 3.28 \text{ feet}$$

$$= 16.72 \text{ feet}$$

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

With all measurements in feet, now calculate the volume in cubic feet

$$\begin{aligned}\text{Vol} &= 50 \text{ ft} * 200 \text{ ft} * 16.72 \text{ ft} \\ &= 167,200 \text{ ft}^3\end{aligned}$$

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

*Now change cubic feet to gallons*

$$\text{Vol} = 167,200 \text{ ft}^3$$

$$167,200 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

## Volumes – Practical Question

What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

*Now change gallons  
to million gallons*

$$\text{Vol} = 1,250,656 \text{ gallons}$$

$$\text{Vol} = \frac{1,250,656 \text{ gallons} * 1 \text{ MG}}{1,000,000 \text{ gal}}$$

## Volumes – Practical Question


What is the volume of the water in the rectangular basin with following characteristics? Answer in MG (million gallons)

- Length 200 feet
- Width 50 feet
- Total Depth 20 feet
- Freeboard is 1 meter

$$\text{Vol} = 1,250,656 \text{ gallons}$$

$$\text{Vol} = \frac{1,250,656 \text{ gallons}}{1,000,000 \text{ gallons}} * 1 \text{ MG} = \underline{\underline{1.25 \text{ MG}}}$$

*Round off the answer*



# Volume –Tank Example (Cylinder)

Volume = Area x Height

$$\pi = \text{pi} = 3.14$$

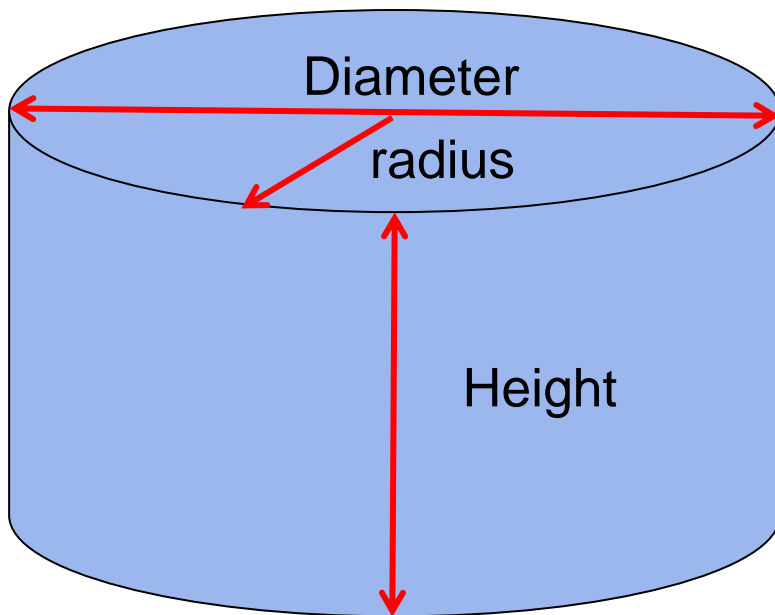
r = radius

D = Dia. = Diameter

$$2 * r = \text{Dia.}$$

$$\begin{aligned} \text{Vol} &= 3.14 * r^2 * \text{height} \\ &= .785 * d^2 * \text{height} \end{aligned}$$

Tank



# Volume –Tank Example



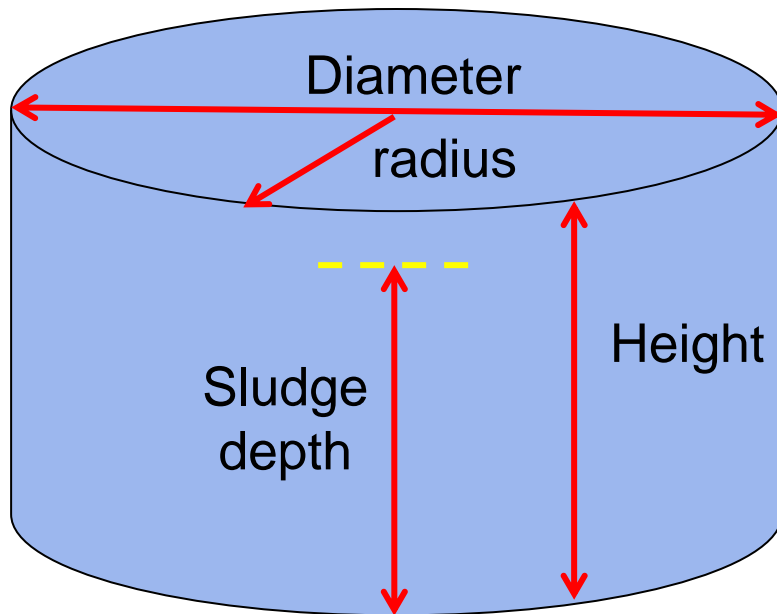
What is volume of sludge holding tank in gallons?

Diameter = 100 feet

Height = 24 feet

Sludge depth = 20 feet

Tank





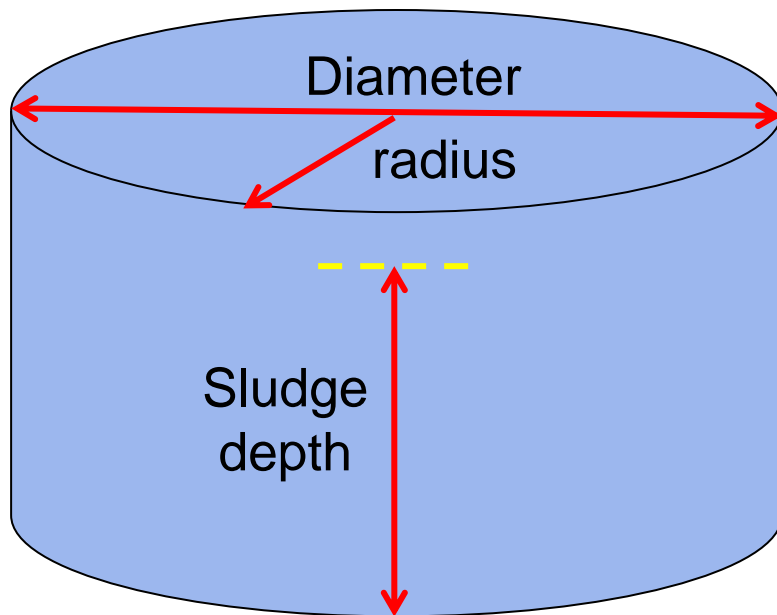
# Volume –Tank Example

What is volume of sludge holding tank in gallons?

Diameter = 100 feet

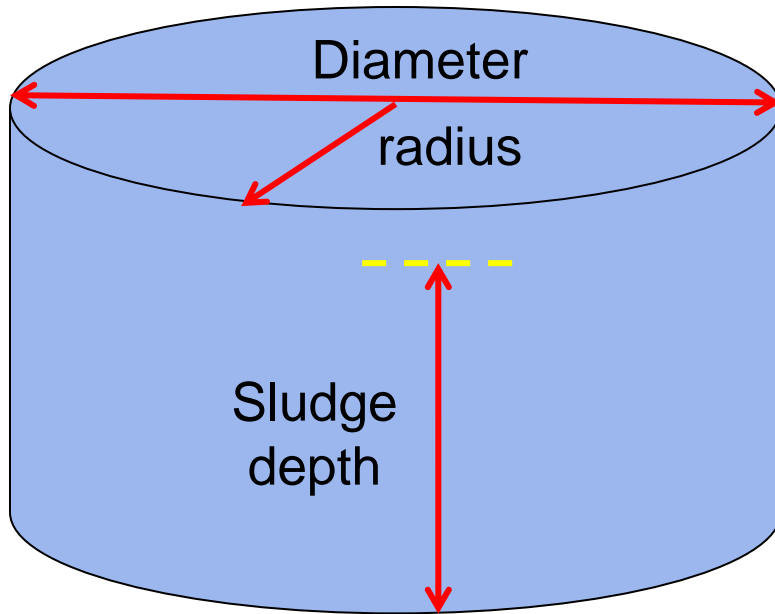
Height = 24 feet

Tank



$$\begin{aligned}\text{Vol} &= 0.785 * d^2 * \text{height} \\ &= 0.785 * (100 \text{ ft})^2 * 20 \text{ ft} \\ &= 157,000 \text{ ft}^3\end{aligned}$$

# Volume –Tank Example



What is volume of sludge holding tank in gallons?

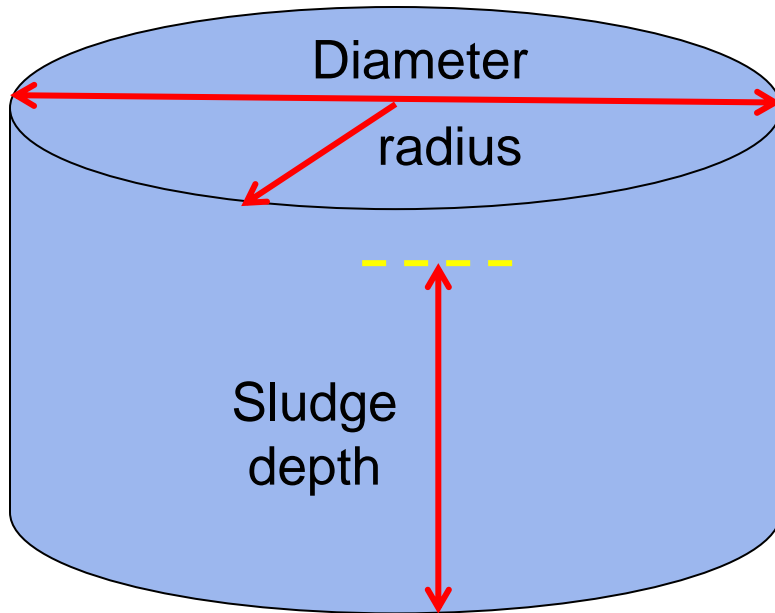
Diameter = 100 ft

Sludge depth = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3$$

$$157,000 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Volume –Tank Example



What is volume of sludge holding tank in gallons?

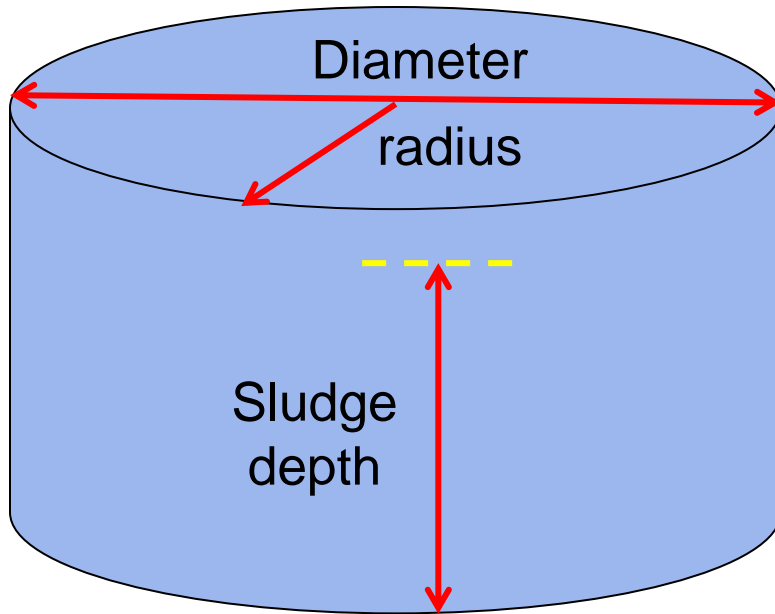
Diameter = 100 ft

Sludge depth = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3$$

$$157,000 \text{ cubic feet} * \frac{7.48 \text{ gallons}}{1 \text{ cubic foot}}$$

# Volume –Tank Example



What is volume of sludge holding tank in gallons?

Diameter = 100 ft

Height = 20 ft

$$\text{Vol} = 157,000 \text{ ft}^3 * 7.48$$

1,174,360 gallons

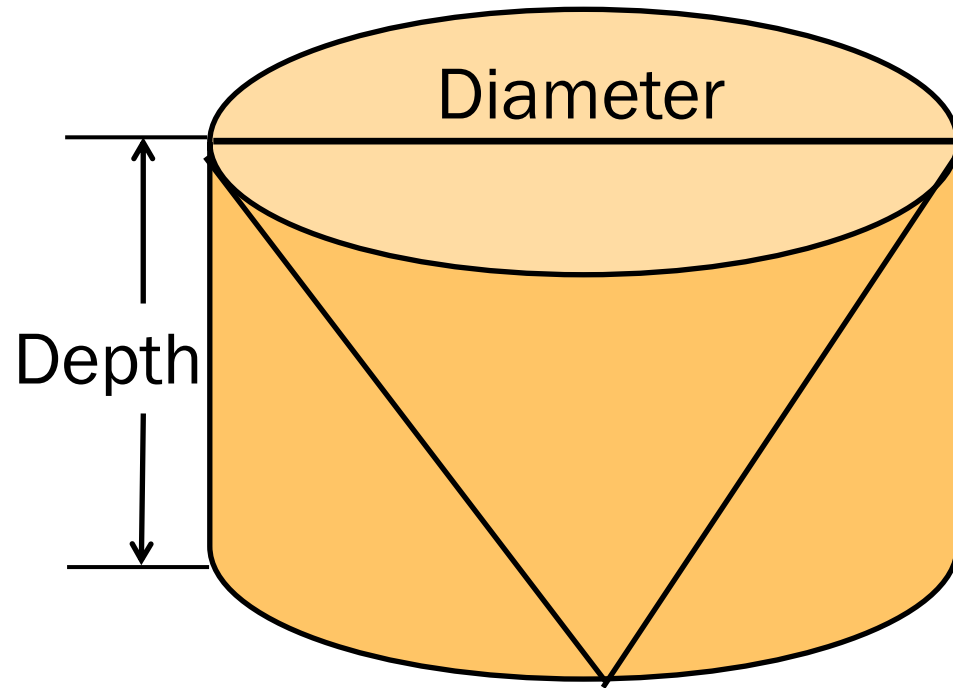
*or*

1.17 MG

Divide by 1,000,000  
and round off

# Volume of a Cone

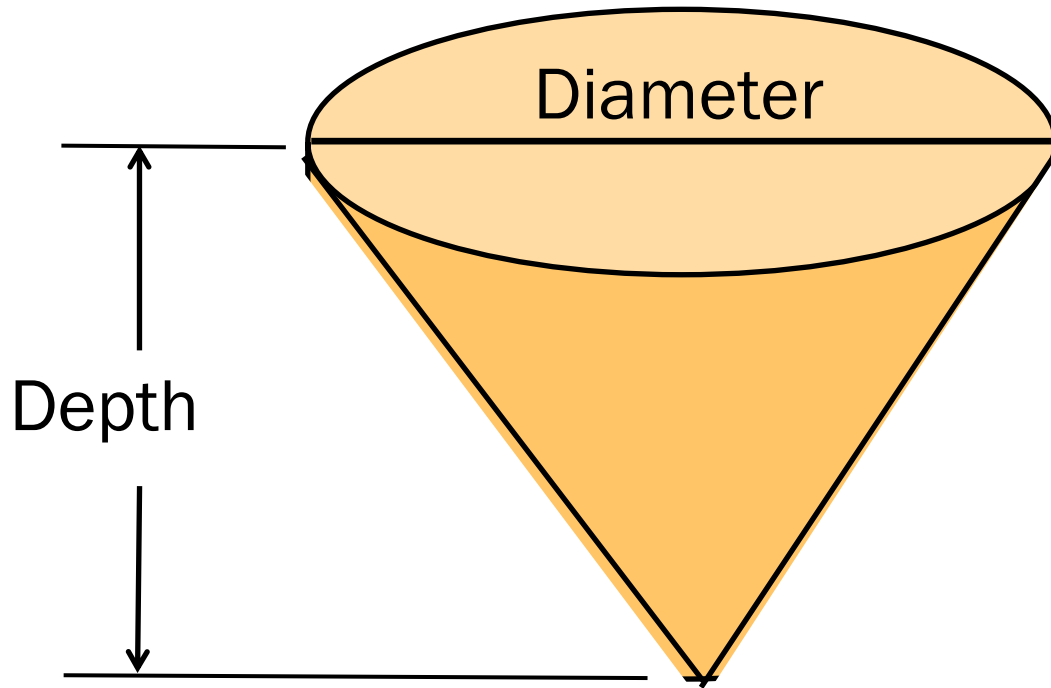
$\frac{1}{3}$  the volume of a cylinder.



## Practical Application



What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?



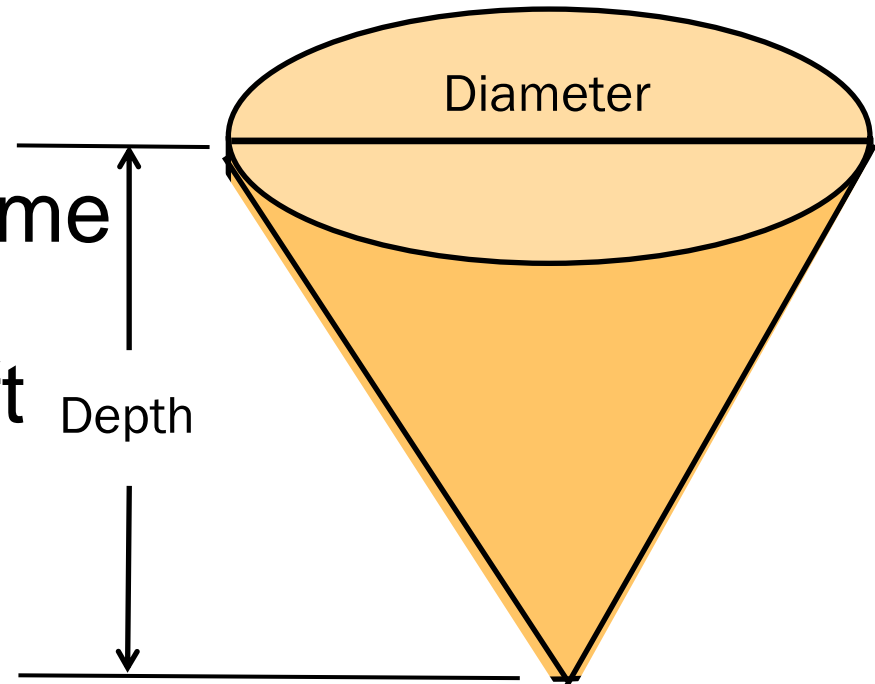
## Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder =  $0.785 * (5\text{ft})^2 * 10\text{ft}$

Cylinder = 196 cu ft



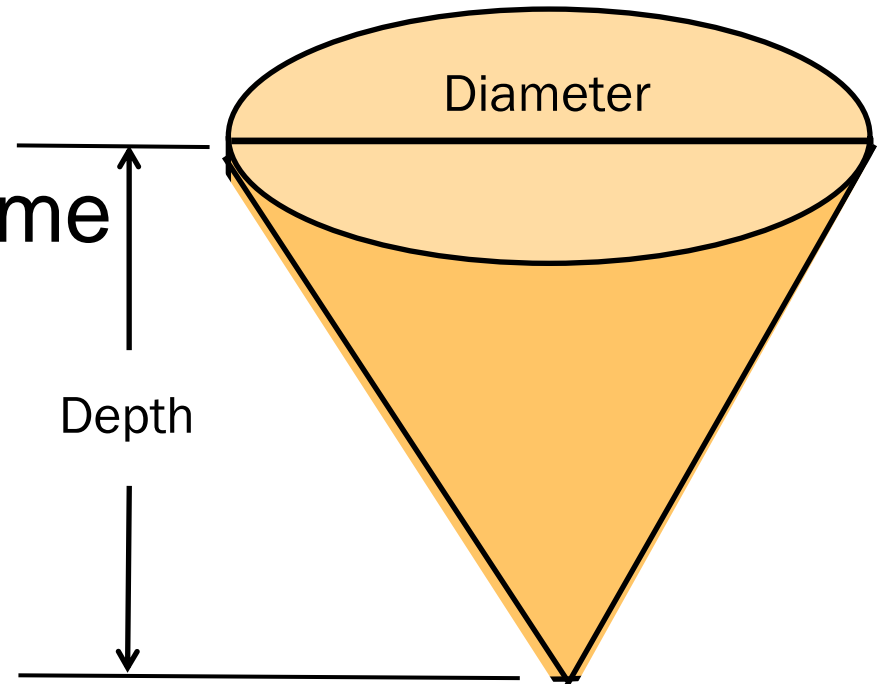
## Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder = 196 cu ft

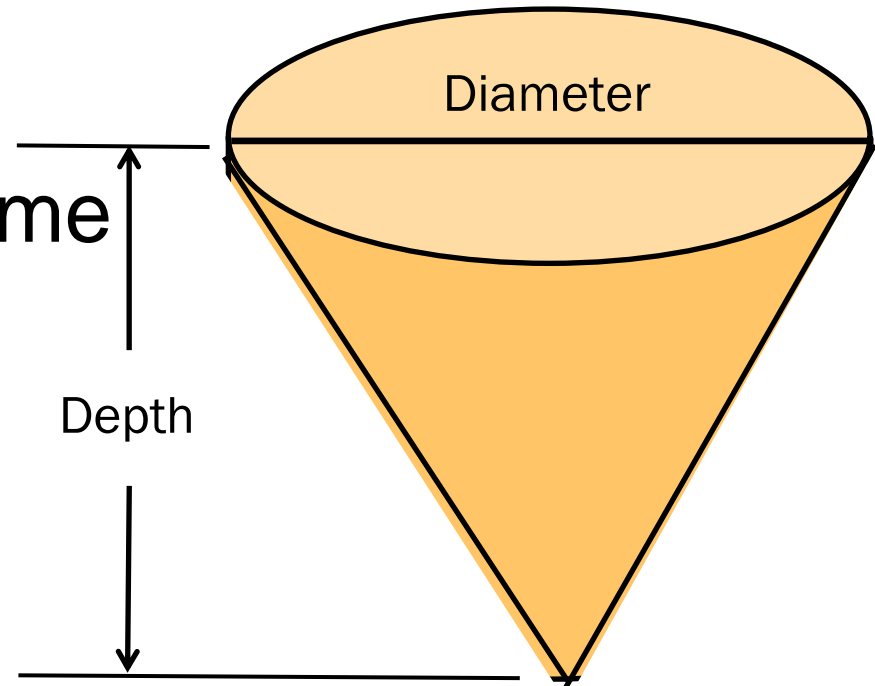
$$\frac{196 \text{ cu ft} * 7.48 \text{ gallons}}{1 \text{ cu ft}}$$





# Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?



Cone =  $\frac{1}{3}$  \* Cylinder Volume

Tank = 196 cu ft

$$\frac{196 \cancel{\text{ cu ft}} * 7.48 \text{ gallons}}{1 \cancel{\text{ cu ft}}}$$

Cylinder = 1,466 gallons

## Practical Application

What is the water volume (gallons) of the grit chamber if it is 10 feet deep with a diameter of 5 feet?

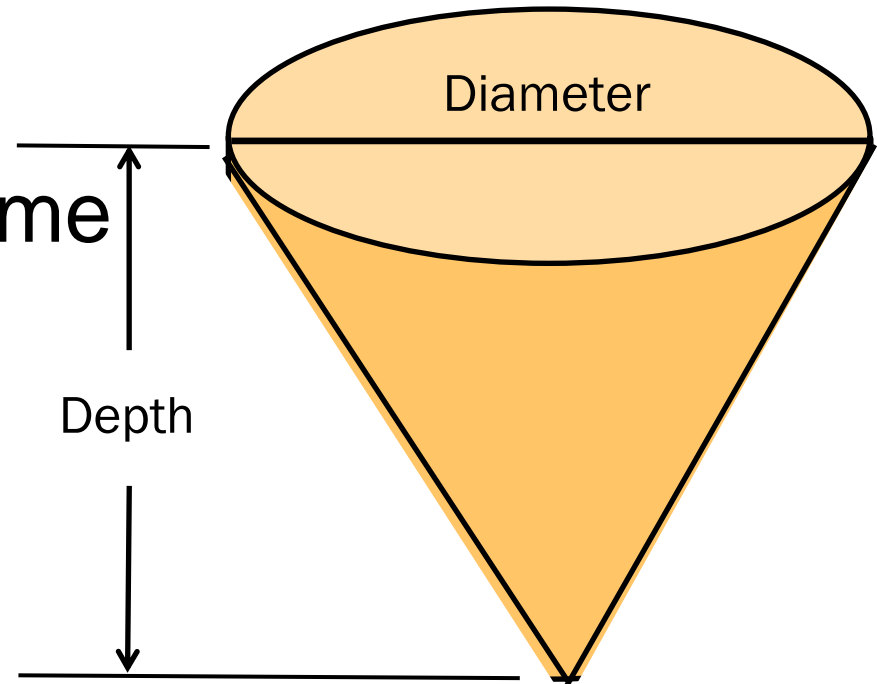
Cone =  $\frac{1}{3}$  \* Cylinder Volume

Cylinder = 196 cu ft

Cylinder = 1466 gallons

Cone =  $\frac{1}{3}$  \* 1466 gal

Cone = 489 gal

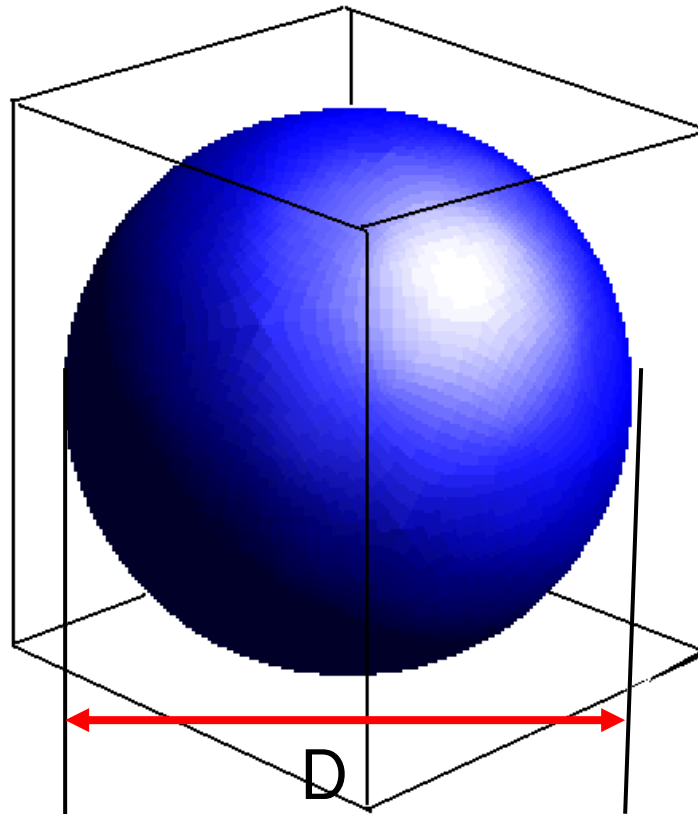


# Practical Application – What About Rounding?

- Tank 1,174,360 gallons or 1.17 MG
  - 1.2 MG “nominal”
- Cone 489 gallons
  - 500 “nominal” gallons
- It all depends on the use

# Volume of a Sphere

3/4 the volume of a cube with the same dimensions



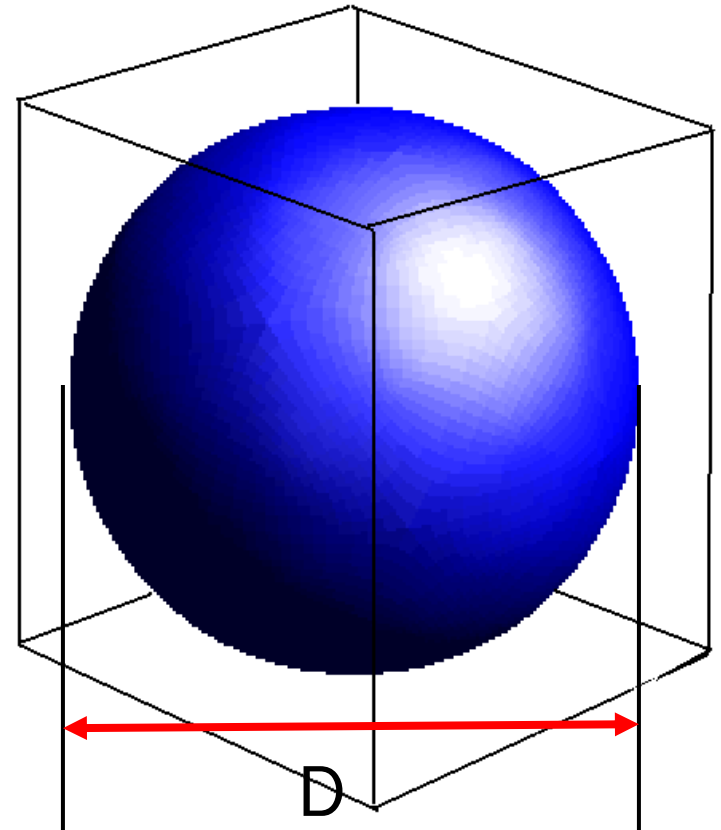
## Practical Application – Sphere Volume

What is the volume of the gas holding sphere if the diameter is 50 feet?

Sphere volume =  
 $\frac{3}{4}$  \* cube volume

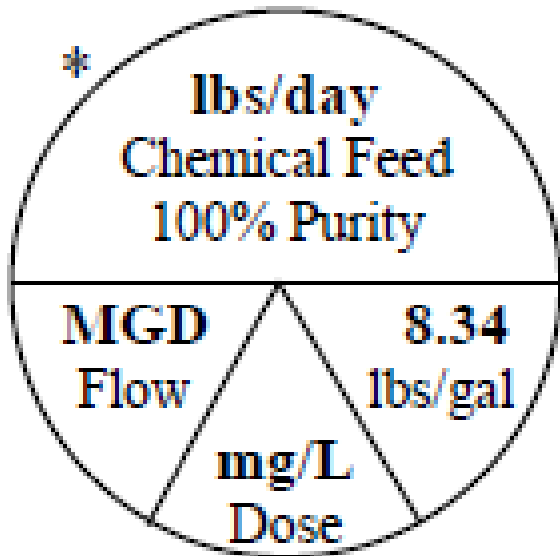
$$\begin{aligned}\text{Volume} &= \\ \frac{3}{4} * 50 \text{ ft} * 50 \text{ ft} * 50 \text{ ft} \\ &= 0.75 * 50^3 \text{ ft}\end{aligned}$$

Volume = 93,750 cubic feet



# Calculation Wheels – Refer to ABC Handout

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



YouTube Links:

<https://www.youtube.com/watch?v=FIH0pkvmuPA>

*Can also be used without rate or flow*  
Feed in pounds, Volume in MG

Formulas or Davidson Pie Wheels  
(Better than a potentially scary formula)

Formulas: **What is the area of a rectangle?**  
Area of Rectangle = Length x Width

2 in

8 in

Area of Rectangle  
16 in<sup>2</sup>

Length (in) 8 in

Width (in) 2 in

Davidson Pie Wheels

1. Draw a circle,
2. Cut it in half with a horizontal line
3. Draw a line(s) from the center of the horizontal line down to the bottom of the circle

• The number in the top half of the circle should equal the product of the numbers in the bottom half of the circle.

# Time Out - Percentages

If something is 56%, what is the mathematical (decimal) way to show that number?

$$56\% = ?$$

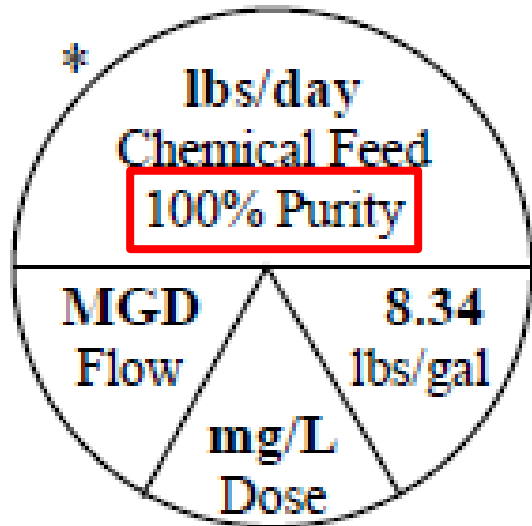
# Time Out - Percentages

If something is 56%, what is mathematical (decimal) way to show number?

$$56\% = \frac{56}{100} = 0.56$$



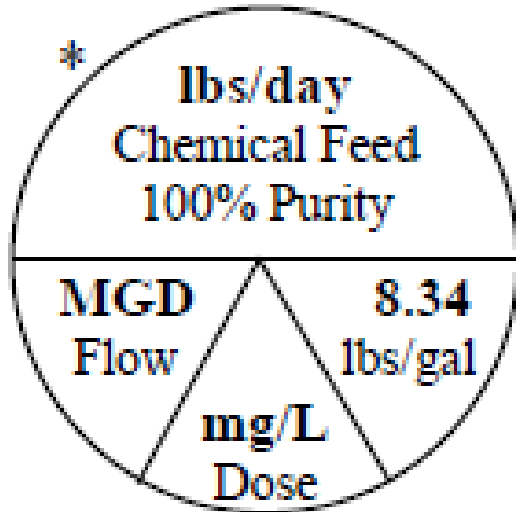
# Back to the Calculation Wheels



$$\text{Feed lbs/day} = \frac{\text{Flow MGD} * \text{Dose mg/l} * 8.34 \text{ lbs/gal}}{\text{Purity decimal percentage}}$$

*This is where that algebra stuff comes into play*

# Back to the Calculation Wheels



What if you know feed, but not flow?

Feed lbs/day

Flow MGD \* Dose mg/l \* 8.34 lbs/gal

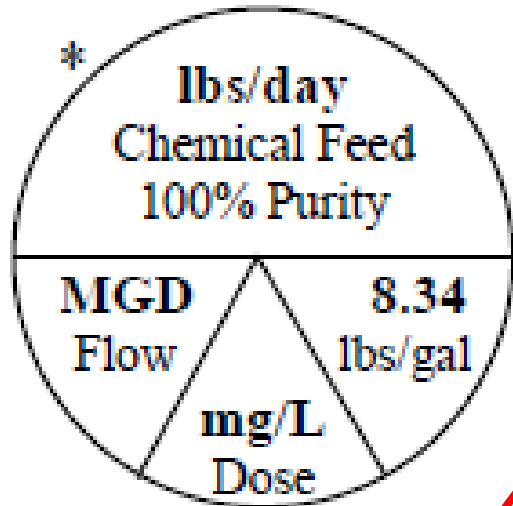
=

Dose mg/l \* 8.34 lbs/gal

Dose mg/l \* 8.34 lbs/gal

Rearrange the equation to isolate flow on one side

# Back to the Calculation Wheels



Division Line

Feed lbs/day

Flow MGD \* ~~Dose mg/l~~ \* ~~8.34 lbs/gal~~

Dose mg/l \* 8.34 lbs/gal

~~Dose mg/l~~ \* ~~8.34 lbs/gal~~

Make sure the units are correct

# Questions, Comments and Suggestions?



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Operator Worked Problems

*Let's see if any of this stuff sunk in!*

***Set A***

Version1.0 & October 2020



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Segment Outline

## Topics:

- **Area & Volume**
- **Pressure**
- **Flow Rate**
- **Chemical & Process**

# Volume & Area

*How big? How Much?*

## Question V1.1:

How many gallons are in 28.65 acre-feet?

A 9,354,282 gallons

B 9,322,137 gallons

C 9,355,000 gallons

D 9,763,599 gallons



## Question V1.1:

How many gallons are in 28.65 acre-feet?

$$28.65 \text{ ac-ft} \times 43,560 \text{ cf} / \text{ac-ft} = 1,247,994 \text{ cf}$$

$$1,247,994 \text{ cf} \times 7.48 \text{ gallons} / \text{cf} = 9,334,995 \text{ gal}$$

C ~9,355,000 gallons

## Question V1.2:

A trench that averages 4.2 ft wide and 5.4 ft in depth is dug for the purpose of installing a 24-in. diameter pipeline. If the trench is 1,287 ft long, how much soil in cubic feet will be put in the trench after the pipe is in place, assuming that the only soil left over is that which the pipe now occupies?

A 1,300 cu ft

B 4,000 cu ft

C 25,000 cu ft

D 29,000 cu ft

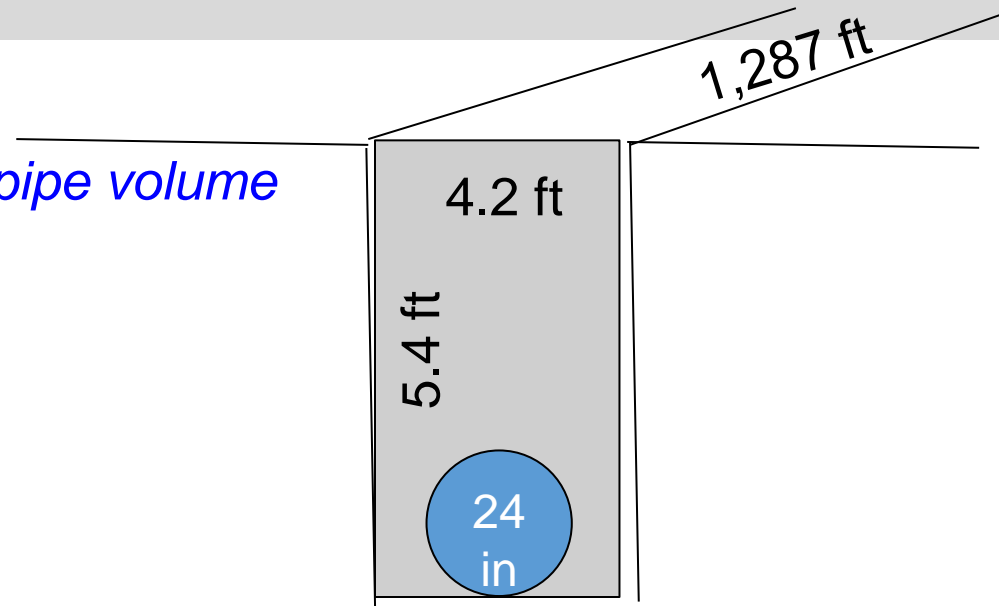
## Question V1.2:

A trench that averages 4.2 ft wide and 5.4 ft in depth is dug for the purpose of installing a 24-in. diameter pipeline. If the trench is 1,287 ft long, how much soil in cubic feet will be put in the trench after the pipe is in place, assuming that the only soil left over is that which the pipe now occupies?

*Soil volume = trench volume – pipe volume*

$$\begin{aligned}\text{Area of trench} &= w \times d \\ &= 4.2 \text{ ft} \times 5.4 \text{ ft} \\ &= 22.7 \text{ sq ft}\end{aligned}$$

$$\begin{aligned}\text{Area of pipe} &= .785 d^2 \\ &= 0.785 \times (24 \text{ in}/12 \text{ in/ft})^2 \\ &= 3.14 \text{ sq ft}\end{aligned}$$



## Question V1.2:

A trench that averages 4.2 ft wide and 5.4 ft in depth is dug for the purpose of installing a 24-in. diameter pipeline. If the trench is 1,287 ft long, how much soil in cubic feet will be put in the trench after the pipe is in place, assuming that the only soil left over is that which the pipe now occupies?

*Area of backfill = trench area – pipe area*

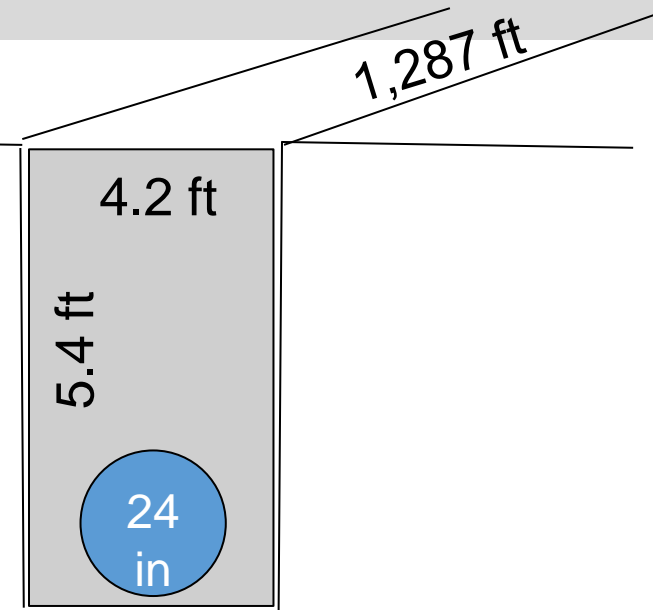
$$\begin{aligned} &= 22.7 \text{ sq ft} - 3.14 \text{ sq ft} \\ &= 19.56 \text{ sq ft} \end{aligned}$$

*Area x length = Volume*

$$\begin{aligned} \text{Volume} &= 19.56 \text{ sq feet} \times 1,287 \text{ ft} \\ &= 25,173 \text{ cu.ft. or CF} \end{aligned}$$

**~25,000 cu ft**

*Assumes excavation is used as pipe bedding!*



*Soil volume typically expressed as cubic yards. 9 CF = 1 CY  
25,173 CF / 9 CF / CY = 2,797 CY*

## Question V1.3:

How many gallons are in a pipe that is 18-inches in diameter and 1,165 ft long



- A 2,060 gallons
- B 10,300 gallons
- C 15,400 gallons
- D 17,200 gallons

## Question V1.3:

How many gallons are in a pipe that is 18-inches in diameter and 1,165 ft long

$$18 \text{ inches} / 12 \text{ inches/ft} = 1.5 \text{ ft}$$

$$1.5^2 \times \text{Pi} / 4 = 1.767 \text{ sf}$$

$$1.767 \text{ sf} \times 1,165 \text{ ft} = 2,058.7 \text{ cf}$$

$$2,058.7 \text{ cf} \times 7.48 \text{ gallons/cf} = 15,399.2 \text{ gal.}$$

**C** ~15,400 gallons

## Question V1.4:

A process chemical tank is 4 ft inside diameter and 10 ft tall. The level is measured in % with 0 being empty and 100% 1 ft below the rim. The tank is refilled anytime the level drops below 20%. If the level is 18.5% how many gallons to refill to 100%?

A 940 gallons

B 690 gallons

C 850 gallons

D 92.2 gallons

## Question V1.4:

A process chemical tank is 4 ft inside diameter and 10 ft tall. The level is measured in % with 0 being empty and 100% 1 ft below the rim. The tank is refilled anytime the level drops below 20%. If the level is 18.5% how many gallons to refill to 100%?

$$\text{Useable depth} = 10\text{ft} - 1\text{ft} = 9\text{ ft}$$

$$\text{Volume/ft} = 4\text{ft}^2 \times \text{Pi} / 4 \times 7.48 \text{ gal/ft}^3 = 94 \text{ gal/ft}$$

$$\text{Full tank volume} = 94 \text{ gal/ft} \times 9 \text{ ft} = 846 \text{ gallons}$$

$$846 \text{ gallons} \times 0.815\% = 689.5$$

D ~690 gallons

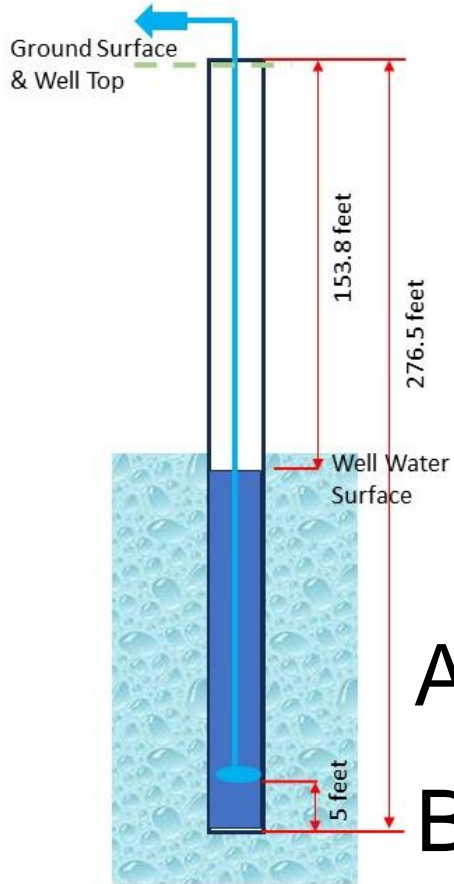


# Pressure

*Can you handle the pressure?*

## Question P1.1:

A well has a depth of 276.5 ft. If the water depth is 153.8 ft., what is the pressure in psi, 5 feet above the bottom (disregard atmospheric pressure)?



A 42 psi

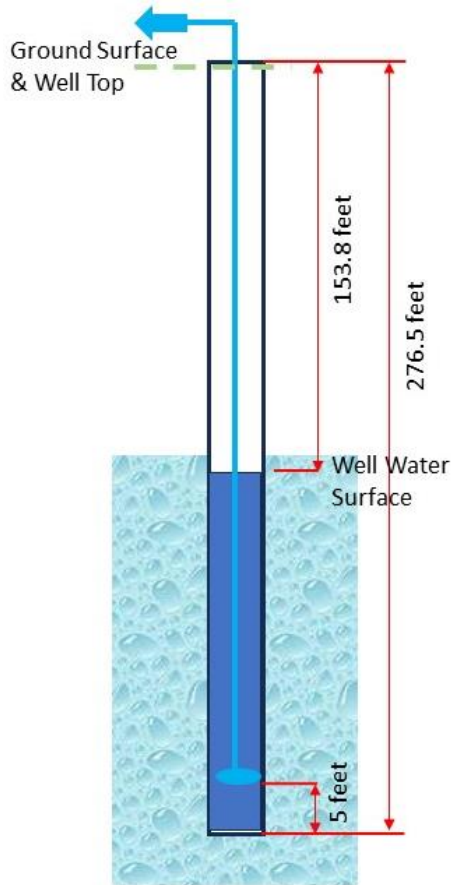
B 46 psi

C 48 psi

D 51 psi

## Question P1.1:

A well has a depth of 276.5 ft. If the water depth is 153.8 ft. below grade, what is the pressure in psi 5 feet above the bottom of the well (disregard atmospheric pressure)?



$$276.5 \text{ ft} - 153.8 \text{ ft} = 122.7 \text{ ft depth of water}$$

$$122.7 \text{ ft} - 5.0 \text{ ft} = 117.7 \text{ ft}$$

$$117.7 \text{ ft} / 2.3104 \text{ ft} / \text{psi} = 50.944$$

**D** ~51 psi

## Question: P1.2

Your utility wants to build a new elevated tank (ground elev. 100) to serve a new large development (elev. 84). What is the minimum WS if the pressure at the edge of the zone is to be 65 psi and the average head loss between the tank and the end of the zone is 12 ft at design flow?

A 153.0 ft

B 145.0 ft

C 238.4 ft

D 230.4 ft

Graphic from Alabama  
News Center

## Question: P1.2

Water tank minimum water surface

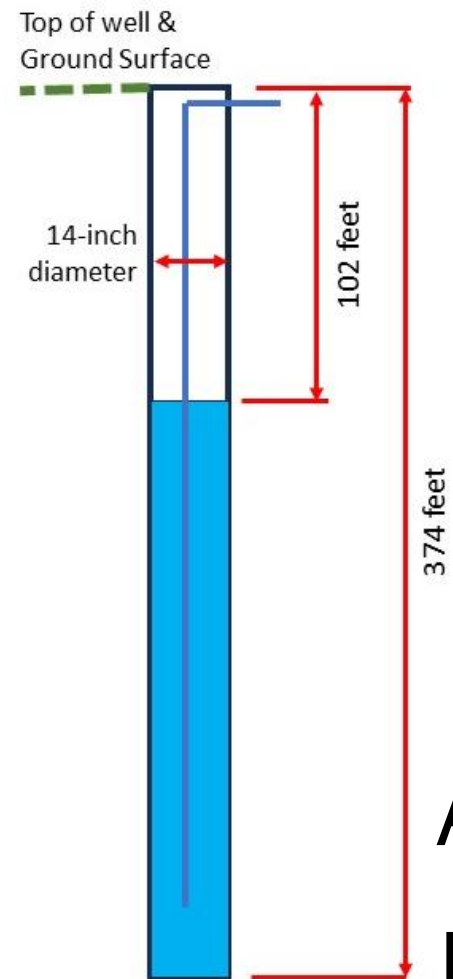
Change pressure from psi to feet

$$65 \text{ psi} * 2.314 \text{ ft} / \text{psi} = 150.4 \text{ ft}$$

Start at the end and work to the tank

$$84 \text{ ft} + 16 \text{ ft (delta elev.)} - 12 \text{ ft (hl)} + 150.4 \text{ ft (system pressure)} = 238.4 \text{ ft}$$

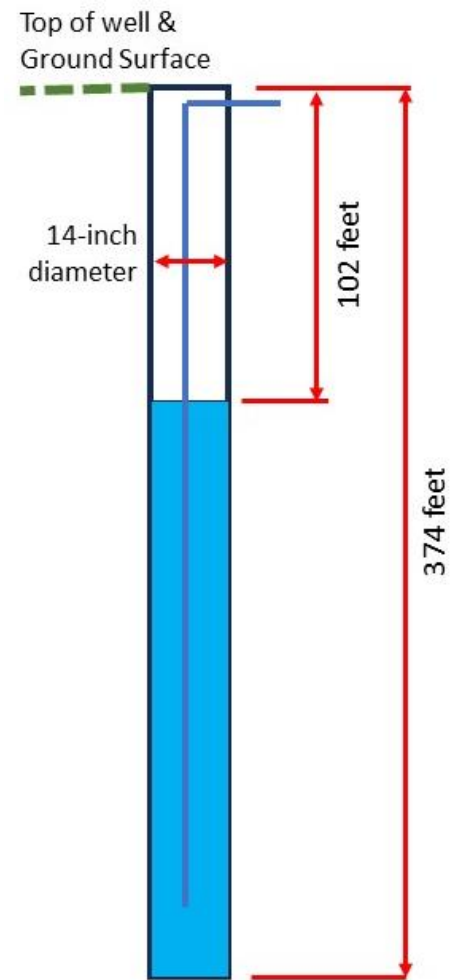
**C 238.4 ft**



## Question P1.3:

A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many pounds of calcium hypochlorite (65% available chlorine) are required?

- A 0.9 lb
- B 1.4 lb
- C 10.5 lb
- D 44.6 lb



## Question P1.3:

A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many pounds of calcium hypochlorite (65% available chlorine) are required?

*First calculate the volume of water in the well, in gallons*

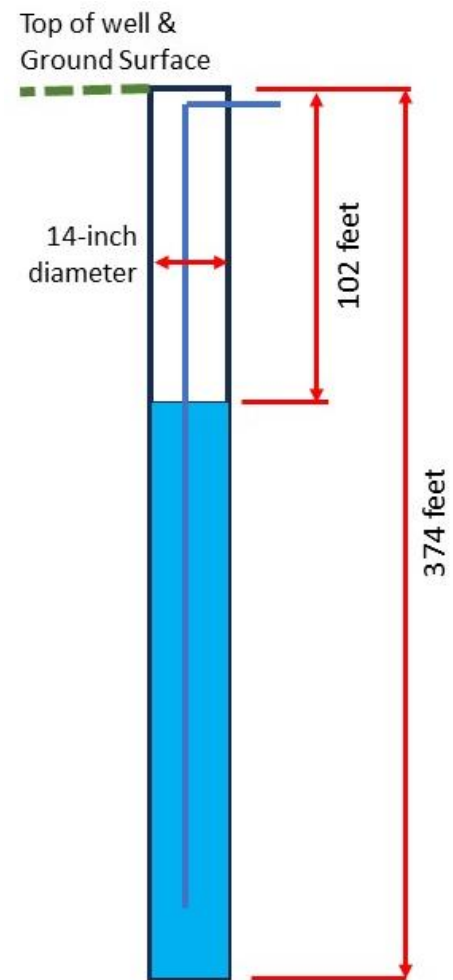
Water volume = X-sectional area x depth

*Step 1 – well casing x-section area*

$$\text{X-section area} = (0.785 \times \text{dia}^2)$$

$$\text{X-section area} = (0.785 \times (14 \text{ in.} / 12 \text{ in./ft.})^2)$$

$$\text{X-section area} = 0.785 \times 1.167 \text{ ft.}^2 = \underline{\underline{1.07 \text{ sq. ft}}}$$



## Question P1.3:

A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many pounds of calcium hypochlorite (65% available chlorine) are required?

*Step 2 – depth of the water in the well*

Water depth = 374 ft - 102 ft.

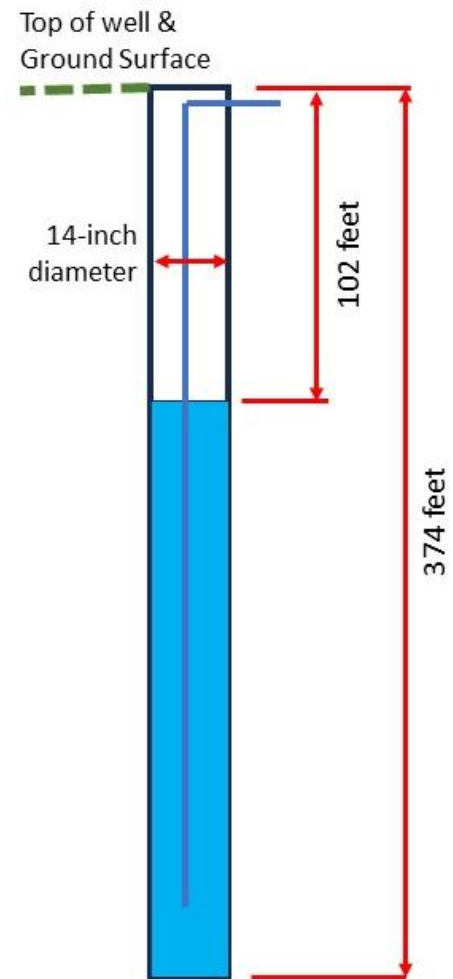
Water depth = **272 ft.**

*Step 3 – Water volume in cu. ft.*

X-section area x depth = 1.07 sq. ft x 272 ft

Water volume = **290 cu ft. or ft.<sup>3</sup>**





## Question P1.3:

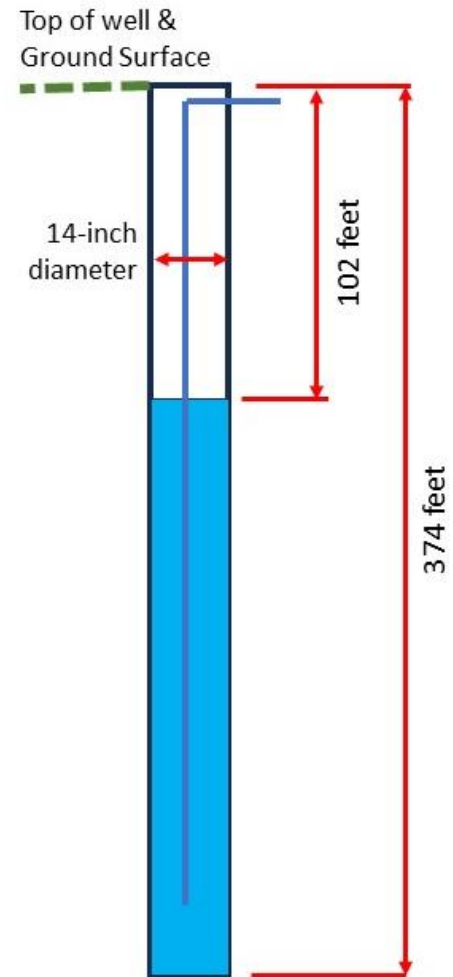
A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many pounds of calcium hypochlorite (65% available chlorine) are required?

*Step 4 – calculate volume in gallons*

$$290 \text{ cu. ft.} \times 7.48 \text{ gal. / cu. ft.} = \underline{\underline{2,174 \text{ gal.}}}$$

*Step 5 - change gallons to million gallons*

$$2,174 \text{ gallons} / 1,000,000 \text{ gal} = \underline{\underline{0.002174 \text{ MG}}}$$



## Question P1.3:

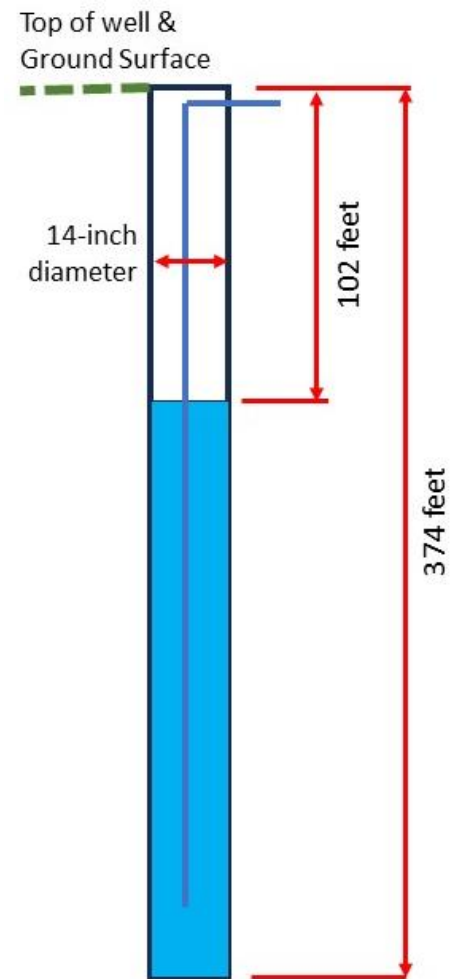
A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many **pounds** of calcium hypochlorite (65% available chlorine) are required?

*Step 6 - calculate the dose of calcium hypochlorite required*

**Pounds CL = Dose x Volume x 8.34 / % purity**

*Dose is in mg/l, Volume is in MG – do we have some unit issues to work out?*

Not in this case – mg/l is parts per million, pounds per MG x unit weight of water provides the same ppm comparison



## Question P1.3:

A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many **pounds** of calcium hypochlorite (65% available chlorine) are required?

*Step 6 – continued*

Pounds CL = Dose x Volume x 8.34 / % purity

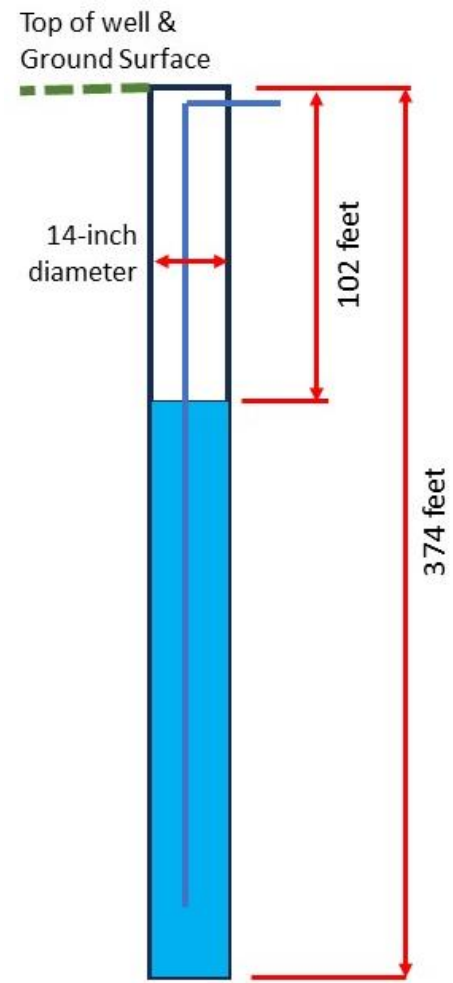
Pounds CL =  $\frac{(50 \text{ ppm} \times 0.00274 \text{ MG} \times 8.34 \text{ lb./gal.})}{65\%}$

Dimensionless

$$\frac{\text{Parts} \times \cancel{\text{million}} \cancel{\text{gallons}} \times \text{lbs} \times 1}{\cancel{\text{million}} \quad \quad \quad \cancel{\text{gallons}} \quad \quad \quad 0.65}$$

Dimensionless

Pounds CL = 1.39 pound



## Question P1.3:

A well that is 374 ft in depth and 14 in. in diameter requires disinfection. Depth to water from top of casing is 102 ft. If the desired dose is 50 mg/L, how many pounds of calcium hypochlorite (65% available chlorine) are required?

3 1.4 lb

# Flow Rate

*How much & how fast?*

## Question Q1.1:

The level in a storage tank rises 3.1 ft. in 4.5 hours. If the tank has a diameter of 225 ft. and the plant is producing 32.4 mgd, what is the average discharge rate of the treated water discharge pumps in gallons per minute?

A 3,408 gpm

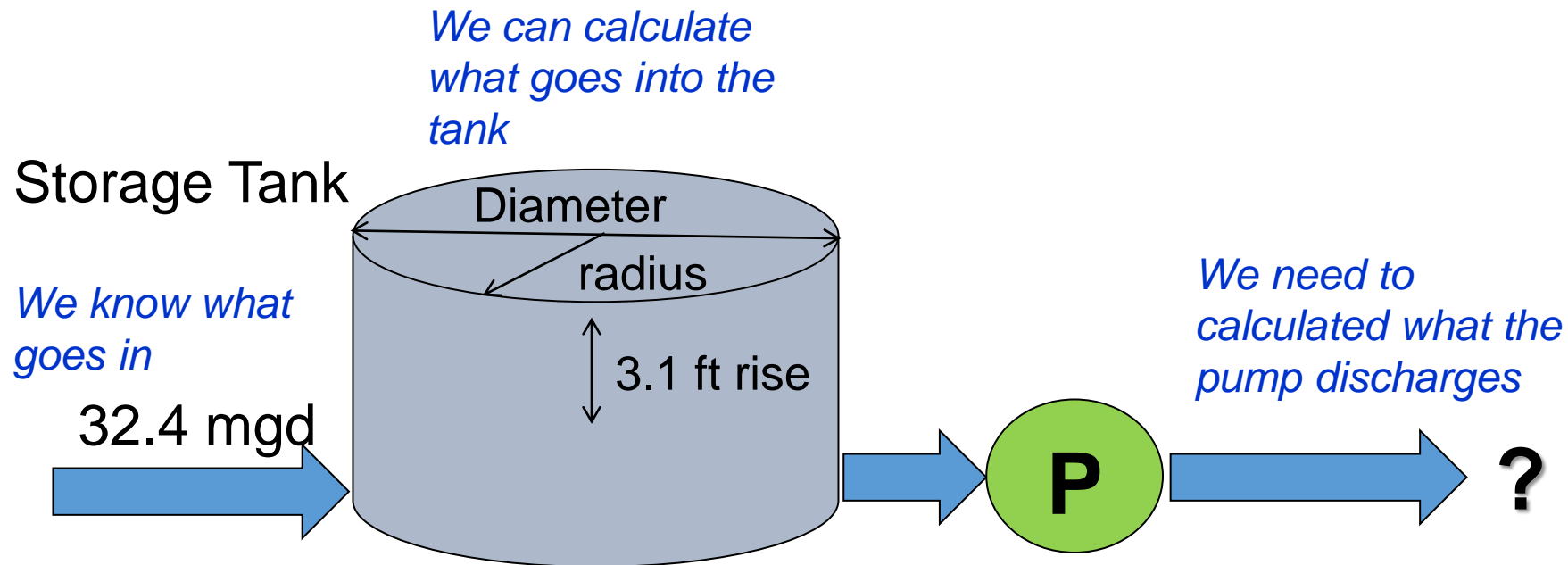
B 15,336 gpm

C 19,088 gpm

D 22,518 gpm

## Question Q1.1:

The level in a storage tank rises 3.1 ft. in 4.5 hours. If the tank has a diameter of 225 ft. and the plant is producing 32.4 mgd, what is the average discharge rate of the treated water discharge pumps in gallons per minute?



# Question Q1.1:

Solve for Discharge Pumping Rate:

*First determine storage used*

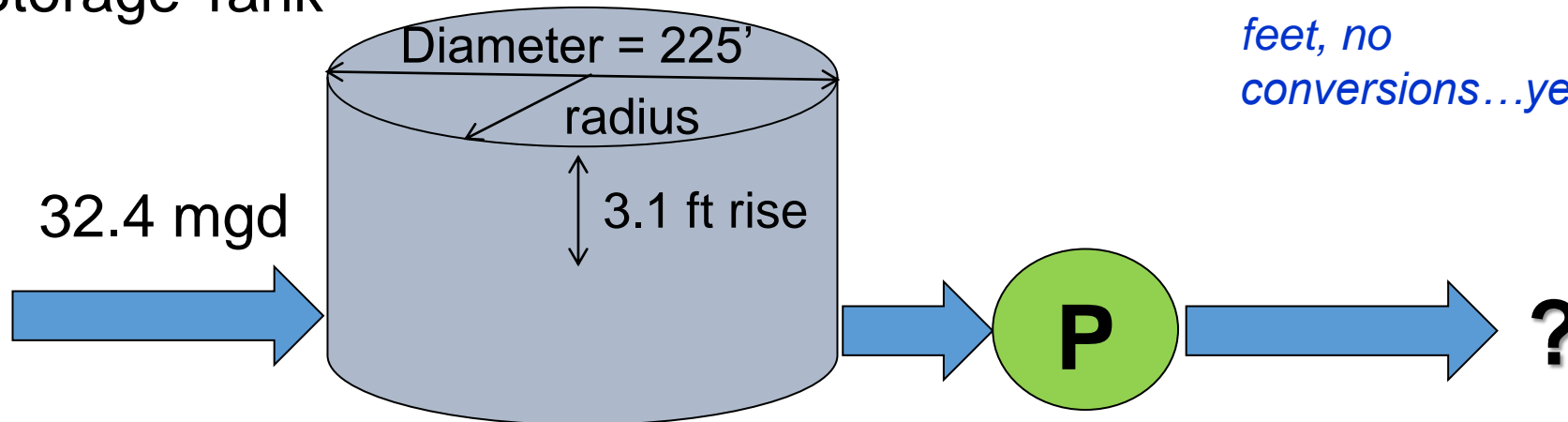
Storage = volume of rise

Storage =  $0.785 \times (\text{dia})^2 \times \text{height of rise}$

$$\begin{aligned} \text{Storage} &= 0.785 \times (225\text{ft})^2 \times 3.1 \text{ ft} \\ &= 123,195 \text{ cu.ft} \end{aligned}$$

*Consistent units of feet, no conversions...yet*

Storage Tank





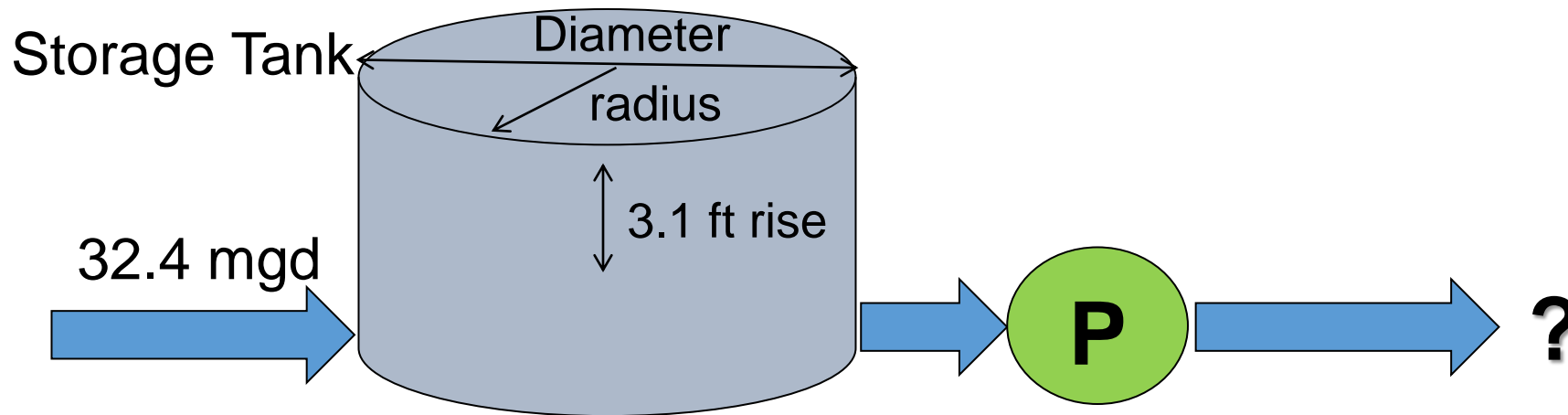
# Question Q1.1:

## Solve for Discharge Pumping Rate:

*Now convert storage in cubic feet to gallons*

$$123,195 \text{ cu.ft} \times 7.48 \text{ gal/cu.ft}$$

$$123,195 \text{ cu.ft.} \times 7.48 \text{ gal/cu.ft.} = 921,498 \text{ gal}$$

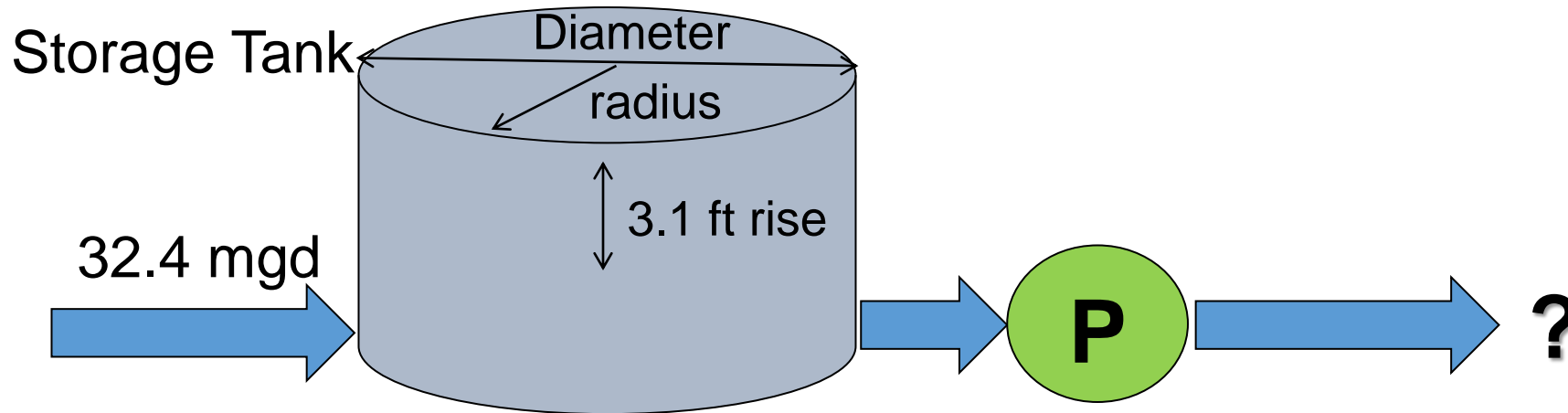


# Question Q1.1:

## Solve for Discharge Pumping Rate:

*Calculate gallons per minute from daily flow*

$$\frac{32.4 \text{ mg}}{\text{day}} \times 1,000,000 \frac{\text{gal}}{\text{mg}} \times \frac{\text{day}}{24 \text{ hr}} \times \frac{\text{hr}}{60 \text{ min}}$$



# Question Q1.1:

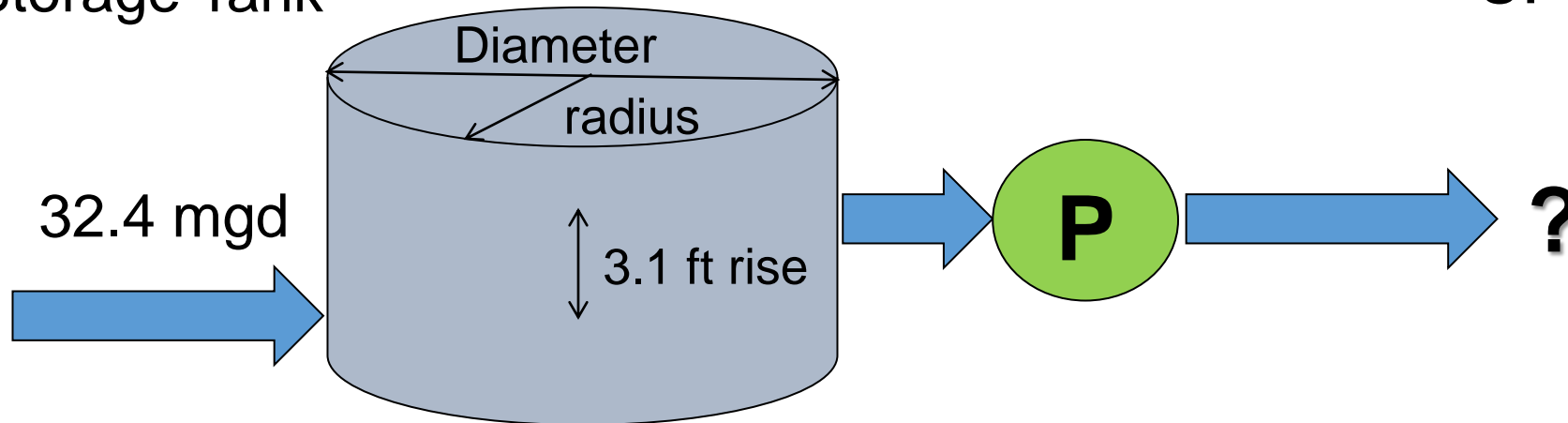
Solve for Discharge Pumping Rate:

*Working through the math and units*

$$\frac{32.4 \text{ mg} \cancel{d} \quad 1,000,000 \text{ gal} \quad \cancel{d} \quad \cancel{\text{hr}}}{\cancel{d} \quad \text{mg} \quad 24 \cancel{\text{hr}} \quad 60 \text{ min}}$$

$$= 22,500 \text{ gpm}$$

Storage Tank



# Question Q1.1:

Solve for Discharge Pumping Rate:

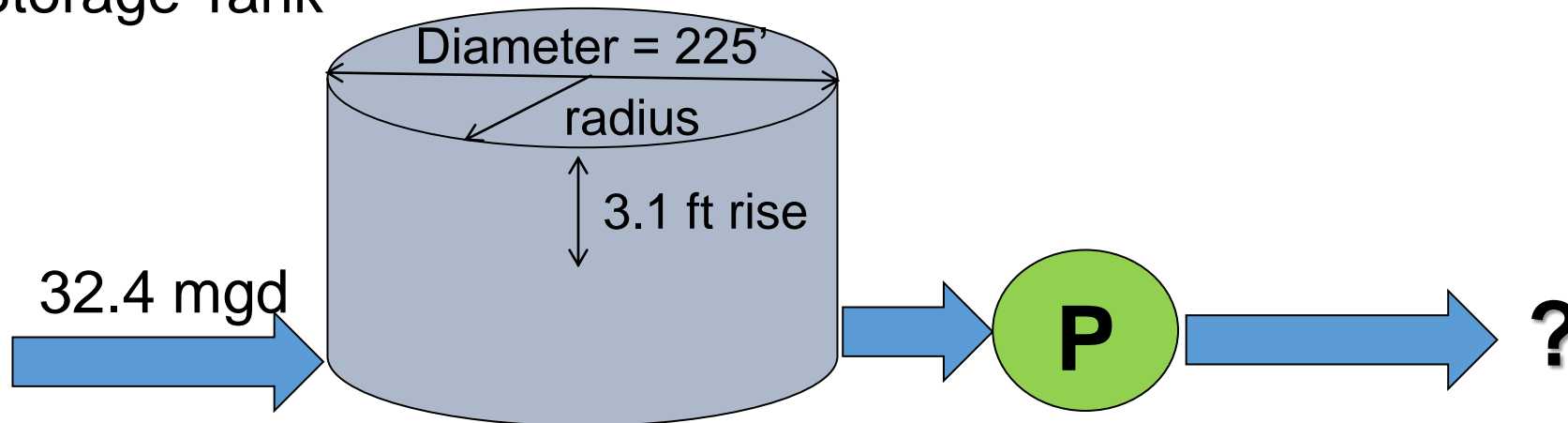
*Determine reservoir inflow or storage rate*

Storage volume = 921,498 gal

Storage rate = storage volume / time

$$\text{Storage rate} = \frac{921,498 \text{ gal}}{4.5 \text{ hr.}} = 204,777 \text{ gal/hr.}$$

Storage Tank



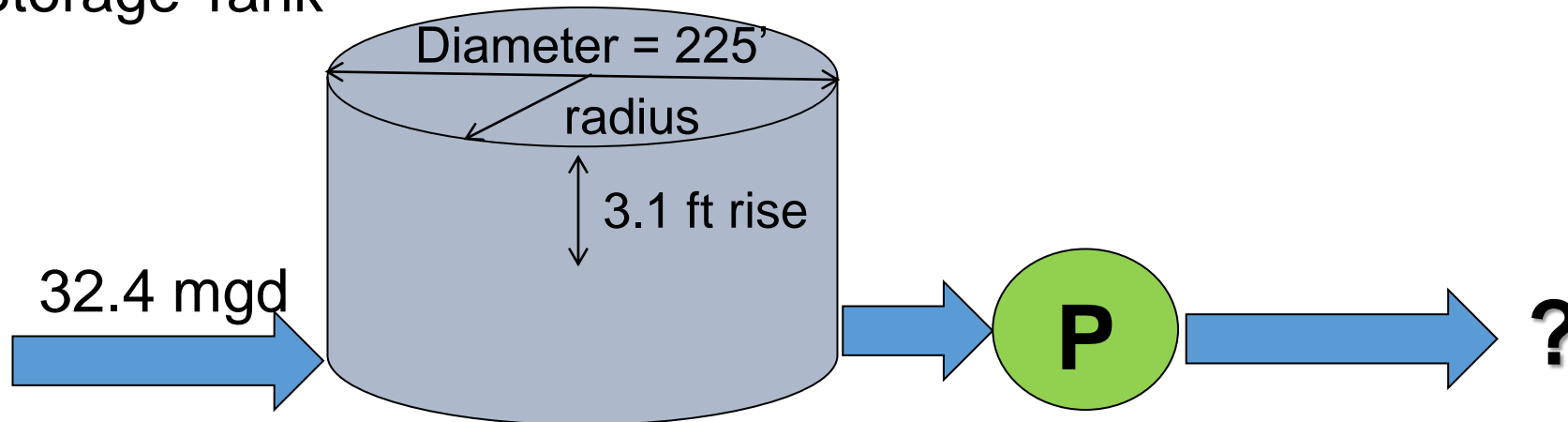
# Question Q1.1:

Solve for Discharge Pumping Rate:

*Convert gallons per hour to gpm*

$$\frac{204,777 \text{ gal}}{\text{hr}} \times \frac{1 \text{ hr}}{60 \text{ min}} = 3,412 \text{ gpm}$$

Storage Tank



# Question Q1.1:

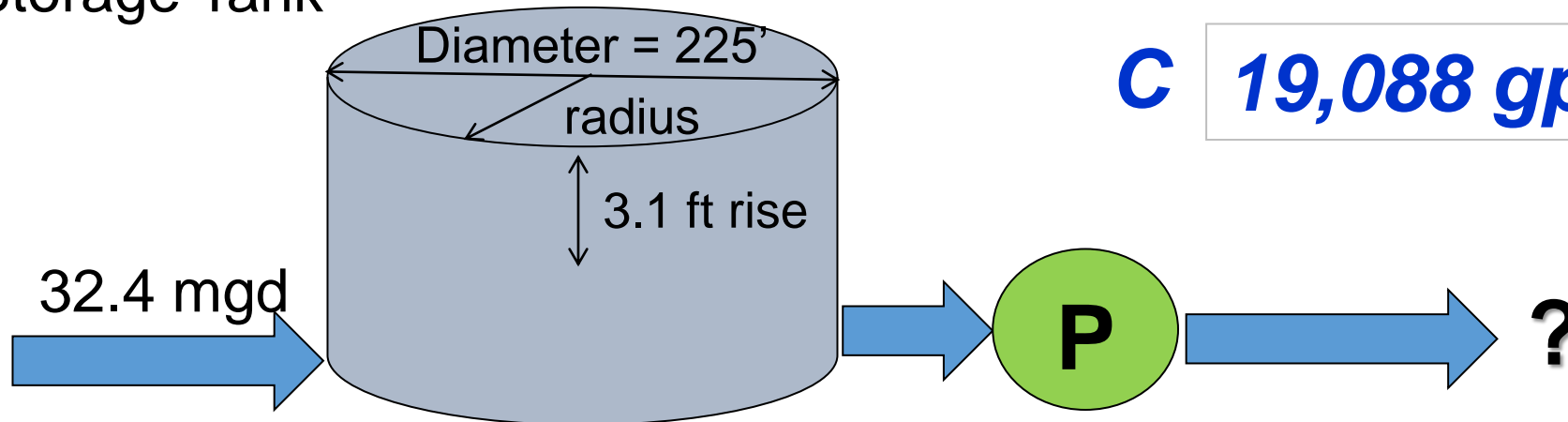
Solve for Discharge Pumping Rate:

Pumping rate = Production minus storage

$$\begin{aligned} \text{Discharge rate} &= 22,500 \text{ gpm} - 3412 \text{ gpm} \\ &= 19,088 \text{ gpm} \end{aligned}$$

*(Same units, no canceling)*

Storage Tank



**C** **19,088 gpm**

## Question Q1.2:

A 6-in. pipeline needs to be flushed. If the desired length of pipeline to be flushed is 316 ft, how many minutes will it take to flush the line at 31 gpm?

A 10 minutes

B 15 minutes

C 30 minutes

D 60 minutes

## Question Q1.2:

A 6-in. pipeline needs to be flushed. If the desired length of pipeline to be flushed is 316 ft, how many minutes will it take to flush the line at 31 gpm?

*First determine the volume of the pipe:*

$$\begin{aligned}\text{Volume of pipeline} &= \text{x-section area} \times \text{length} \\ &= (0.785 \times (6 \text{ in}/12 \text{ in/ft.})^2) \times 316 \text{ feet} = 62 \text{ cu.ft.} \\ &62 \text{ cu.ft.} \times 7.48 \text{ gal/cu.ft.} = 464 \text{ gal.}\end{aligned}$$



## Question Q1.2:

A 6-in. pipeline needs to be flushed. If the desired length of pipeline to be flushed is 316 ft, how many minutes will it take to flush the line at 31 gpm?

*Next determine the time required to flush:*

$$\begin{aligned}\text{Minutes to flush} &= \text{volume of pipe} / \text{flush rate} \\ &= 464 \text{ gal} / 31 \text{ gpm} \\ &= \underline{\underline{15 \text{ min}}}\end{aligned}$$

B 15 minutes

## Question Q1.4:

If a 6-in. force main has a metered flow of 200,000 gpd, what is the velocity of the fluid through the force main?

A 1.6 ft/sec

B 2.5 ft/sec

C 3.1 ft/sec

D 3.9 ft/sec

## Question Q1.4:

If a 6-in. force main has a metered flow of 200,000 gpd, what is the velocity of the fluid through the force main

$$\text{Flow} = \text{Velocity} \times \text{Area}$$

$$\text{Area} = 0.785 \times \text{dia}^2$$

$$\text{Area} = 0.785 \times (6\text{in} / 12\text{in/ft})^2 = 0.196 \text{ sq ft}$$

$$\text{Flow (in cfs)} = 200,000 \text{ gpd}$$

$$24 \text{ hr/day} \times 60 \text{ min/hr} \times 60 \text{ min/sec}$$

$$\text{Flow} = 0.2 \text{ mgd} \times 1.55 \text{ cfs/mgd} = 0.31 \text{ cfs}$$

*(assumes constant flow)*

## Question Q1.4:

If a 6-in. force main has a metered flow of 200,000 gpd, what is the velocity of the fluid through the force main

$$\text{Velocity} = \text{Flow}/\text{Area}$$

– *Rearrange the equation to isolate what you want to calculate*

$$\text{Velocity} = 0.31 \text{ cfs} / 0.196 \text{ sq ft} = \underline{\underline{1.6 \text{ ft/sec}}}$$

A 1.6 ft/sec

## Question Q1.5:

If a pump discharges 10,350 gallons in 3 hours 45 minutes, what is the pump flow rate in gpm?

A 43 gpm

B 44 gpm

C 45 gpm

D 46 gpm

## Question Q1.5:

If a pump discharges 10,350 gallons in 3 hours 45 minutes, what is the pump flow rate in gpm?

$$\begin{aligned}\text{Time in minutes} &= 3 \text{ hr} \times 60 \text{ min/hr} + 45 \\ &\text{min.} = 225 \text{ min.}\end{aligned}$$

$$Q = 10,350 \text{ gal} / 225 \text{ min.} = 46 \text{ gpm}$$

**D** 46 gpm

## Question Q1.6:

A filter has a surface area of 920 sf. What is the filtration rate in gpm/sf if the filter receives a flow of 4,875 gpm?

A 2.4 gpm/sf

B 4.8 gpm/sf

C 5.3 gpm/sf

D 9.2 gpm/sf

## Question Q1.6:

A filter has a surface area of 920 sf. What is the filtration rate in gpm/sf if the filter receives a flow of 4,875 gpm?

$$4,875 \text{ gpm} / 920 \text{ sf} = 5.29891 \text{ gpm/sf}$$

**C ~5.3 gpm/sf**



# Treatment Process & Chemical Dosing

*Tracking the treatment*

## Question T1.1:

A system uses 250 gal of 15% hypochlorite solution each day. The system operator receives a call from his/her chemical supplier saying that the 15% hypochlorite solution will no longer be available but is being replaced with a 10% hypochlorite solution. In order to keep the dosage the same, how much of the 10% solution will the operator need to feed every day?

A 150 gal

C 250 gal

B 375 gal

D 420 gal

## Question T1.1:

A system uses 250 gal of 15% hypochlorite solution each day. The system operator receives a call from his/her chemical supplier saying that the 15% hypochlorite solution will no longer be available but is being replaced with a 10% hypochlorite solution. In order to keep the dosage the same, how much of the 10% solution will the operator need to feed every day?

*First determine the volume of 100% hypo*

$$\text{Dosage of hypo} = 250 \text{ gal} \times 15\%$$

$$\text{Dosage of hypo} = 250 \text{ gal} \times .15 = 37.5 \text{ gal}$$

## Question T1.1:

A system uses 250 gal of 15% hypochlorite solution each day. The system operator receives a call from his/her chemical supplier saying that the 15% hypochlorite solution will no longer be available but is being replaced with a 10% hypochlorite solution. In order to keep the dosage the same, how much of the 10% solution will the operator need to feed every day?

*Next calculate the volume of the new more dilute solution*

Dosage of hypo = 37.5 gal      New solution = 10% hypo

$$\text{New solution} = \frac{37.5 \text{ gal}}{0.10} = 375 \text{ gallons}$$

## Question T1.2:

Determine the specific gravity (SG) of an unknown liquid if the density of the liquid is  $70.9 \text{ lb/ft}^3$

A 1.05 SG

B 1.14 SG

C 1.18 SG

D 1.21 SG

## Question T1.2:

Determine the specific gravity (SG) of an unknown liquid if the density of the liquid is 70.9 lb/ft<sup>3</sup>.

Note - *SG is a ratio & dimensionless*

$$70.9 \text{ lb/ft}^3 / 62.4 \text{ lb/ft}^3 = 1.1362 \text{ SG}$$

B ~1.14 SG

## Question T1.3:

Determine the percentage strength of a solution mixture if 875 lb of a 49.6% strength solution is mixed with 293 lb of a 17.2% solution.

A 41.5%

B 42.4%

C 43%

D 43.1%

## Question T1.3:

Determine the percentage strength of a solution mixture if 875 lb of a 49.6% strength solution is mixed with 293 lb of a 17.2% solution.

$$875 \text{ lb} + 293 \text{ lb} = 1,168 \text{ lb total solution weight}$$

$$((875 \text{ lb} \times 0.496) + (293 \text{ lb} \times 0.172)) / 1,168 \text{ lb} =$$

$$= 0.41472 \times 100 = 41.472\%$$

**A** ~41.5%



## Question T1.4:

An 84 ft diameter tank that's 24.25 ft high at the overflow requires disinfection at a dosage of 50 mg/l. How much 12.5% sodium hypochlorite that weighs 9.59 lb/gallon is required?

A 310 gallons

B 350 gallons

C 380 gallons

D 410 gallons

## Question T1.4:

84 ft diameter tank x 24.25 ft high

Disinfection of 50 mg/l.

12.5% sodium hypochlorite @ 9.59 lb/gallon

$$84^2 \text{ ft}^2 \times \text{Pi} / 4 \times 24.25 \text{ ft} = 134,390 \text{ ft}^3$$

$$134,390 \text{ ft}^3 \times 7.48 \text{ gal/ft}^3 = 1.005 \times 10^6 \text{ gallons}$$

$$50 \text{ mg} / \text{L} / 12.5\% = 400 \text{ mg} / \text{L} \text{ hypo reqd}$$

$$400 \text{ mg/L} \times 10^{-6} \text{ kg/mg} \times 2.2 \text{ lb/kg} = 8.82 \times 10^{-4} \text{ lb/L}$$

$$8.82 \times 10^{-4} \text{ lb/L} \times 3.7854 \text{ L/gal} / 9.59 \text{ lb/gal} =$$

$$3.81 \times 10^6 \text{ L} \times 3.7854 \text{ L/gal} \times 8.82 \times 10^{-4} \text{ lb/L} =$$

**B 350 gallons**

## Question T1.5:

Your group uses 80 units of an item per week. You are required to have a 10 week reserve of the item on hand at all times, and it requires 4 weeks to obtain a new supply. What is the minimum reorder point?

A 320 units

B 800 units

C 1,120 units

D 2,240 units

## Question T1.5:

Your group uses 80 units of an item per week. You are required to have a 10 week reserve of the item on hand at all times, and it requires 4 weeks to obtain a new supply. What is the minimum reorder point?

$$Q_W = 80 \text{ units}$$

$$Q_M = 80 \text{ units} \times 10 \text{ weeks} = 800 \text{ units}$$

$$Q_{ST} = 80 \text{ units} \times 4 \text{ weeks} = 320 \text{ units}$$

$$Q_R = 800 \text{ units} + 320 \text{ units} = 1,120 \text{ units}$$

C 1,120 units

## Question T1.6:

What percentage is 34,411 of 74,818?

A 34.411%

B 45.993%

C 74.818%

D 217.42%

## Question T1.6:

What percentage is 34,411 of 74,818?

$$34,411 / 74,818 = 0.459929$$

$$0.459929 \times 100 = 45.993\%$$

**B** 45.993% ~ **46%**

## Question T1.7:

The iron content of raw water is 1.81 mg/l. What is the % removal if the finished water contains 0.11 mg/l?

A 17%

B 20%

C 60%

D 94%

## Question T1.7:

The iron content of raw water is 1.81 mg/l. What is the % removal if the finished water contains 0.11 mg/l?

$$\text{Iron removed (weight)} = 1.81 \text{ mg/l} - 0.11 \text{ mg/l} = 1.7 \text{ mg/l}$$

$$\text{Iron removed \%} = 1.70 \text{ mg/l} / 1.81 \text{ mg/l} = 0.93923 \text{ (dimensionless ratio)}$$

$$0.93923 \times 100 = 93.926\%$$

**D ~94%**



# Questions were taken from the following: (with some modifications)

*Operator Certification Study Guide* — *A Guide to Preparing for Water Treatment and Distribution Operator Certification Exams*, Fifth Edition. Written by John Giorgi, Prepared by the Association of Boards of Certification. American Water Works Association, 2003

*WEF/ABC Wastewater Operators'* — *Guide to Preparing for the Certification Examination*. Water Environment Federation, 2002

*WEF/ABC Collection Systems Operators'* — *Guide to Preparing for the Certification Examination*. Water Environment Federation, 2002

*OpFlow Certification Corner* — *Monthly publication from AWWA*

# Questions, Comments and Suggestions?



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

# Example Problems

*Let's work through some practical examples*

Version 1.0 & October 2020



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*

## Segment topics:

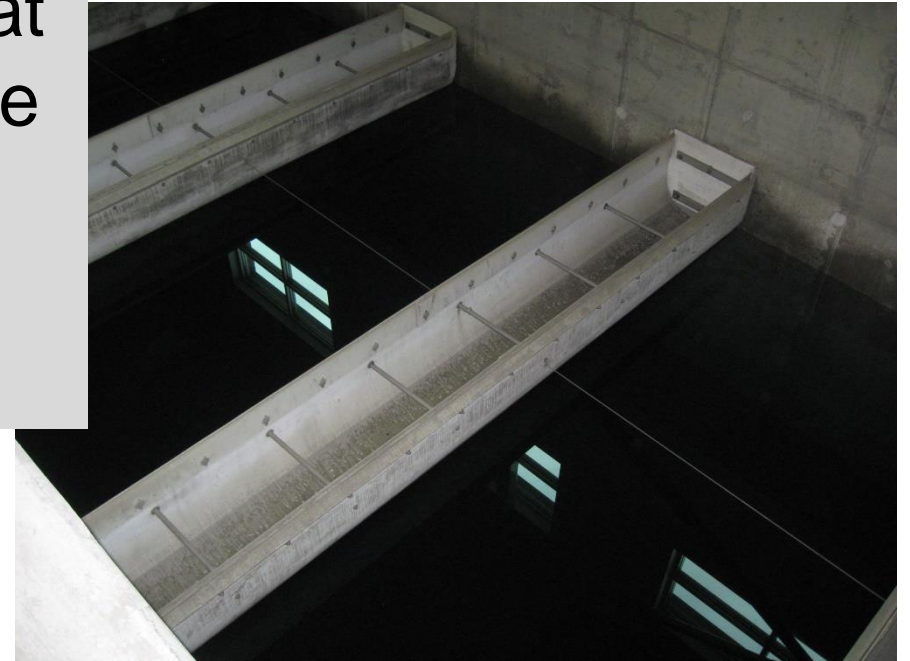
- **Length, area & volumes**
- **Pressure**
- **Rates of flow & velocity**
- **Chemicals & Process**

# Length, Area & Volumes

*Get out your pencils, paper & calculators*

## Question:

Your new WTP will have 8 filter beds and you are planning on 7 being in service at any time. The flow rate is 8 gal/sf/min for clean bed and 6.5 for a bed that is ready for backwashing. If the beds will be close to square, what are the plan dimensions for a capacity of 40.0 mgd?



*Photo from City of  
Lynden, WA*

## Question:

### Filter Area

$$\text{Average capacity} = (8.0 + 6.5)/2 = 7.25 \text{ gal/sf/min}$$

$$7.25 \text{ g/sf/min} \times 60 \text{ min/hr} \times 24 \text{ hr/d} = 10,440 \text{ gal/sf/day}$$

$$10,440 \text{ gal/day} \times (1 \text{ MG} / 1,000,000 \text{ gal}) = 0.010440 \text{ MG/sf/day}$$

$$\text{Area required} = 40.0 \text{ mgd} / 0.01044 \text{ MG/sf/d} = 3,831 \text{ sf}$$

$$\text{Area required / filter bed} = 3,831 \text{ sf} / 7 = 547 \text{ ft}^2 / \text{bay}$$

$$\text{Rough dimensions} = (547 \text{ sf})^{0.5} = 23.4 \text{ ft / side}$$

$$\sim \mathbf{24 \text{ ft} \times 24 \text{ ft} = 576 \text{ sf}} \text{ (multiples of 4 ft wide forms)}$$

$$\text{or } \mathbf{20 \text{ ft} \times 28 \text{ ft} = 560 \text{ sf}} \text{ (multiples of 4 ft wide forms)}$$

## Question:

Your new reservoir is to have a active storage capacity of 1 MG and a pressure range of 25 psi. What is the diameter of the reservoir?



*Graphic from City of  
Troutdale, OR*



## Question:

Tank diameter

$$\text{Height range } 25 \text{ psi} \times 2.31 \text{ ft/psi} = 57.75 \text{ ft}$$

$$\text{Volume } 1,000,000 \text{ gal.} / 7.48 \text{ gal./ft}^3 = 133,690 \text{ ft}^3$$

$$133,690 \text{ ft}^3 / 57.75 \text{ ft} = 2,415 \text{ ft}^2 = \text{tank area}$$

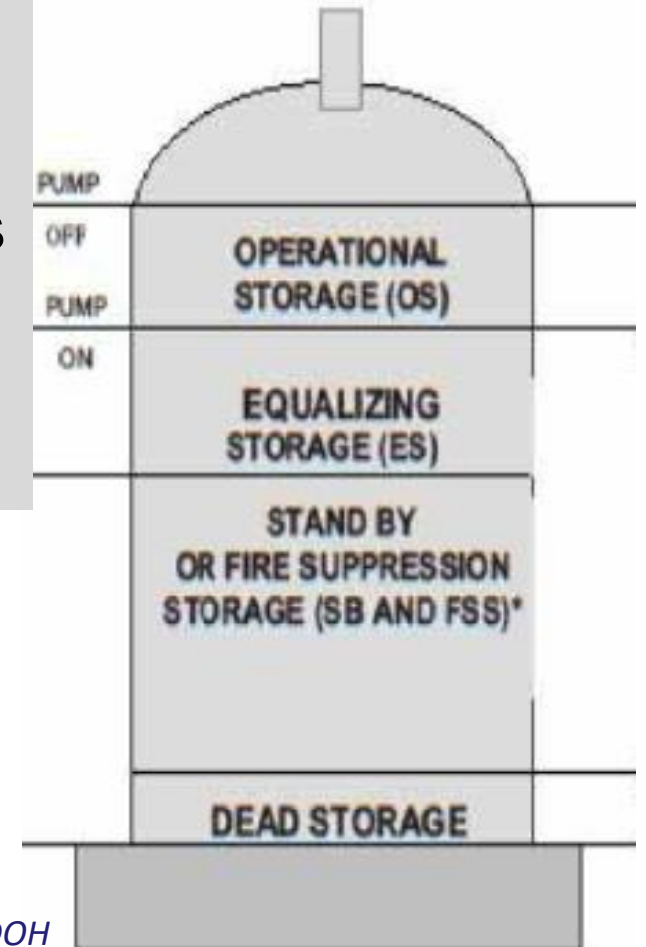
$$\text{Area} = D^2 \times \text{PI} / 4 \quad \text{rearranged } D = (\text{area} * 4 / \text{PI})^{0.5}$$

$$(2,415 * 4 / 3.14159)^{0.5} = 54.29 \text{ ft inside diameter}$$

~55 ft

## Question:

You've been given a screaming good deal for a new water tank but the Canadian contractor wants to do the job in metric units. You need 500,000 gallons of storage (operational + equalizing + standby). The proposed tanks is 12 meters in diameter x 20 meters to the overflow. Is the tank big enough? If yes, what is the volume of the dead storage?



Graphic from WSDOH

## Question:

Is the tank big enough?

$$\text{Area} = 12^2 * 3.14159 / 4 = 113.10 \text{ m}^2$$

$$\text{Volume} = 113.10 \text{ m}^2 * 20 \text{ m} = 2,262 \text{ m}^3$$

$$\text{Volume conversion } 264.172 \text{ gallons} / \text{m}^3$$

$$2,263 \cancel{\text{ m}^3} * 264.172 \text{ gallons} / \cancel{\text{ m}^3}$$

597,543 gallons – **YES** big enough

$$597,543 \text{ gal.} - 500,000 \text{ gal.} = 97,543 \text{ gal excess}$$

## Question:

A lime tank is a cone at the bottom and cylindrical at the top. The cylinder portion is 28 feet tall. The cone has a minimum diameter of 2 feet and is 12 feet tall. What is the volume of the tank in cubic feet to 3 significant figures?



## Question:

A lime tank is a cone at the bottom and cylindrical at the top. The cylinder portion is 28 feet tall. The cone has a minimum diameter of 2 feet and is 12 feet tall. What is the volume of the tank in cubic feet to 3 significant figures?

$$\text{Cylinder volume} = \pi \times d^2 / 4 \times H$$

$$\text{Cone volume} = (d_1^2 + d_2^2) / 2 \times \pi / 4 \times H$$

$$\pi \times 15^2 / 4 \times 28 + (15^2 + 2^2) / 2 \times \pi / 4 \times H$$

$$6,030 \text{ ft}^3$$

# Question:

Convert 16,912,000 liters to acre-feet



*Photo from the Town of Friday Harbor*

## Question:

Convert 16,912,000 liters to acre-feet

Liters → gallons → cubic feet → acre-feet

$$16,912,000 \text{ liters} \times 0.2642 \text{ gal/liter} = 4,468,150 \text{ gal}$$

$$4,468,150 \text{ gallons} / 7.48 \text{ gallons/cf} = 597,346 \text{ cf}$$

$$597,346 \text{ cf} / 43,560 \text{ cf/acre-feet} = 13.7138 \text{ acre-ft}$$

13.7 acre-feet

## Question:

A new section of pipe is 16" in diameter and 550 feet long. How many gallons does the pipe contain? And why do we care?



*Photo from Kana Pipeline, Inc.*



## Question:

A pipe is 16" in diameter and 550 feet long. How many gallons does the pipe contain?

$$1.33 \text{ ft}^2 \times \text{PI} / 4 \times 1 \text{ ft} = 1.39 \text{ ft}^3 / \text{ft}$$

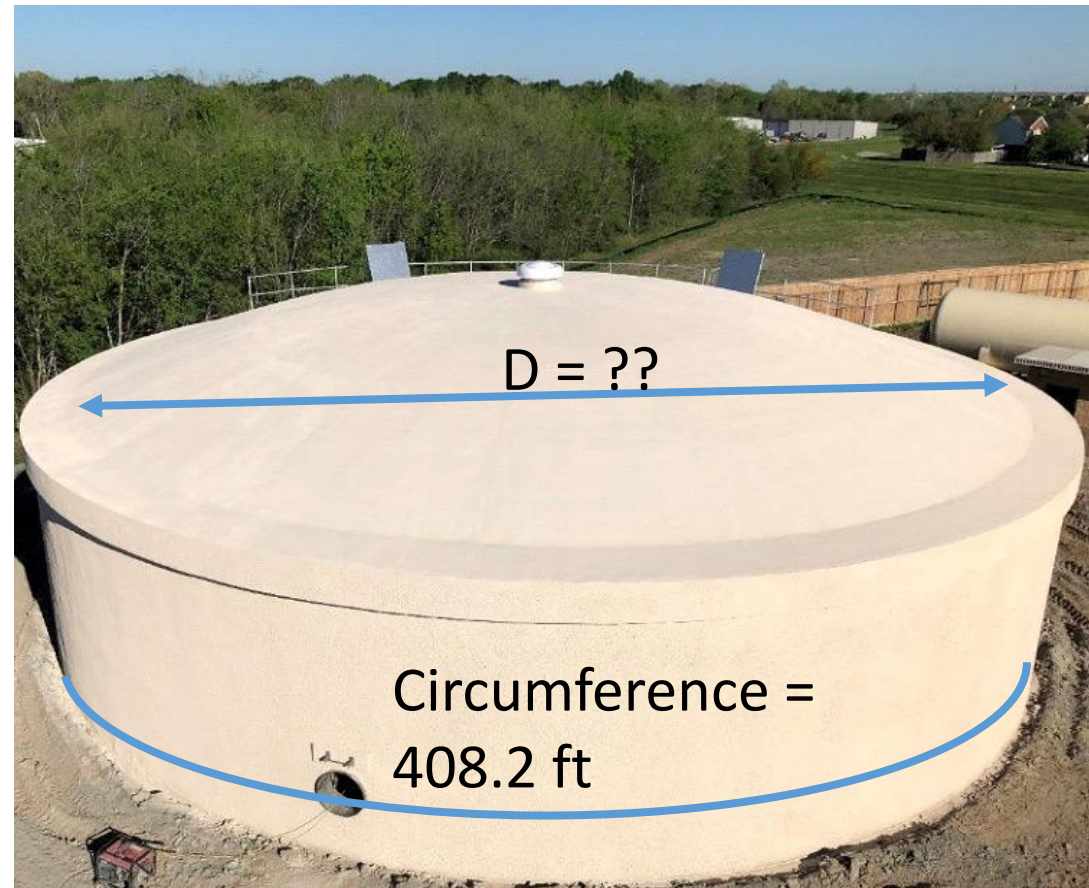
$$1.39 \text{ ft}^3 / \text{ft} \times 550 \text{ ft} = 764.11 \text{ ft}^3$$

$$764.11 \text{ ft}^3 \times 7.48 \text{ gal.} / \text{ft}^3 = 5,715.5 \text{ gallons}$$

5,715.5 gallons – *round off to 5,720 gallons*

## Question:

What is the diameter of a tank with a circumference of 408.2 ft?



*Photo from DN Tanks*

## Question:

What is the diameter of a tank with a circumference of 408.2 ft?

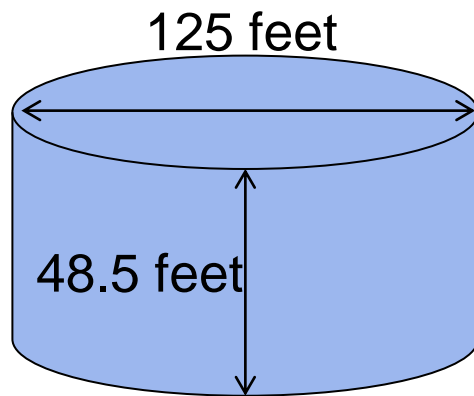
$$408.2 \text{ feet} / \pi = 408.2 \text{ feet} / 3.14159 =$$

$$= 129.93 \text{ feet in diameter}$$

$$\sim 130 \text{ feet}$$

## Question:

What is the internal surface area of a cylindrical tank (bottom, top, and the cylinder wall), if it is 125.0 ft in diameter and 48.5 ft high



### **Top = Area 1**

$$\text{Area 1} = 0.785 * \text{dia}^2$$

$$\text{Area 1} = 0.785 \times (125 \text{ ft})^2$$

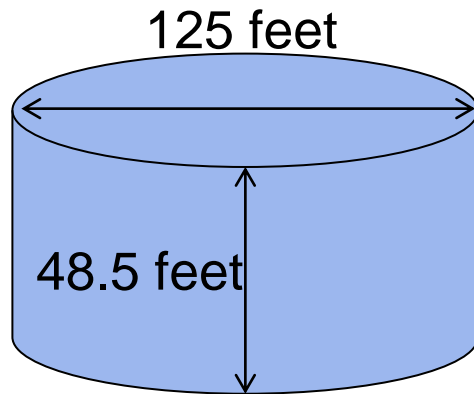
$$\text{Area 1} = 12,265 \text{ sq ft}$$

$$\text{Top \& Bottom} = 2 \times 12,265 \text{ sq ft}$$

$$\text{Top \& Bottom} = 24,530 \text{ sq ft}$$

## Question:

What is the internal surface area of a cylindrical tank (bottom, top, and the cylinder wall), if it is 125.0 ft in diameter and 48.5 ft high



### ***Cylinder wall = Area 2***

Area 2 = circumference x ht

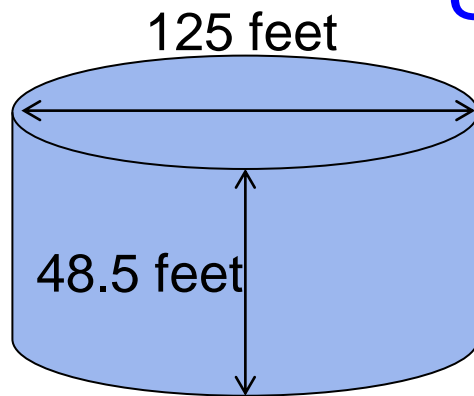
Area 2 =  $\Pi$  x diameter x ht

Area 2 =  $3.14 \times 125 \times 48.5$

Area 2 = 19,036 sq ft

## Question:

What is the internal surface area of a cylindrical tank (bottom, top, and the cylinder wall), if it is 125.0 ft in diameter and 48.5 ft high



$$\begin{aligned} \text{Surface area} &= 2 \times \text{Area1} + \text{Area2} \\ &= 24,530 \text{ sq ft} + 19,036 \text{ sq ft} \\ &= 43,566 \text{ sq ft} \end{aligned}$$

43,600 sq ft

# Pressure

*Often the limiting factor*

## Question:

What is the pounds per square inch pressure at the bottom of a tank, if the water level is 38.29 ft.?



*Photo from City of Marysville*



## Question:

What is the pounds per square inch pressure at the bottom of a tank, if the water level is 38.29 ft.?

$$1 \text{ foot of water} = 0.433 \text{ psi}$$

$$38.29 \text{ ft} * 0.433 \text{ psi / ft water} = 16.6 \text{ psi}$$

$$16.6 \text{ psi} \sim 17 \text{ psi}$$

## Question:

The pressure at a fire hydrant is 171 feet. What is the pressure in pounds per square inch (psi)?



*Photo from City of Palm Springs*

## Question:

The pressure at a fire hydrant is 171 feet. What is the pressure in pounds per square inch (psi)?

$$= 171 \text{ ft} / 2.31 \text{ psi/ ft}$$

74 psi

## Question:

What is the pressure head at a fire hydrant in feet, if the pressure gauge reads 121 psi



*Photo by Jeff Lundt*

## Question:

What is the pressure head at a fire hydrant in feet, if the pressure gauge reads 121 psi

$$1 \text{ foot of water} = 0.433 \text{ psi}$$

$$121 \text{ psi} / 0.433 \text{ psi} / \text{ft water} = 279.45 \text{ ft}$$

$$\sim 280 \text{ ft}$$

## Question:

Determine the pressure in psi at the bottom of an alum storage tank if the tank's level is 8.95 feet and alum density is 11.32 lb / gallon



*Photo from DN Tanks*

## Question:

Determine the pressure in psi at the bottom of an alum storage tank if the tank's level is 8.95 feet and alum density is 11.32 lb / gallon

Pressure is the weight of the fluid above the point of measurement

$$11.32 \text{ lb/gallon} \times 7.48 \text{ gallons/cf} = 84.67 \text{ lb/cf}$$

$$8.95 \text{ feet} \times 84.67 \text{ lb/cf} = 757.8 \text{ lb/sf}$$

$$757.8 \text{ lb/sf} / 144 \text{ in}^2/\text{sf} = 5.2625 \text{ lb/in}^2 \text{ or psi}$$

$$5.26 \text{ psi}$$

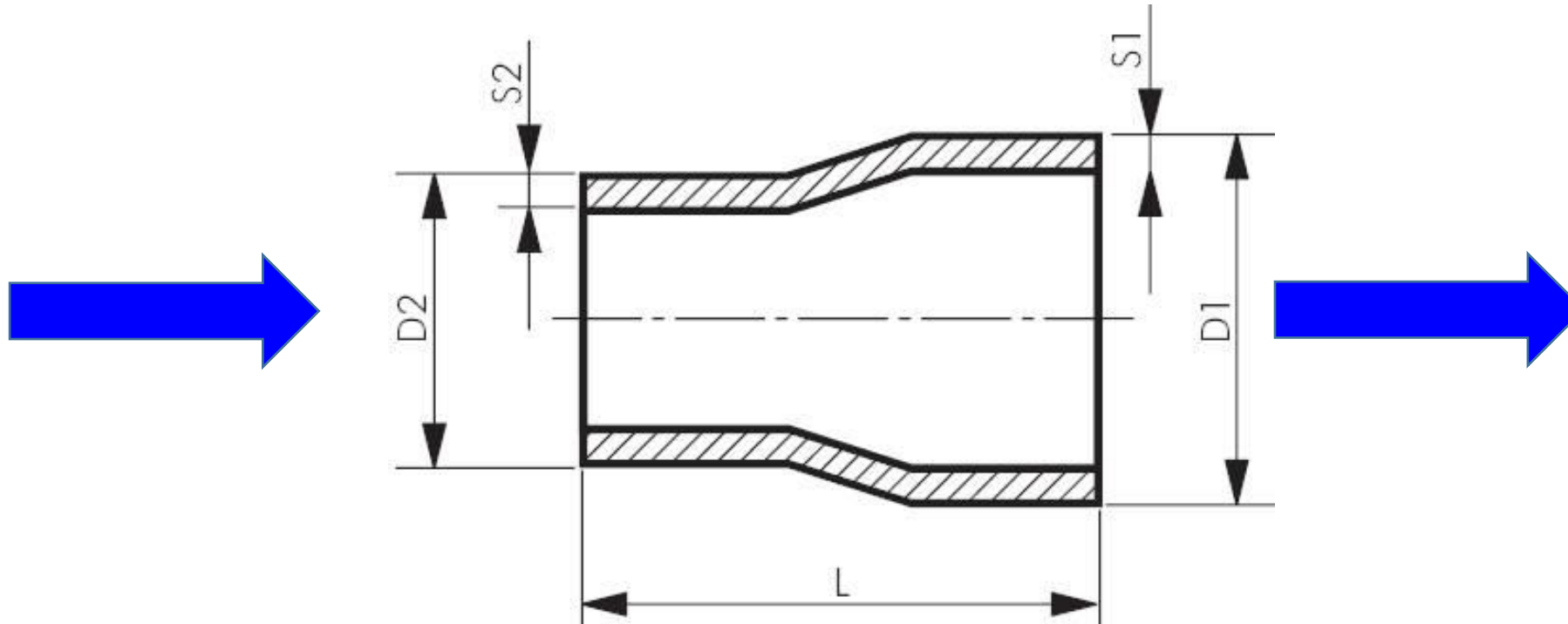
# Rates of Velocity & Flow

*How fast?*



## Question:

Water flows at a velocity of 3.75 fps in a 10-in. diameter pipe. If the pipe changes from the 10-in. to a 12-in. pipe, what will the velocity be in the 12-in. pipe?



## Question:

Water flows at a velocity of 3.75 fps in a 10-in. diameter pipe. If the pipe changes from the 10-in. to a 12-in. pipe, what will the velocity be in the 12-in. pipe?

*Use the ratio of the areas (w/o pi & constant)*

$$10^2 / 12^2 = 100 / 144 = 0.694$$

$$3.75 \text{ fps} \times 0.694 = 2.60 \text{ fps}$$

2.6 fps

## Question:

Water is flowing in a pipeline at a rate of 2.65 cu/ft per sec. What is the flow rate in gallons per min.?

## Question:

Water is flowing in a pipeline at a rate of 2.65 cu.ft. per sec. What is the flow rate in gallons per min.?

$$2.65 \text{ cfs} \times 7.48 \text{ gal/cf} \times 60 \text{ sec/min.} = \\ 1,189.3 \text{ gpm}$$

1,190 gpm

## Question:

An 18-inch diameter distribution pipe delivers 988,000 gallons in 24 hours. What is the average velocity during the 24 hour period in feet / second?



*Photo from 123RF.com*

## Question:

An 18-inch diameter distribution pipe delivers 988,000 gallons in 24 hours. What is the average flow during the 24 hour period in feet / second?

$$(18 \text{ inches} / 12 \text{ inch} / \text{ft})^2 \times \text{PI} / 4 = 1.77 \text{ sf}$$

$$24 \text{ hr} \times 60 \text{ min} / \text{hr} \times 60 \text{ sec} / \text{min} = 86,400 \text{ sec}$$

$$988,000 \text{ gal} / 7.48 \text{ ft}^3 / \text{gal} = 132,085.6 \text{ ft}^3$$

$$132,085.6 \text{ ft}^3 / 1.77 \text{ sf} / 86,400 \text{ sec} =$$

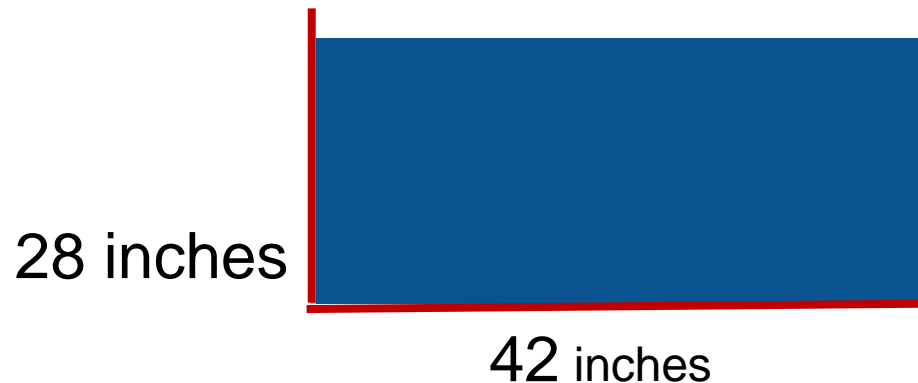
$$0.87 \text{ ft} / \text{sec}$$

## Question:

A rectangular section channel is 42" wide and the water is a depth of 28". You toss a float in and determine that it travels 30 feet in 15 seconds. What is the flow rate in ft<sup>3</sup>/sec? gpm?

*Dimensions in inches, change to feet*

Flow = Velocity x Area



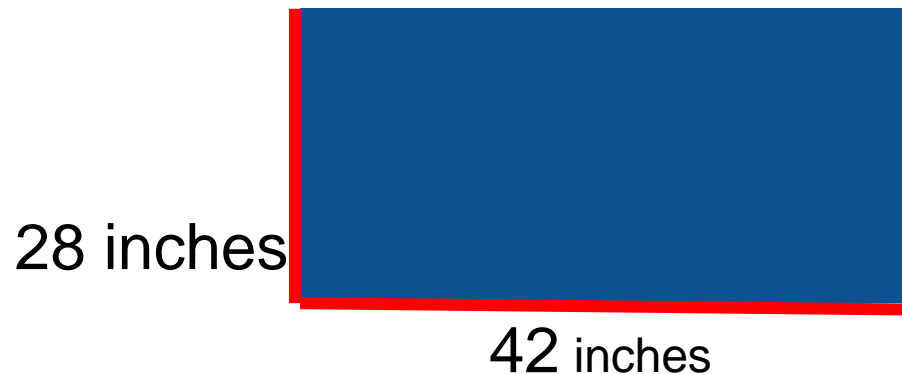
$$\text{Width} = \frac{42 \text{ in} \left| \frac{1 \text{ ft}}{12 \text{ in}} \right.}{12 \text{ in}} = 3.5 \text{ ft}$$

$$\text{Depth} = \frac{28 \text{ in} \left| \frac{1 \text{ ft}}{12 \text{ in}} \right.}{12 \text{ in}} = 2.3 \text{ ft}$$

## Question:

A channel is 42" wide and the water is a depth of 28". You toss a float in and determine that it travels 30 feet in 15 seconds. What is the flow rate in ft<sup>3</sup>/sec? gpm?

***Flow = Velocity x Area***



$$\begin{aligned} \text{Area} &= 2.3 \text{ ft} \times 3.5 \text{ ft} \\ \text{Area} &= 8.05 \text{ sq ft} \end{aligned}$$

$$\text{Velocity} = \frac{30 \text{ feet}}{15 \text{ seconds}} = 2 \text{ fps}$$

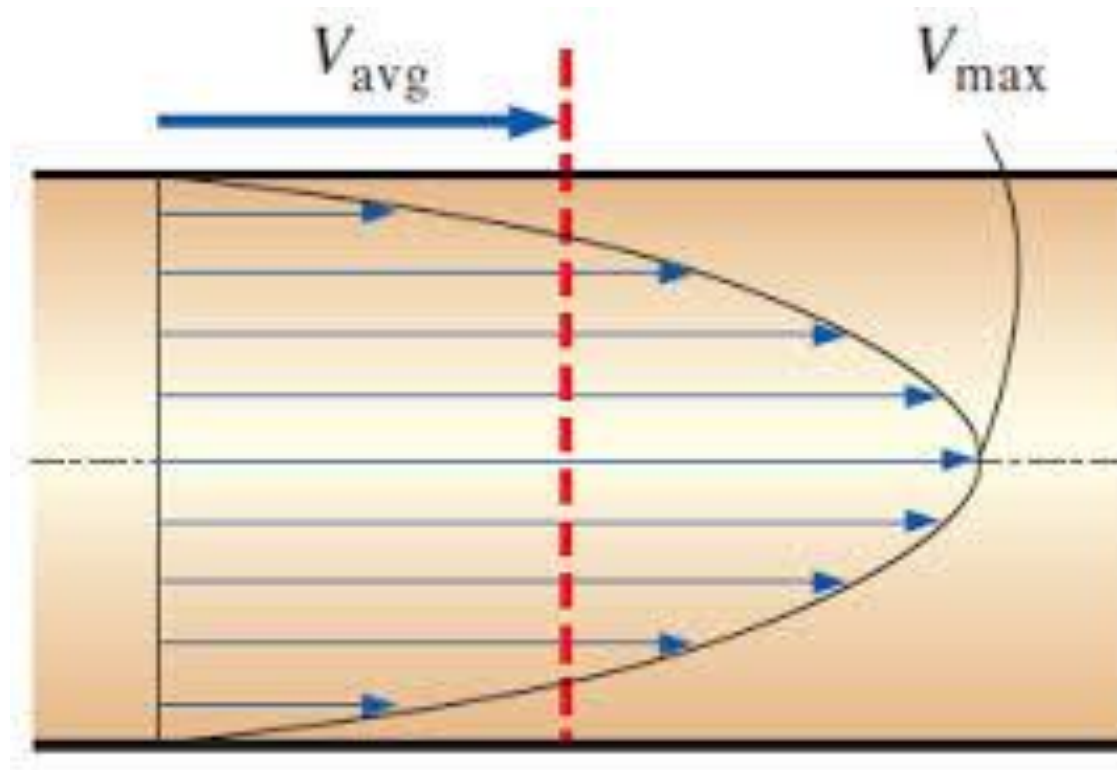
$$\text{Flow} = 2 \text{ fps} \times 8.05 \text{ sq ft}$$

$$\underline{\underline{\text{Flow rate} = 16.1 \text{ cfs}}}$$



## Question:

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?



Graphic from [drive.uqu.edu.sa](http://drive.uqu.edu.sa)

**Question:**

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?

$$\text{Flow (Q)} = \text{Velocity} \times \text{Area}$$

$$\begin{aligned} 8 \text{ inches} &= 8/12 \text{ foot} \\ &= .67 \text{ foot} \end{aligned}$$

$$600 \text{ gpm} = \text{Velocity} \times (.67 \text{ ft})^2 \times .785$$

**Question:**

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?

$$\text{Flow (Q)} = \text{Velocity} \times \text{Area}$$

$$\begin{aligned} 8 \text{ inches} &= 8/12 \text{ foot} \\ &= .67 \text{ foot} \end{aligned}$$

$$600 \text{ gpm} = \text{Velocity} \times (.67 \text{ ft})^2 \times .785$$



$$\frac{600 \text{ gpm}}{(.67 \text{ ft})^2 \times .785} = \frac{\text{Velocity} \times (.67 \text{ ft})^2 \times .785}{(.67 \text{ ft})^2 \times .785}$$

**Question:**

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?

$$\text{Flow (Q)} = \text{Velocity} \times \text{Area}$$

$$600 \text{ gpm} = \text{Velocity} \times (.67 \text{ ft})^2 \times .785$$



$$\frac{600 \text{ gpm}}{(.67 \text{ ft})^2 \times .785} = \frac{\text{Velocity} \times (.67 \text{ ft})^2 \times .785}{(.67 \text{ ft})^2 \times .785}$$



$$\frac{600 \text{ gal}}{\text{min}} \left| \frac{1 \text{ cu ft}}{7.48 \text{ gal}} \right. = 80.2 \text{ cfm}$$

**Question:**

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?

$$\text{Flow (Q)} = \text{Velocity} \times \text{Area}$$

$$600 \text{ gpm} = \text{Velocity} \times (.67 \text{ ft})^2 \times .785$$



$$\frac{600 \text{ gpm}}{(.67 \text{ ft})^2 \times .785} = \frac{\text{Velocity} \times (.67 \text{ ft})^2 \times .785}{(.67 \text{ ft})^2 \times .785}$$



$$\frac{600 \text{ gal}}{\text{min}} \left| \frac{1 \text{ cu ft}}{7.48 \text{ gal}} \right. = 80.2 \text{ cfm} \rightarrow \frac{80.2 \text{ cu ft}}{\text{min}} \left| \frac{1 \text{ min}}{60 \text{ sec}} \right. = 1.3 \text{ cfs}$$

## Question:

An 8-inch diameter pipe is flowing full at 600 gpm, what is the velocity in ft/sec?

$$\text{Flow (Q)} = \text{Velocity} \times \text{Area}$$

$$600 \text{ gpm} = \text{Velocity} \times (.67 \text{ ft})^2 \times .785$$



$$\frac{600 \text{ gpm}}{(.67 \text{ ft})^2 \times .785} = \frac{\text{Velocity} \times (.67 \text{ ft})^2 \times .785}{(.67 \text{ ft})^2 \times .785}$$



$$\frac{600 \text{ gal}}{\text{min}} \times \frac{1 \text{ cu ft}}{7.48 \text{ gal}} = 80.2 \text{ cfm} \rightarrow \frac{80.2 \text{ cu ft}}{\text{min}} \times \frac{1 \text{ min}}{60 \text{ sec}} = 1.3 \text{ cfs}$$

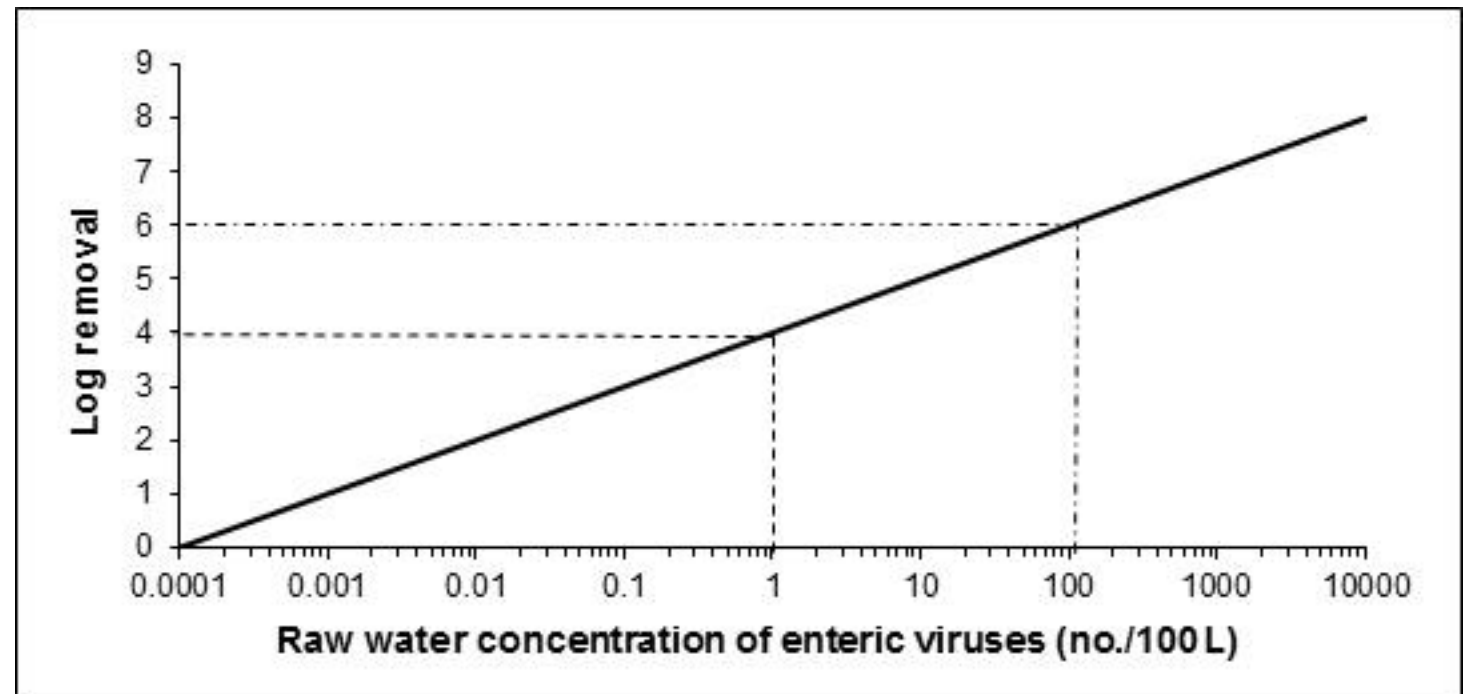
$$\frac{1.3 \text{ cfs}}{(.67 \text{ ft})^2 \times 0.785} = \text{Velocity} = \mathbf{3.7 \text{ ft/sec}}$$

# Chemicals & Process

*More of the same but with a twist*

## Question:

Calculate the log removal for a water treatment plant if the samples show a raw water coliform count of 295/100 ml (through extrapolation) and the finished water shows 2/100 ml?



*Graphic from Health Canada*



## Question:

Calculate the log removal for a water treatment plant if the samples show a raw water coliform count of 295/100 ml (through extrapolation) and the finished water shows 2/100 ml?

$$295 / 2 = 147.5$$

$$\text{Log}_{10} (147.5) = 2.1688 \sim 2.2$$

2.2 log removal

## Question:

A 10 foot inside diameter chemical tank drops 4.31 inches in exactly 3 hours. What's the pumping rate for the chemical in gpm?



*Photo from City of Anacortes*

## Question:

A 10 foot inside diameter chemical tank drops 4.31 inches in exactly 3 hours. What's the pumping rate for the chemical in gpm?

$$10 \text{ ft}^2 \times \Pi / 4 = 78.53 \text{ sf}$$

$$4.31 \text{ inches} / 12 \text{ inches} / \text{ft} = 0.3592 \text{ ft}$$

$$78.53 \text{ sf} \times 0.3592 \text{ ft} \times 7.48 \text{ gal} / \text{ft}^3 = 210.98 \text{ gal.}$$

$$210.98 \text{ gal} / 3 \text{ hr} / 60 \text{ min./hr} = 1.17 \text{ gpm}$$

$$1.17 \text{ gpm}$$

## Question:

How many pounds per day of 65% calcium hypochlorite are required for maintaining a 2.5 mg/l dosage for a 2,575 gpm treatment plant?



*Photo from Kemcore*

## Question:

How many pounds per day of 65% calcium hypochlorite are required for maintaining a 2.5 mg/l dosage for a 2,575 gpm treatment plant?

$$2.5 \text{ mg / L} / 0.65\% = 3.85 \text{ mg calcium hypo / L}$$

$$3.85 \text{ mg/ L} / 1000 \text{ mg / g} / 1000 \text{ g / kg} \times 2.2 \text{ lb / kg} / 0.264 \text{ L / gallon} = 3.45 \times 10^{-5} \text{ lb / gallon}$$

$$2,575 \text{ gpm} \times 60 \text{ min/hr} \times 24 \text{ hr/day} = 3.71 \times 10^6 \text{ gpd}$$

$$3.71 \times 10^6 \text{ gpd} \times 3.45 \times 10^{-5} \text{ lb / gallon}$$

$$120 \text{ lb / day}$$

## Question:

Determine the percent mineral rejection from a reverse osmosis plant if the feedwater contains 1,230 mg/l total dissolved solids (TDS) and the product water contains 135 mg/l TDS.



*Photo from Seattle Yacht Club,  
Henry Island*

## Question:

Determine the percent mineral rejection from a reverse osmosis plant if the feedwater contains 1,230 mg/l total dissolved solids (TDS) and the product water contains 135 mg/l TDS.

$$(1 - (135\text{mg/l} / 1,230 \text{ mg/l})) = 0.8902 \times 100 \\ = 89.02\%$$

*Note all the units are the same and cancel (mg/l) so we get a unitless number as a ratio and assign % to it.*

~89 percent

## Question:

How many pounds of chlorine gas are necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L?



*Photo from City of Anacortes*



# Davidson Pie Chart Examples – Chemical Dosing

YouTube Link:

[Water Math: Basic Dosage Questions For Treatment \(youtube.com\)](#)

[Water Math: Advanced Dosage Questions For Treatment \(youtube.com\)](#)

## Basic Dosage Questions

How many pounds of chlorine gas must be added to disinfect a storage tank with a capacity of 1,600,000 gallons for a dose of 18 mg/L?

LBS

---

MG/LMGD

8.34

Figure 1.0 Davidson's Pie Chart

Play (k)

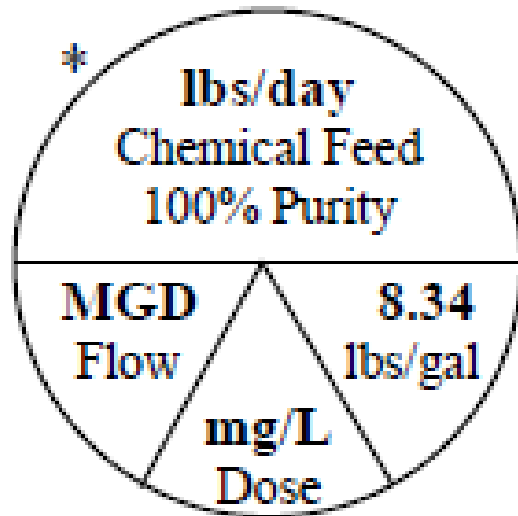
0:06 / 4:38

1  
3

## Question:

How many pounds of chlorine gas are necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



$$\text{Pounds} = \frac{4 \text{ MG} * 2 \text{ mg/l} * 8.34 \text{ lbs/gal}}{1.0 \text{ purity}}$$

Answer is 67 lb

## Question:

A 1.81 MG reservoir is being disinfected with a chlorine dosage of 9.75 mg/l. If the sodium hypochlorite is 11.5% available chlorine, how many pounds are needed?

Answer Time!



*Photos from Roche Harbor & Silver Lake Water & Sewer District*

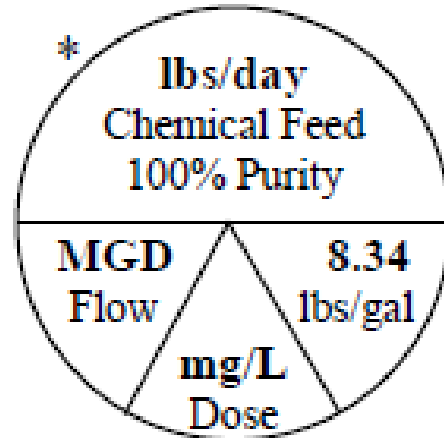


## Question:

A 1.81 MG reservoir is being disinfected with a chlorine dosage of 9.75 mg/l. If the sodium hypochlorite is 11.5% available chlorine, how many pounds are needed?

*Use the wheel!*

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



$$= \frac{1.81 \text{ MG} \times 9.75 \text{ mg/l} \times 8.34 \text{ lb/gallons}}{0.115 \text{ (Purity in decimal)}}$$

$$= 1280 \text{ lbs}$$

## Question:

How many pounds of 12.5% sodium hypochlorite is necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L?

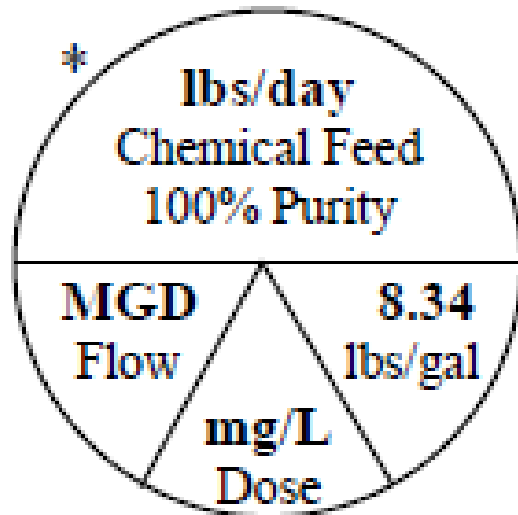


*Photo from City of Marysville*

## Question:

How many pounds of 12.5% sodium hypochlorite is necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



$$\text{Pounds} = \frac{4 \text{ MG} * 2 \text{ mg/l} * 8.34 \text{ lbs/gal}}{0.125 \text{ purity}}$$

Answer is 534 lb (533.76)

## Question:

How many pounds of 0.8% onsite generated sodium hypochlorite are necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L?

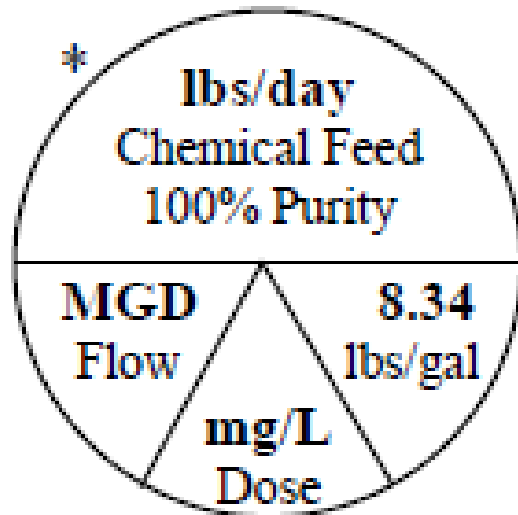


*Photo from City of Marysville*

## Question:

How many pounds of chlorine gas are necessary to treat 4,000,000 gallons of water at a dosage of 2 mg/L

$$\text{Feed Rate, lbs/day} = \frac{(\text{Dosage, mg/L})(\text{Capacity, MGD})(8.34 \text{ lbs/gal})}{(\text{Purity, decimal percentage})}$$



$$\text{Pounds} = \frac{4 \text{ MG} * 2 \text{ mg/l} * 8.34 \text{ lbs/gal}}{0.008 \text{ purity}}$$

Answer is 8,340 lb (= 1,115 gallons)



# Questions, Comments and Suggestions?



American Water Works Association  
**Pacific Northwest** Section

*Prepared by the Training Coordination  
Committee, PNWS-AWWA*